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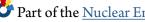
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# Techniques for Active 3He Activation Analysis for Carbon and Oxygen

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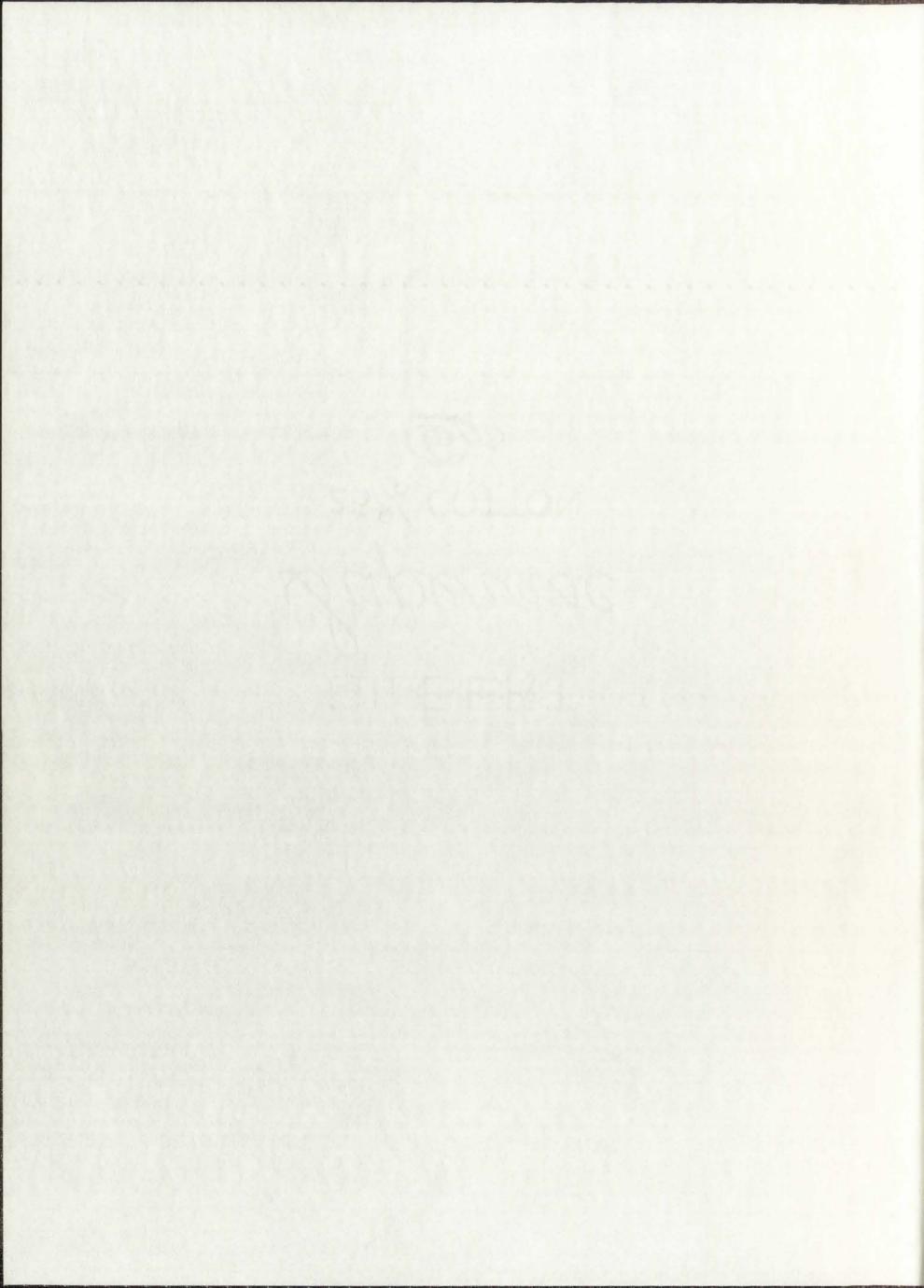
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LD 3781 N584Se562 wp. 2 ACTIVE <sup>3</sup>HE ACTIVATION ANALYSIS

SANDERS



# THE UNIVERSITY OF NEW MEXICO ALBUQUERQUE, NEW MEXICO 87106

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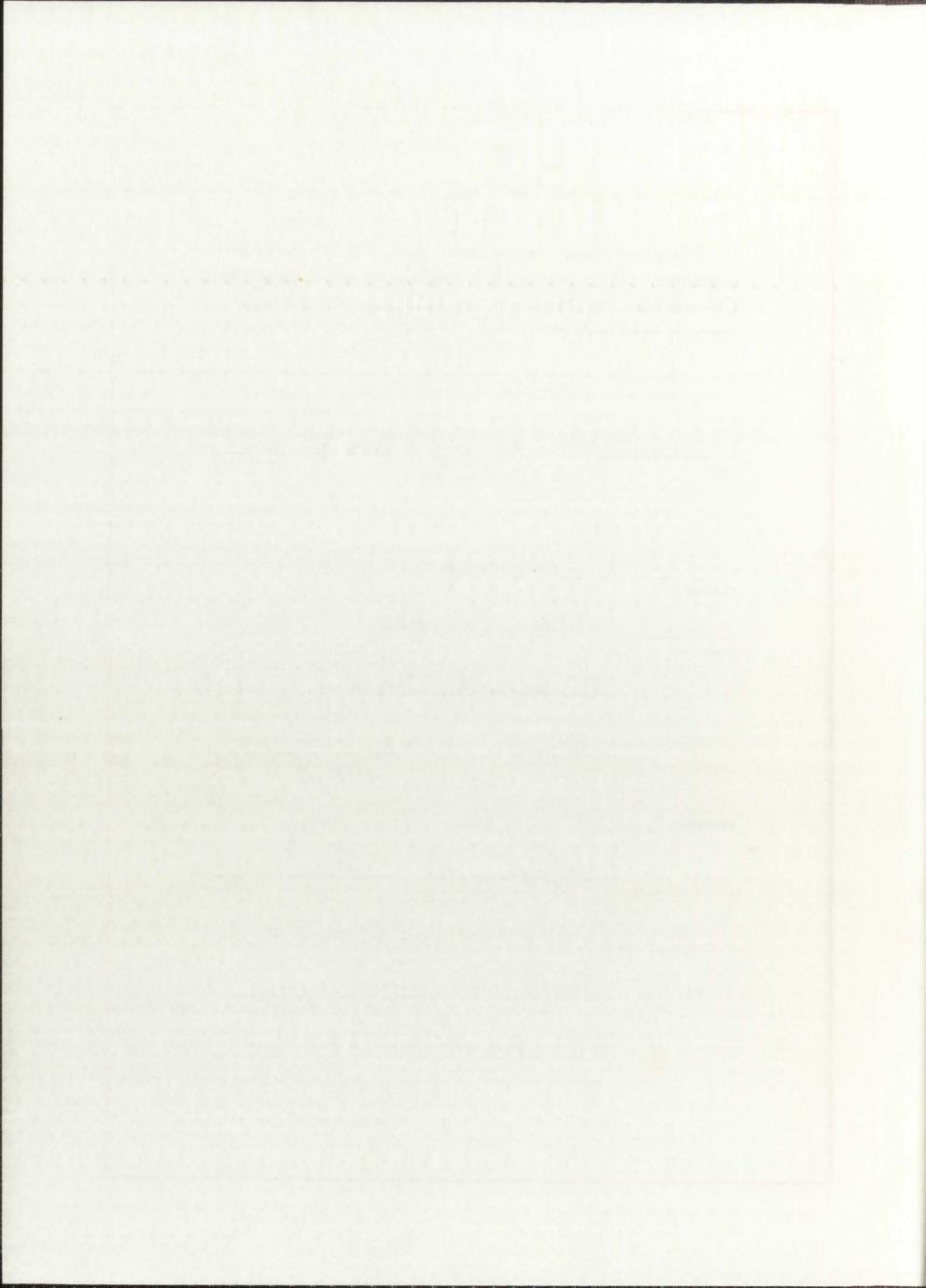
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This dissertation, directed and approved by the candidate's committee, has been accepted by the Graduate Committee of The University of New Mexico in partial fulfillment of the requirements for the degree of

-	DOCTOR OF PHILOSOPHY
TECHNI	QUES FOR ACTIVE <sup>3</sup> He ACTIVATION ANALYSIS
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# TECHNIQUES FOR ACTIVE <sup>3</sup>He ACTIVATION ANALYSIS FOR CARBON AND OXYGEN

#### BY WM. MORT SANDERS

B.S., Kansas State University, 1961 M.S., University of New Mexico, 1966

#### DISSERTATION

Submitted in Partial Fulfillment of the
Requirements for the Degree of
Doctor of Philosophy in Nuclear Engineering
in the Graduate School of
The University of New Mexico
Albuquerque, New Mexico
December, 1971

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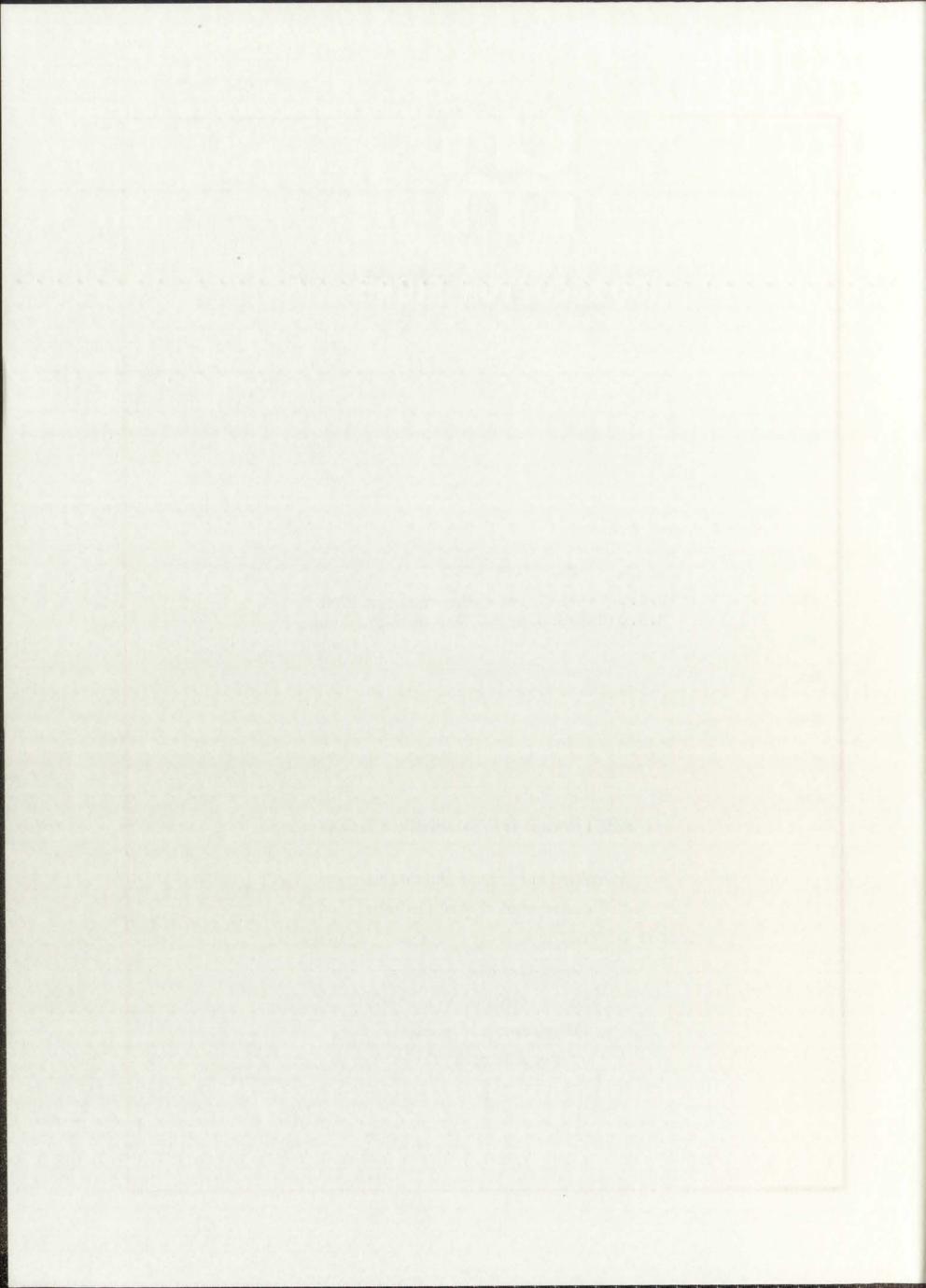
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December, 1971



#### ABSTRACT

The surface and body concentrations of carbon and oxygen have been measured in various materials using <sup>3</sup>He activation. Channeling techniques have been used to differentiate between interstitial and substitutional location of these impurities.

Thin target excitation functions were determined for (<sup>3</sup>He,p) reactions with carbon and oxygen over a <sup>3</sup>He energy range from 2.5 to 9.0 MeV. These data were used to calculate the activation curves for various combinations of incident particle energy, impurity distributions, and material.

Information on several computer codes used during this study is presented.

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#### CHAPTER I

#### INTRODUCTION

Carbon and oxygen, two common low-Z impurities that are found in metals and semiconductors, can influence the behavior of these materials. For example, oxygen impurities greatly affect the manufacture of large Ge(Li) detectors from germanium (Ref. 1). Techniques need to be developed that will allow the experimenter to determine the distribution and concentration of these impurities in materials. The <sup>3</sup>He-induced nuclear reactions with carbon and oxygen and their subsequent reaction products present several ways of studying the distributions and concentrations of these impurities. These include the prompt emission of charged particles, the prompt emission of gamma rays, and the delayed positron and gamma-ray emission of the reaction products. In general, nuclear reactions are not sensitive to the chemical composition of the impurity and can be quite selective if the proper reaction and irradiation parameters are used.

The <sup>3</sup>He reactions and other charged-particle reactions have been used by many experimenters in activation analysis work (Refs. 2-6). The coulomb electrostatic repulsion of high-Z nuclei effectively prevents interaction between them and the <sup>3</sup>He particles. Thus, small concentrations of low-Z impurities, which do allow nuclear interactions, may be studied in the presence of large amounts of high-Z materials. The classical coulomb barrier vs the atomic number is shown in Fig. 1. It should be noted, however, that some activation is obtained at particle energies below the classical barrier due to tunneling effects.

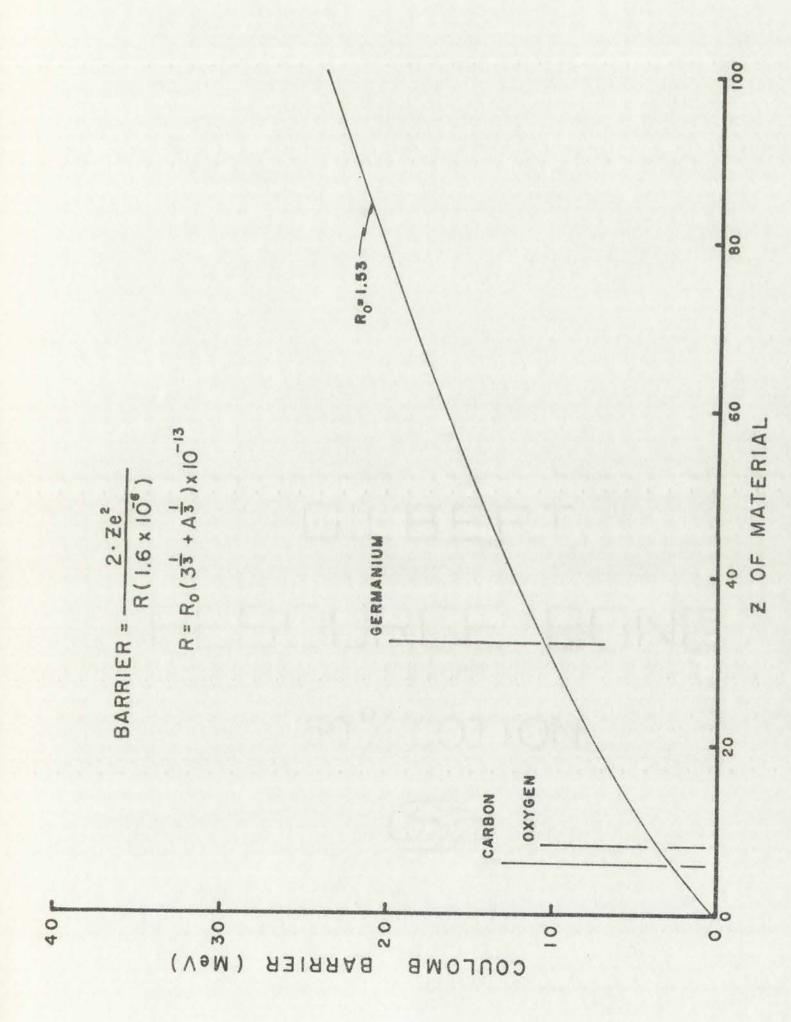
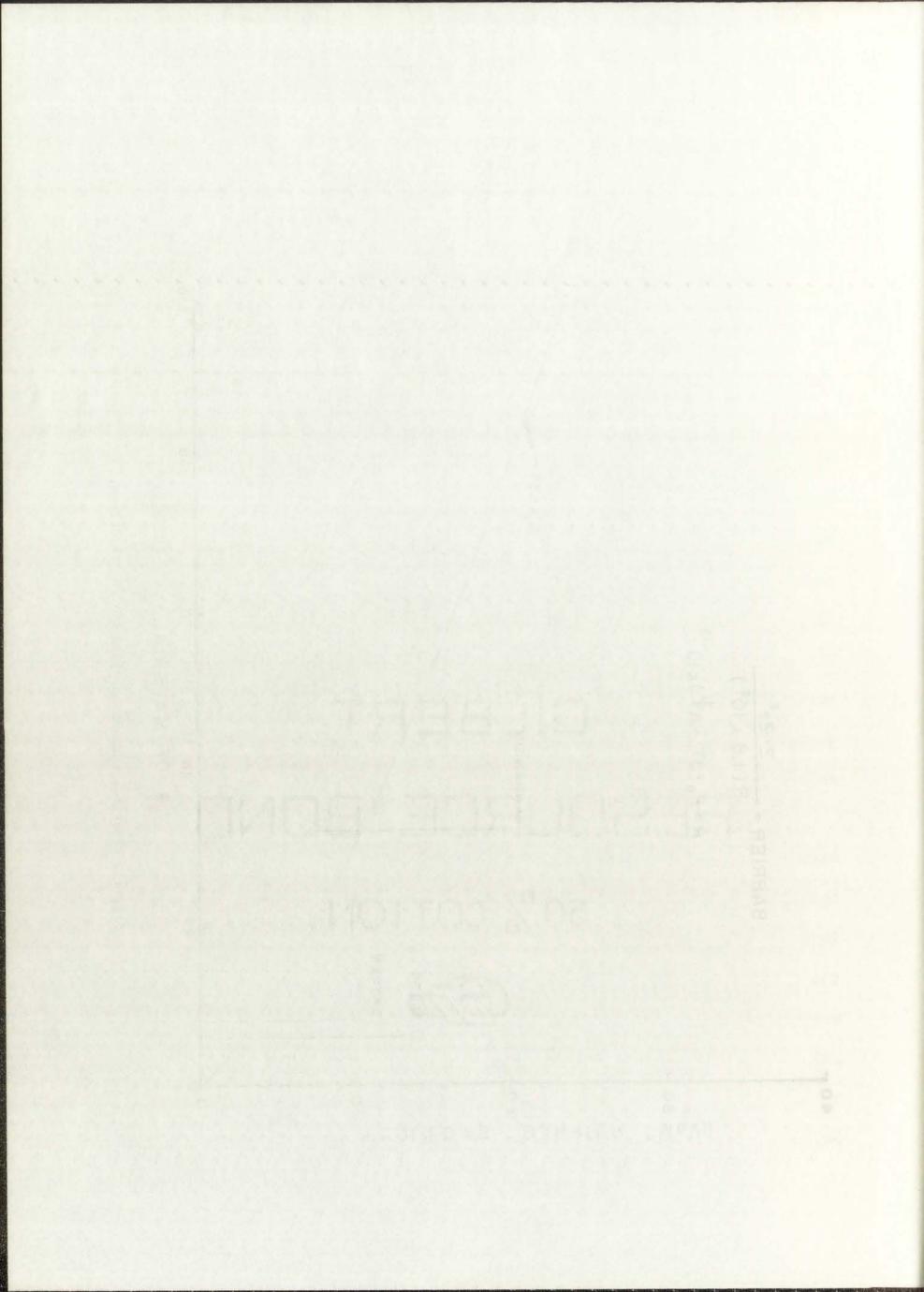


Fig. 1. Classical coulomb barriers for 3He reactions.

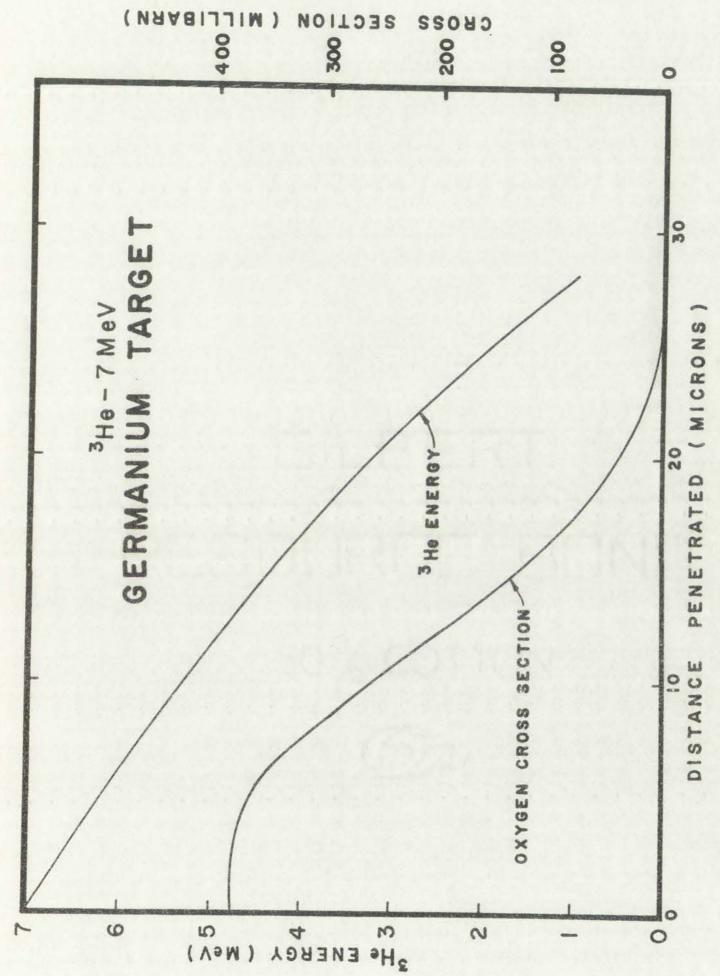


There are several other reasons why <sup>3</sup>He is attractive for studying low-Z impurities in a high-Z matrix or substrate:

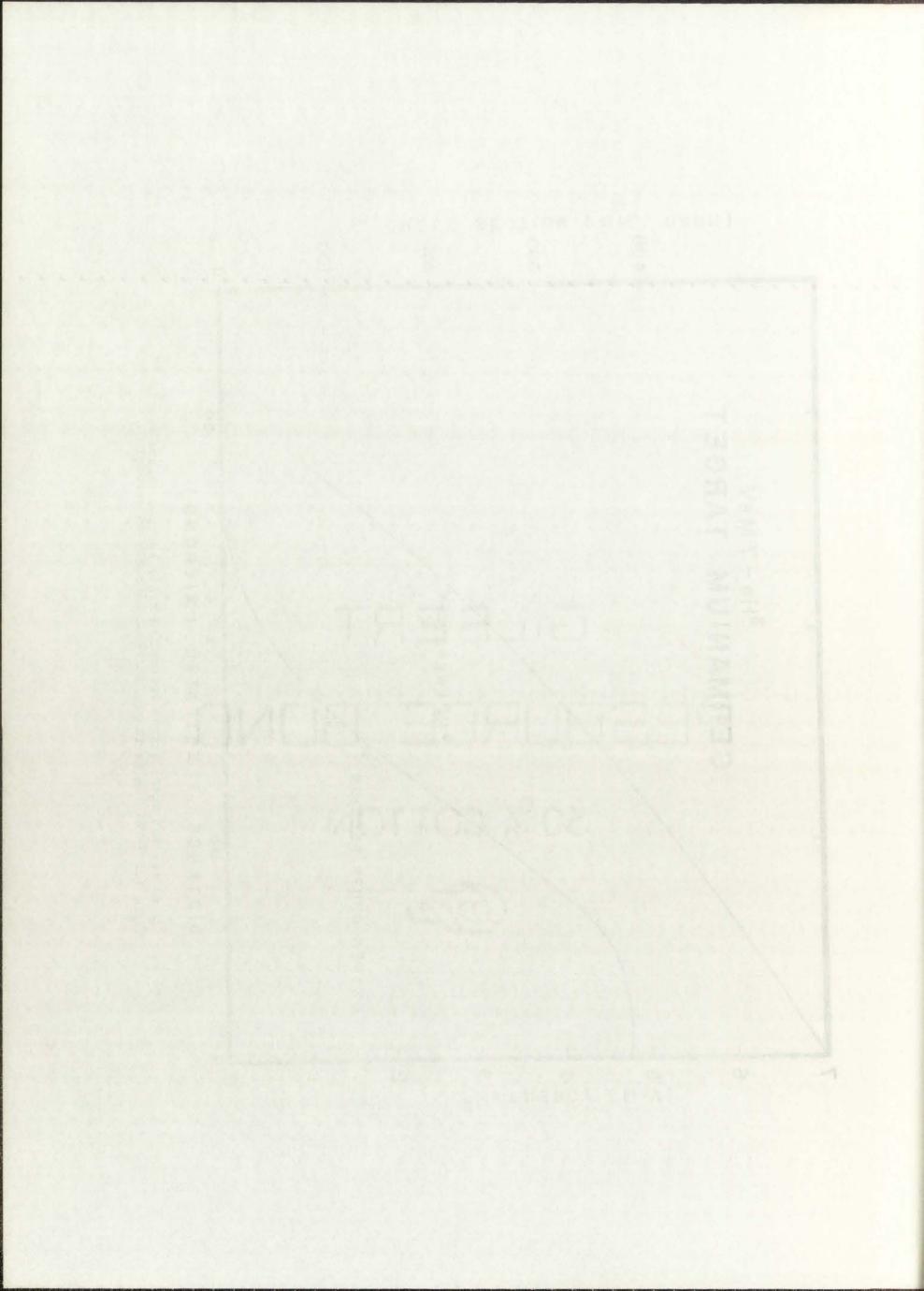
- 3. He does not have an excess of neutrons; therefore, complicating secondary reactions from (<sup>3</sup>He,n) reactions are not common as for (d,n) and (t,n) reactions;
- 2. <sup>3</sup>He has a low binding energy that leads to energetic reactions in which the reaction products have high kinetic energies;
- 3. The short range of the <sup>3</sup>He particles makes them particularly suitable for measuring surface concentrations and distributions. However, this may be a detriment if one is interested in measuring the bulk concentration of the impurity and the distribution of the impurity is not uniform throughout the material; and
- 4. The background associated with the prompt charged-particle activation analysis techniques is extremely low.

The total  $^{16}$ O to  $^{18}$ F cross section and the average  $^3$ He energy vs sample penetration are shown in Fig. 2 for a 7 MeV  $^3$ He irradiation of germanium in a nonchanneling orientation. Recoil and energy straggling effects have been ignored. The cross section has decreased to half its peak value at 10  $\mu$ . There is essentially no activation at sample depths exceeding 25  $\mu$ .  $^3$ He activation and autoradiographic techniques have been used for studying the surface concentrations and distributions of carbon and oxygen on various materials (Ref. 7). Similar activation techniques were used to determine the carbon gradient from a carburized stainless steel sample (Ref. 8).

Variations in the surface distributions and surface gradients can cause discrepancies in activation analysis results with charged particles.



<sup>3</sup>He energy and total oxygen activation cross section versus sample depth for 7-MeV <sup>3</sup>He particles incident randomly on germanium. Fig. 2.



References 6 and 8 above show that the carbon and oxygen can be preferentially concentrated at grain boundaries or surface defects in the material. This can cause a large variation in results if the irradiated area or volume is small.

The existence of large gradients in the concentration of the impurity from the surface of the material or discontinuities from surface layers can cause extraneous results if these are not considered in the analysis of the data. If the sample oxidizes readily, as is the case for germanium, surface oxide layers may be present during the irradiation. For passive analyses, these can be removed by either chemical or mechanical means after the bombardment. However, it is difficult to remove precisely a given amount from the surface; and, if the range of the incident particle is small, as is the case for <sup>3</sup>He, the error introduced can be quite large. If the matrix is a single-crystal or polycrystalline material, channeling of the recoil impurity atoms from the surface layer into the matrix material may increase their range so that the heavy ions travel distances comparable with those traveled by the incident particle (Ref. 9). These displaced surface atoms will cause extraneously high results.

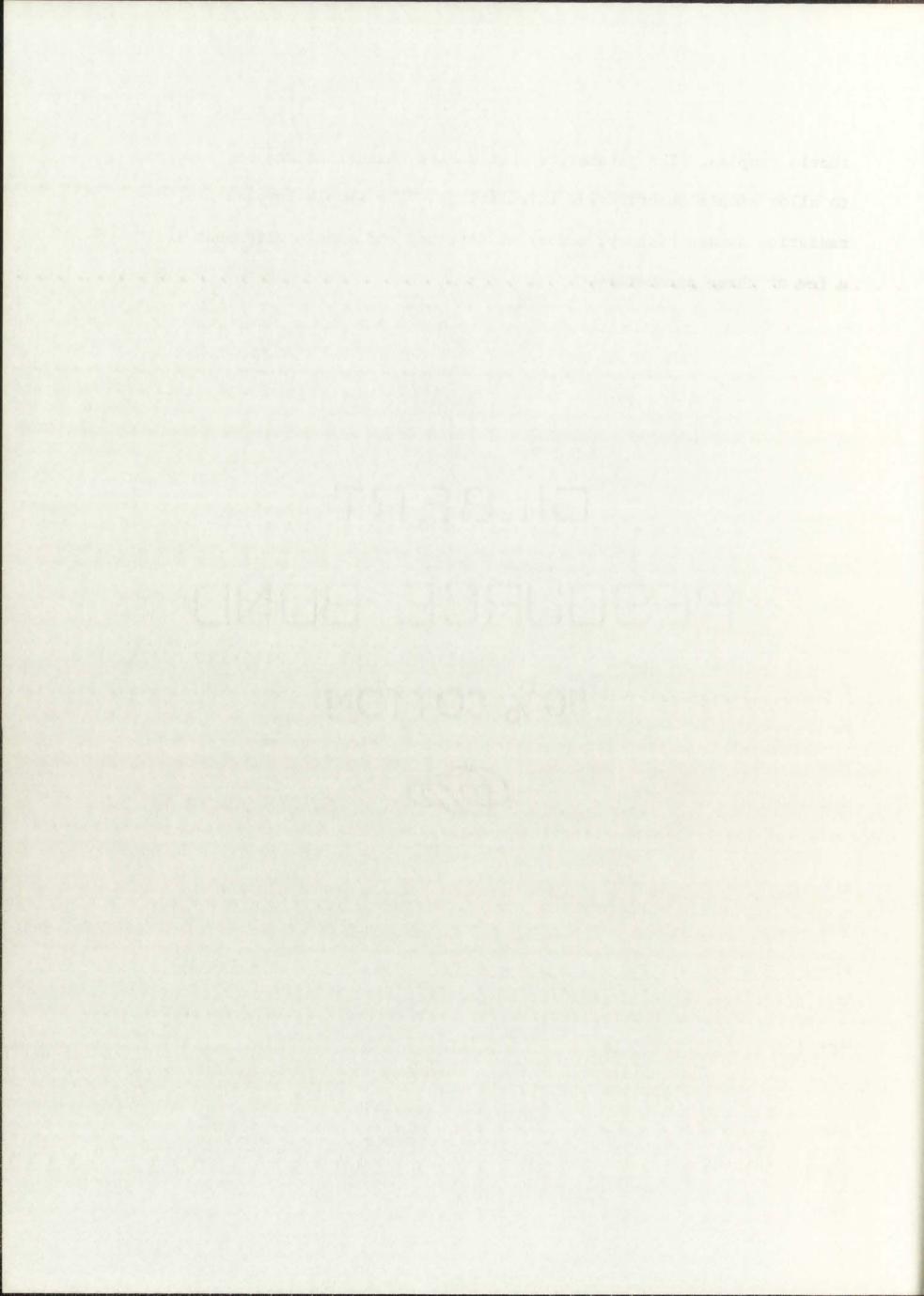
The techniques presented in this paper solve some of these problems. The samples were bombarded with <sup>3</sup>He particles, and the energy spectrum from the reaction protons was recorded after the protons had passed through an absorber to remove the backscattered <sup>3</sup>He ions. The range of the heavy recoil reaction products was immaterial. From the kinematics of the reaction, the cross sections of the reaction, and the absorber thickness, the proton spectrum and the sample depths that correspond to the proton energies can be calculated. Therefore, from the proton spectra, information about the distribution of the impurity atoms in the beam direction can be determined.

In reality, the activation curve or detector response is a function of the matrix material, the incident particle energy, the detector geometry, the impurity cross sections, and the distribution of the impurity on or in the matrix. In order to have the capability of calculating the detector response for various materials and distributions of the impurity atoms in these materials at various 3He energies, the thin target excitation functions had to be determined. Knowing the thin target excitation functions, one can calculate the activation curves or detector response for any matrix for which the stopping-power data can be calculated and for any 3He energies for which the excitation functions have been determined. Other methods of analyzing charged-particle activation data are the "equivalent thickness" method (Ref. 10) and the transform technique (Ref. 11). Neither of these techniques has the flexibility of the method presented in this paper. The "equivalent thickness" method is based on an established activation curve for a given reaction in a given material. The second method transforms a well-determined activation curve, using the different stopping powers, for use with different experimental cases.

The largest uncertainty in the method presented in this paper is the effect that energy straggling of the <sup>3</sup>He particles and of the protons in the sample and foil may have on the final resolution of the proton energy spectrum. This has been empirically resolved by defining a Gaussian resolution function whose width is a function of the proton energy of the reaction and the proton energy at the detector.

Qualitative information on the location of impurities in crystal matrices can be obtained if the sample is oriented so that the incident particles channel between the rows and planes of the structure (Ref. 12). Several such irradiations were performed on single-crystal germanium and

thoria samples. The parameters that affect channeling are too numerous to allow simple quantitative calculations. The sample temperature, irradiation damage history, number of defects, and sample alignment are a few of these parameters.



#### CHAPTER II

#### EXPERIMENTAL PROCEDURE

### Introduction

The <sup>3</sup>He irradiations were performed on the Los Alamos vertical Van de Graaff accelerator with particle energies ranging from 2.6 to 9.0 MeV. Doubly ionized <sup>3</sup>He was accelerated exclusively to prevent possible contamination of the beam from <sup>3</sup>T<sup>+</sup> and <sup>3</sup>(HD)<sup>+</sup> which might be present in the source but could not be separated by the magnet since they have the same charge-to-mass ratio as singly ionized <sup>3</sup>He. The <sup>3</sup>He<sup>++</sup> target currents were below 500 nA and were typically about 100 nA. These low target currents were due to the high beam collimation.

Anodized tantalum was used for the "thin" oxygen samples, and carbon evaporated on tantalum was used for the "thin" carbon samples. In addition to these, thick  ${\rm Ta}_2{\rm O}_5$ , carbon, and germanium samples were irradiated.

Pulse-height distributions of the prompt gamma rays and prompt protons from <sup>3</sup>He-induced nuclear reactions in these materials were recorded and analyzed. In addition, passive analyses of the delayed positron decay were made. Germanium samples were irradiated in channeling and non-channeling orientations to determine the effects of channeling in crystal-line materials on activation-type analyses.

## Sample Preparations

The "thin" oxygen and carbon samples used in these experiments were not self-supporting. Carbon was evaporated onto tantalum disks to form "thin" carbon samples (Ref. 13), and "thin" oxygen samples were formed by anodizing tantalum disks. The tantalum disks used were 0.86 mm thick

and about 5 cm diam. The high-Z and corresponding high-coulomb barrier of the tantalum prevented significant interactions of the <sup>3</sup>He ions with the tantalum nuclei. Therefore, the tantalum did not contribute greatly to the signals being measured, and these "thin" samples were similar to the actual surface layers that were to be investigated. The carbon, oxygen and other low-Z impurities present in the tantalum were of low enough concentration that they presented negligible interference. The most significant interference from the tantalum was in the prompt-gamma detector system. A gamma ray, apparently from excitation of a nuclear level in <sup>181</sup>Ta of approximately 136 keV, was present in the prompt-gamma spectra at the higher <sup>3</sup>He energies. The high count rate from this gamma degraded the resolution of the Ge(Li) detector system.

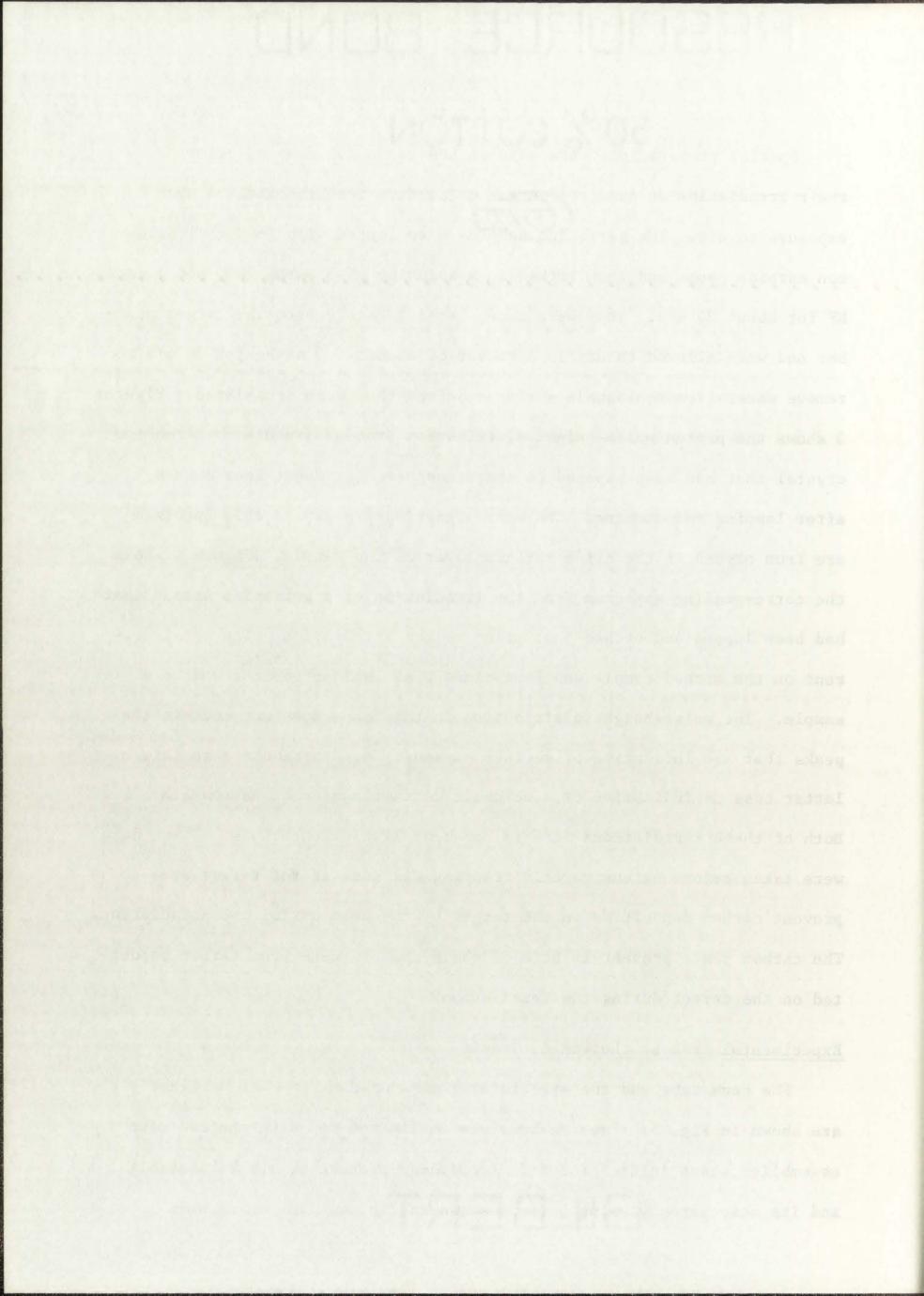
Carbon was evaporated in a vacuum directly onto one side of the tantalum. This gave a thin uniform carbon layer that was typically 15  $\mu g-carbon/cm^2$  thick. Oxygen targets were prepared by anodizing the tantalum in a very dilute  $\mathrm{H_2SO_4}$  solution (few drops of  $\mathrm{H_2SO_4}$  per 100 ml  $\mathrm{H_2O}$ ). The maximum current used in the anodization process was approximately 100 mA. The thicknesses of the anodic oxide films were varied by using various anodizing voltages. The thickest film corresponded to an anodizing voltage of 150 V and was measured to be 47.6  $\mu g-oxygen/cm^2$ . The measurement of these surface layer thicknesses is described in Chapter III. Prior to the deposition of the carbon and oxygen, the tantalum disks were etched in a solution of 25 parts 70%  $\mathrm{HNO_3}$ , 55 parts 95%  $\mathrm{H_2SO_4}$ , and 20 parts 48% HF for a few minutes to remove surface oxide layers and grease.

 $<sup>^1</sup>$  The corresponding thicknesses that are consistent with the cross sections presented in Chapter IV are 18.8 and 33.6  $\mu g/cm^2$  .

Special preparations were made on the germanium samples prior to their irradiation because the germanium surface readily oxidized upon exposure to air. The germanium samples were lapped with #600 grit silicon carbide paper and then etched in a solution of 3 parts HNO3 and 1 part HF for about 30 sec. They were then placed directly into the target chamber and were allowed to dry in a vacuum of about 10<sup>-6</sup> mm-Hg for 70 min to remove water from the sample surfaces before they were irradiated. Figure 3 shows the proton pulse-height distribution from an irradiated germanium crystal that had been exposed to the atmosphere for about four months after lapping and etching. The most significant peaks in this spectrum are from oxygen in the oxide surface layer on the sample. Figure 4 shows the corresponding spectrum from the irradiation of a germanium sample that had been lapped and etched just prior to the irradiation. The total current on the etched sample was four times that incident on the unetched sample. The pulse-height distribution in this case does not contain the peaks that are indicative of surface oxygen. The distribution in this latter case is indicative of a volumetric distribution of the oxygen. Both of these irradiations were in nonchanneling orientations. These data were taken before extensive cold trapping was done in the target area to prevent carbon deposition on the target by the beam during the irradiation. The carbon peaks present in both of these spectra were from carbon deposited on the target during the irradiation.

# Experimental Area at the Van de Graaff

The beam tube and the experimental area used at the Van de Graaff are shown in Fig. 5. The <sup>3</sup>He beam was collimated by using the two slit assemblies shown in the picture. A close-up picture of a slit assembly and its associated viewing port is shown in Fig. 6. The slits were



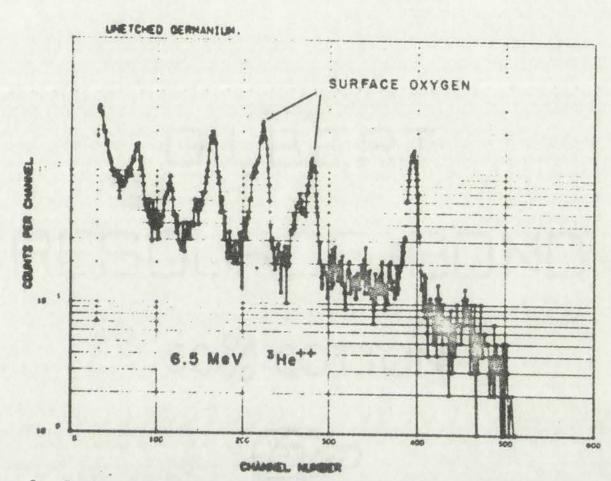


Fig. 3. Proton spectrum from the irradiation of a germanium crystal after its surface was allowed to oxidize in air.

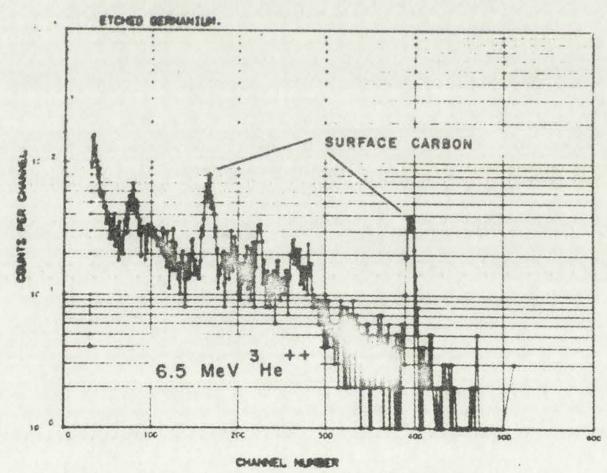
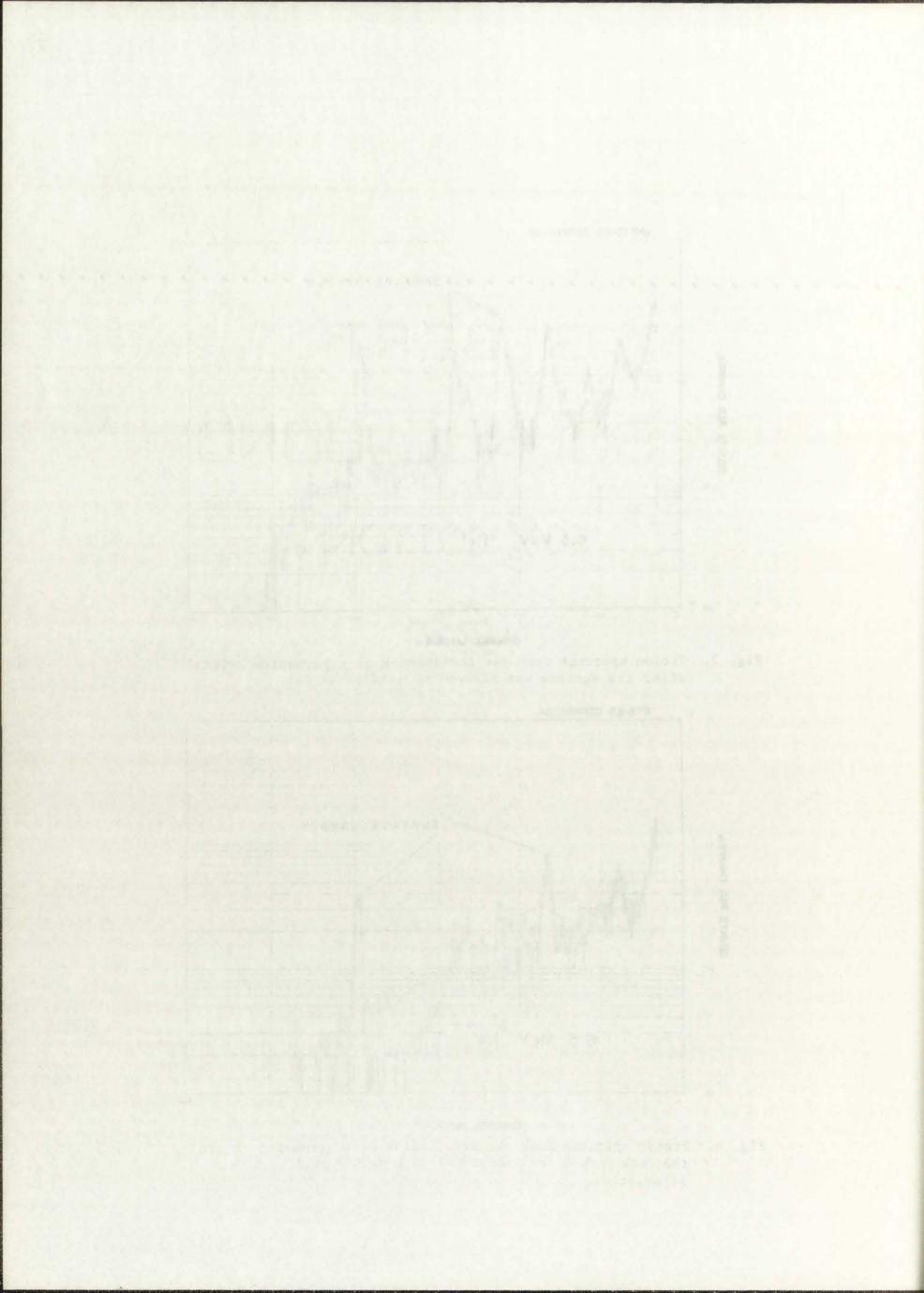
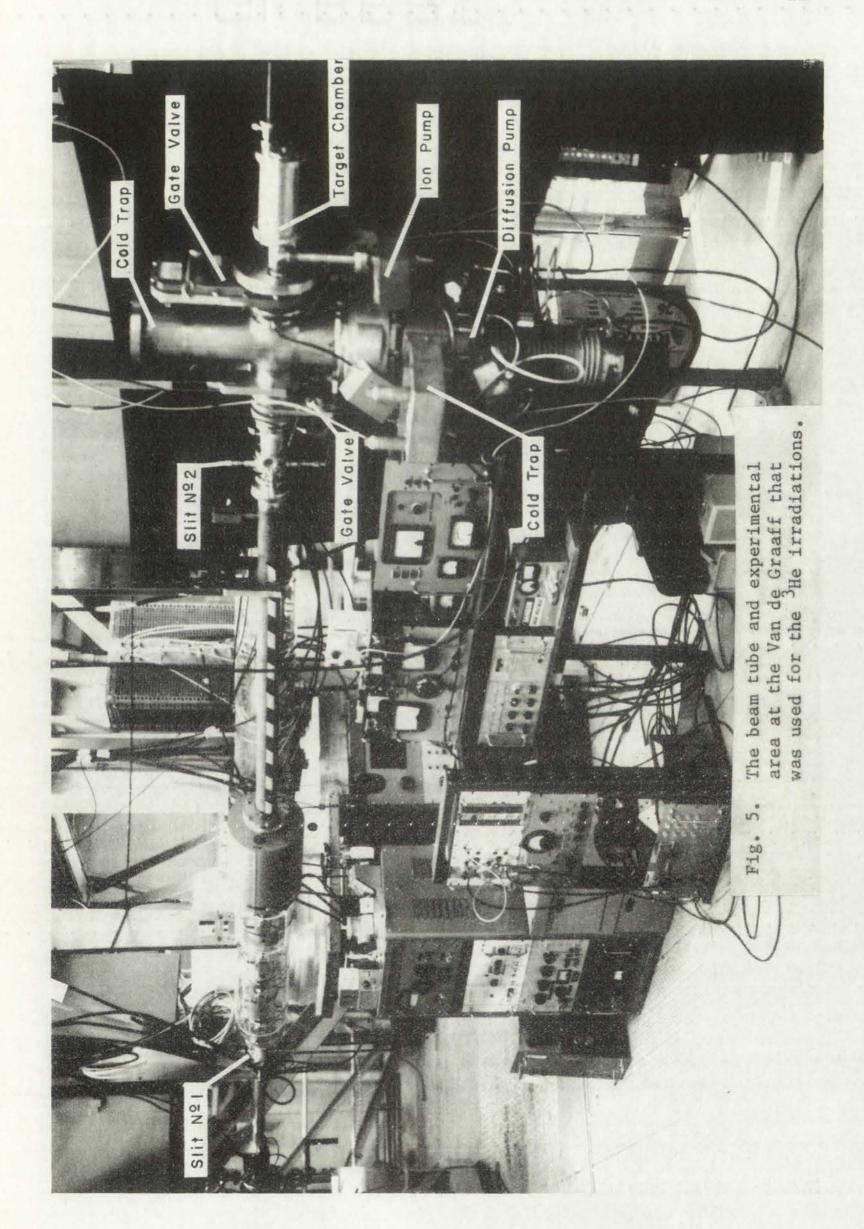
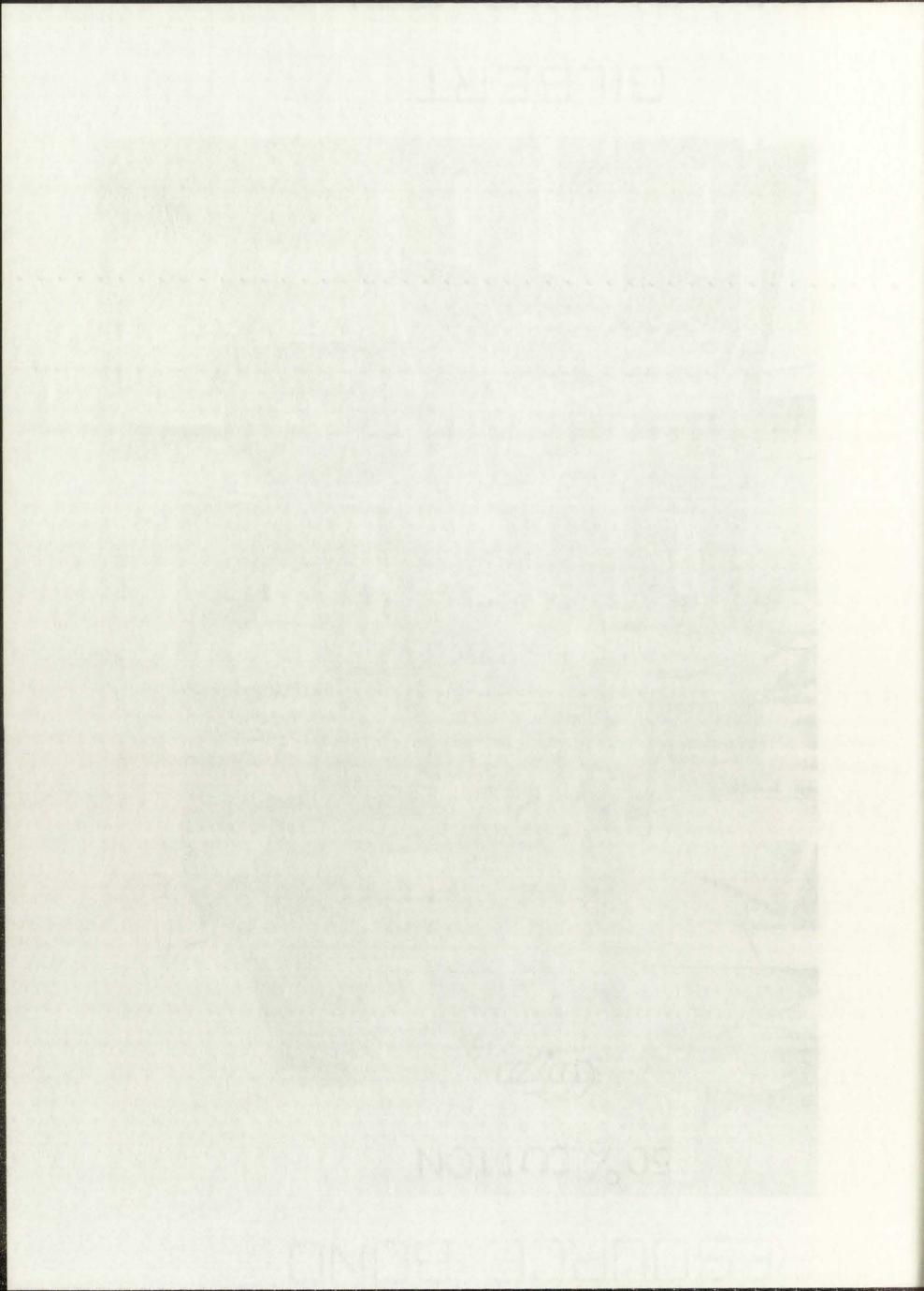
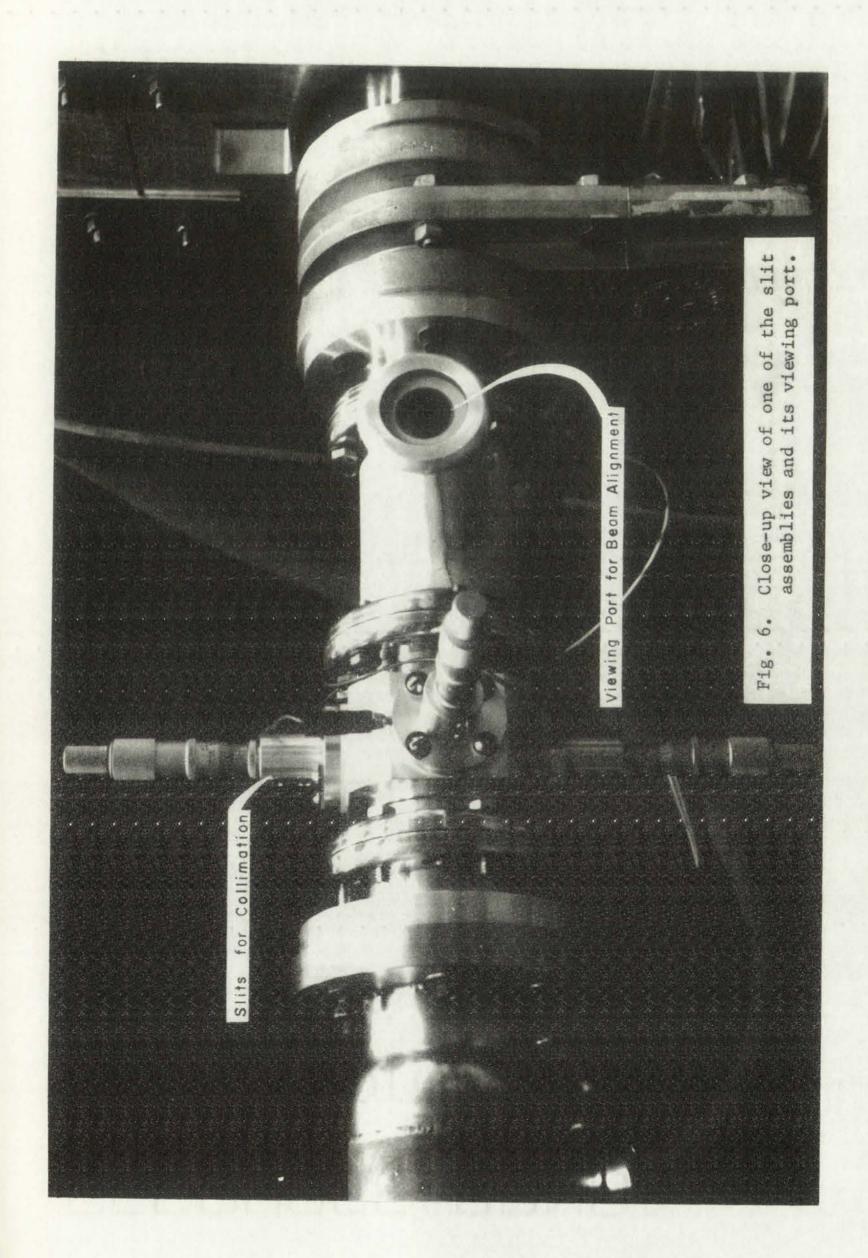


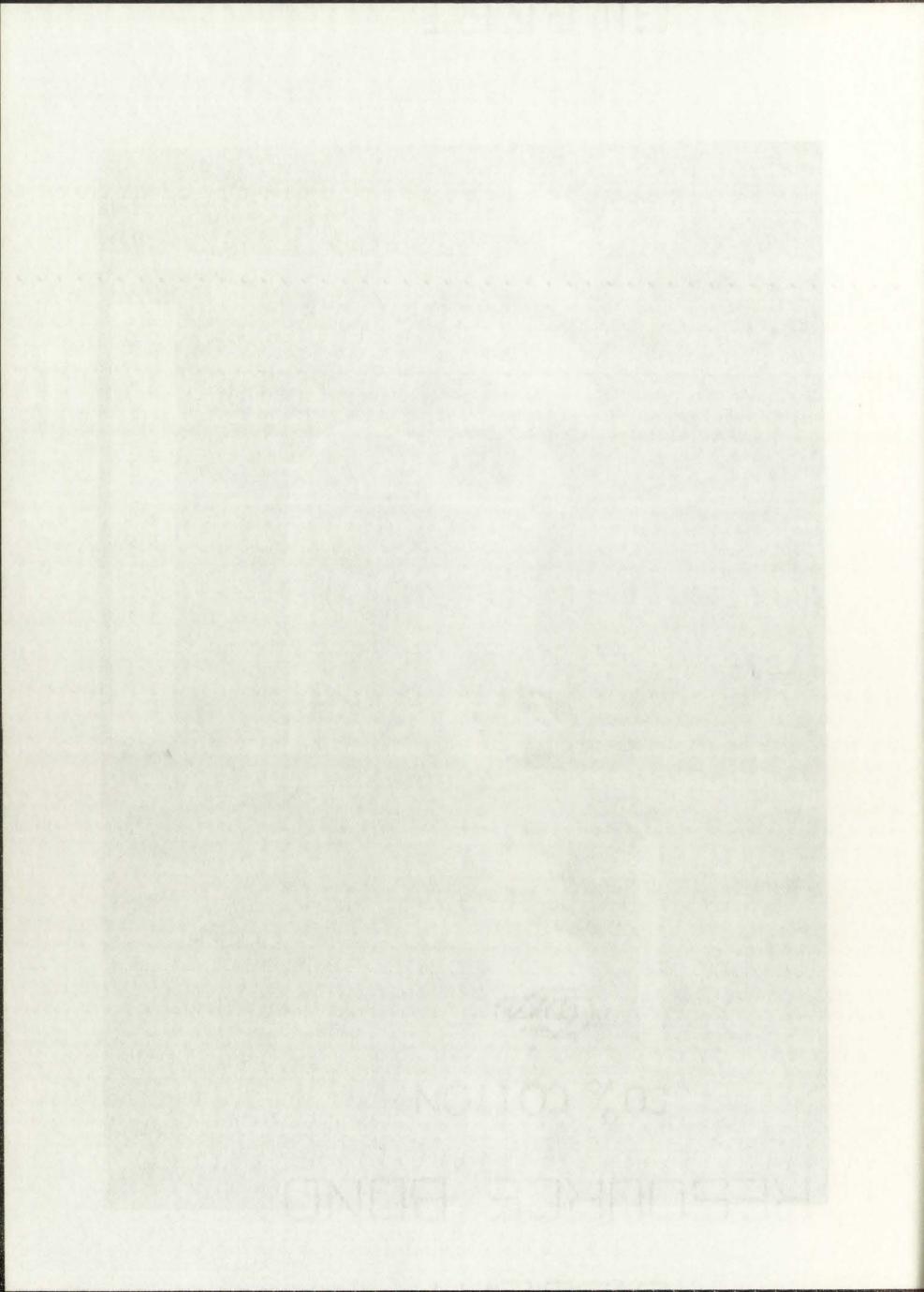
Fig. 4. Proton spectrum from the irradiation of a germanium crystal that was etched and then dried in a vacuum prior to the irradiation.







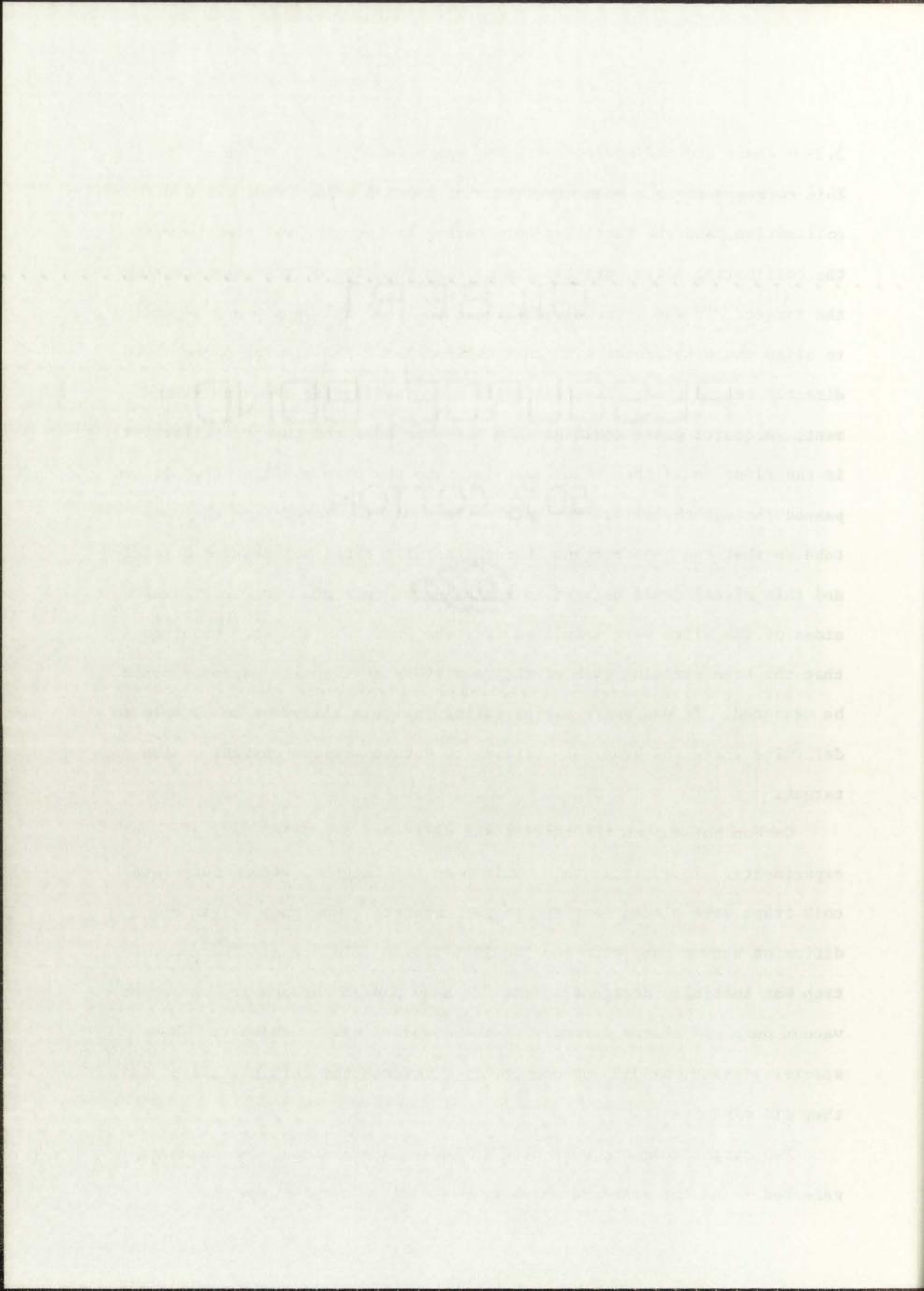




3.34 m apart and had square apertures approximately 1.36 mm on a side. This corresponds to a beam divergence of about 4 x 10<sup>-4</sup> rad. This high collimation, and the fact that no steering or focusing was used between the collimating slits, greatly limited the fraction of the beam striking the target. It was extremely difficult to steer the beam properly and to align the accelerator with this collimation. The viewing ports shown directly behind the collimating slits were used during the beam alignment. A quartz glass could be slid into the beam and the scintillations in the glass could then be used to indicate the beam profile after it had passed through the slit. The quartz glass was insulated from the beam tube so that the beam current through the slit could be measured directly and this signal could be used to maximize the current. The individual sides of the slits were insulated from the beam tube and each other so that the beam striking each of the four sides of the slit assembly could be measured. It was quite useful during the beam alignment to be able to determine where the beam was striking to obtain maximum current on the target.

carbon buildup on the targets and slits was a problem during these experiments. To minimize this buildup on the targets, vacuum pumps and cold traps were placed near the target chambers. One pump was an oil diffusion vacuum pump with two liquid nitrogen cold traps. The top cold trap was specially designed so the <sup>3</sup>He beam passed through it. A second vacuum pump was placed directly on the standard target chamber. These special precautions did not completely eliminate the carbon buildup, but they did minimize it.

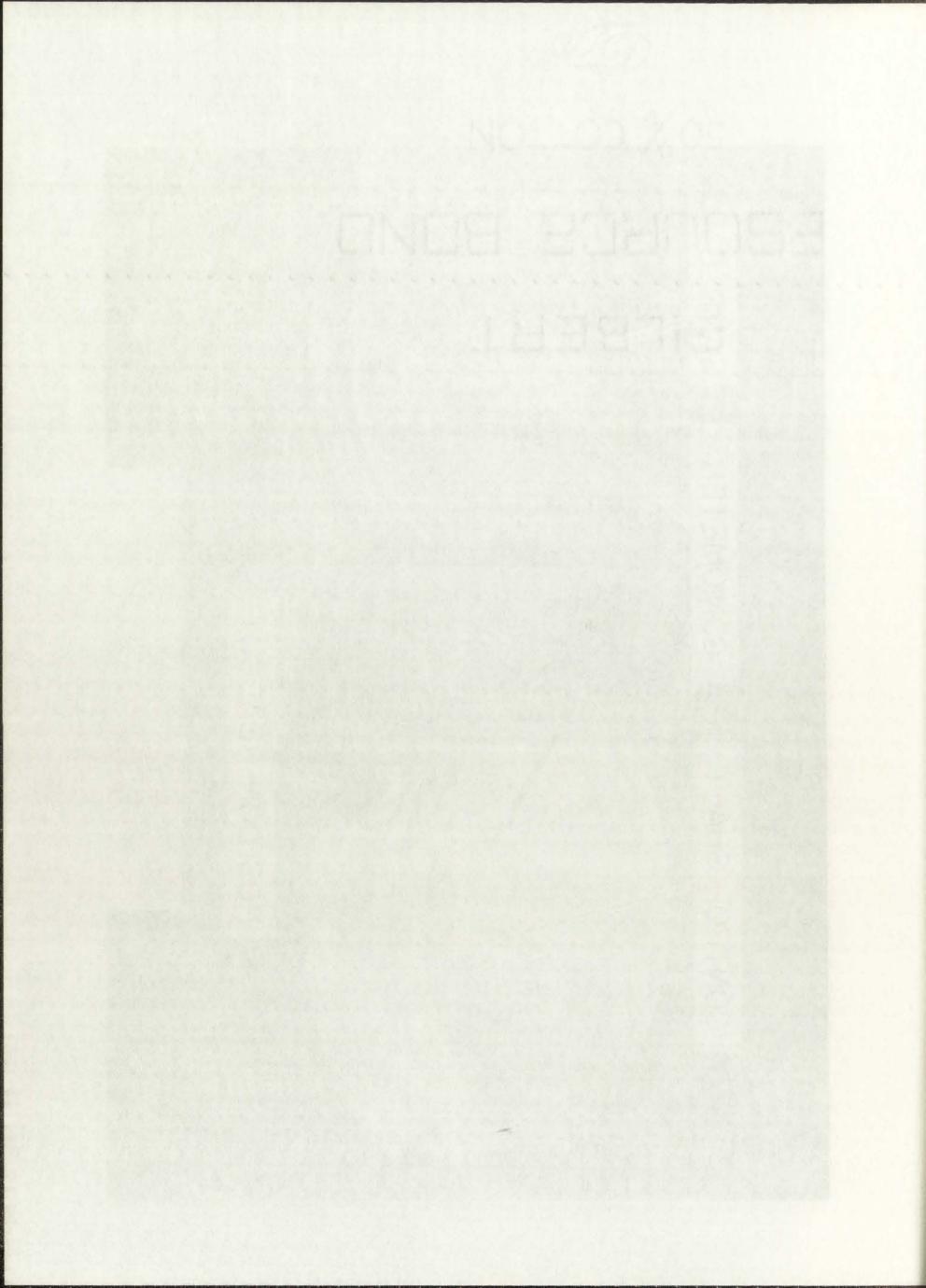
Two target chambers were used in these experiments. One chamber, referred to as the standard chamber, was used in determining the



excitation functions and for the calibration runs. The other chamber, with similar detector arrangements, contained a goniometer so that oriented irradiations could be made on germanium crystals. The outer wall of the standard chamber was 30 mil aluminum and designed so a Ge(Li) detector system could be placed near the target but outside the chamber so the prompt gamma-ray spectrum could be recorded during the irradiations. A collimated silicon surface barrier detector was located inside the chamber at 160° from the direction of the incident beam and was used to detect protons from 3He-induced nuclear reactions. Thin aluminum foils (1 mil each) were placed between the target and detector so the backscattered He particles and reaction alphas would not be detected. The resistivity of the detectors was about 25,000  $\Omega/cm$  and they were operated at 100 V. This gave a maximum full-energy detection range to about 11.0 MeV for protons. An electron suppressor operated at -300 V was placed in front of the target to repel the scattered electrons back to the target so that the full charge was collected.

The goniometer target chamber is shown in Fig. 7. This chamber was mounted directly behind the second gate valve shown in Fig. 3. Two silicon surface barrier detectors were mounted in front of the gate valve next to the cold trap. One detector was collimated and had aluminum foils between it and the target so that only the prompt protons were detected. The other detector was bare and was used to detect the backscattered <sup>3</sup>He particles during the alignment of the single crystals. The variations in the backscattered <sup>3</sup>He spectrum can be correlated with the various crystal planes and axes for the channeling experiments.



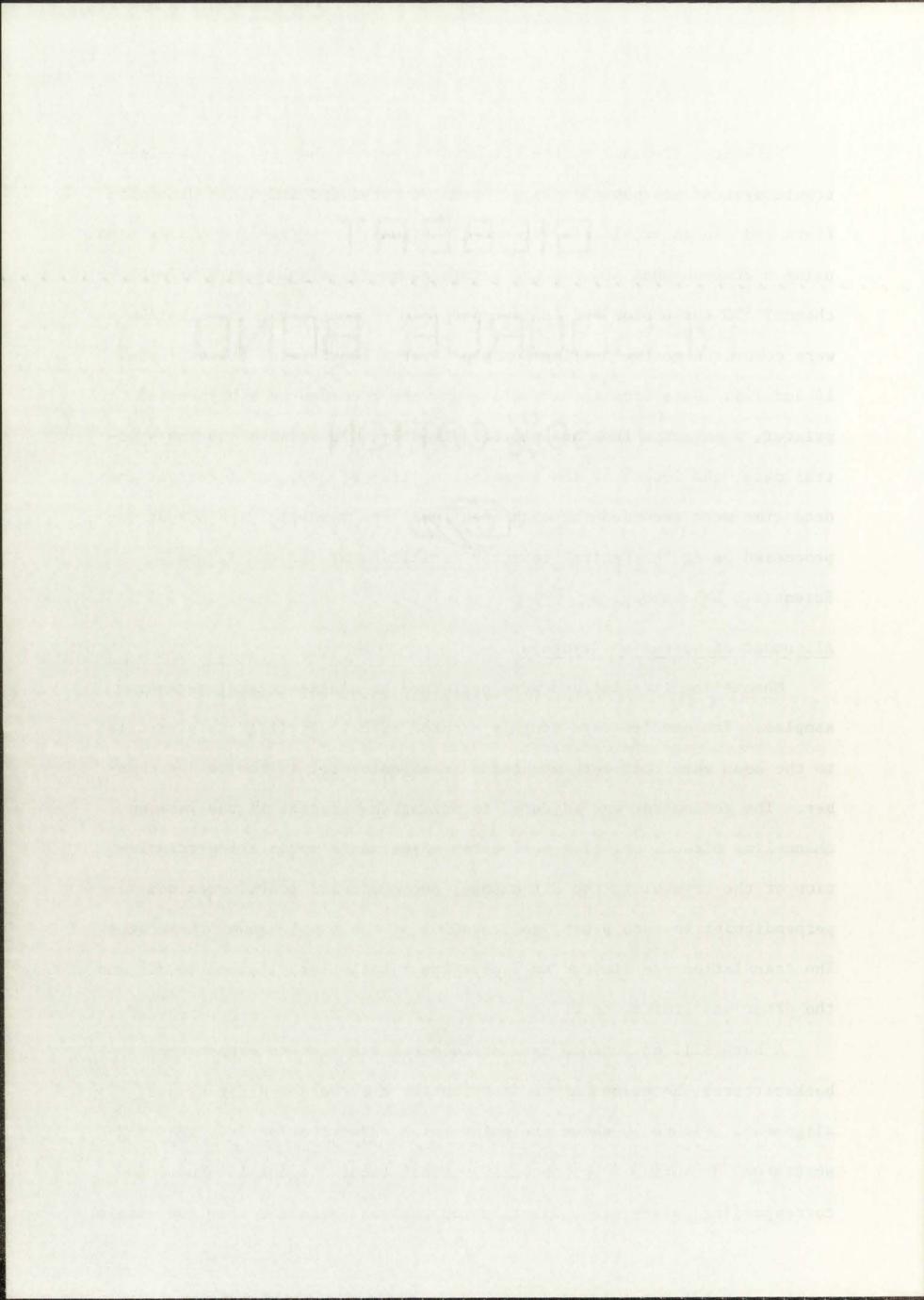


Schematic drawings of the standard target chamber and of the electronic systems are shown in Figs. 8 and 9. Standard low-noise preamplifiers and linear amplifiers were used. Signals from these were digitized using a 2048-channel ADC for the prompt gamma-ray signal and a 512-channel ADC for proton and charged-particle detector systems. The ADC's were connected to the on-line computer system at the accelerator (Refs. 14 and 15). Data from the irradiations were recorded on a high-speed printer, a magnetic tape and plotted directly. In addition to the spectral data, the length of the irradiation, time of day, total current and dead time were recorded for each spectrum. The magnetic tape output was processed using the central computer facilities at the Los Alamos Scientific Laboratory.

## Alignment of Germanium Crystals

Channeling irradiations were performed on single-crystal germanium samples. The samples were roughly aligned with their (111) axis parallel to the beam when they were mounted on the goniometer in the target chamber. The goniometer was adjusted to orient the crystal in the various channeling directions. The goniometer adjustments would allow translation of the crystal in two directions, perpendicular to the beam and perpendicular to each other, and rotation of the sample about these axes. The translation was limited to 1 cm. One rotation was limited to 30° and the other was limited to 25°.

A bare silicon surface barrier detector was used to detect the backscattered <sup>3</sup>He pulse-height distribution that was used for sample alignment. Figure 10 shows the pulse-height distribution from the backscattered <sup>3</sup>He during a nonchanneling irradiation. Figure 11 shows the corresponding pulse-height distribution that was obtained when the sample



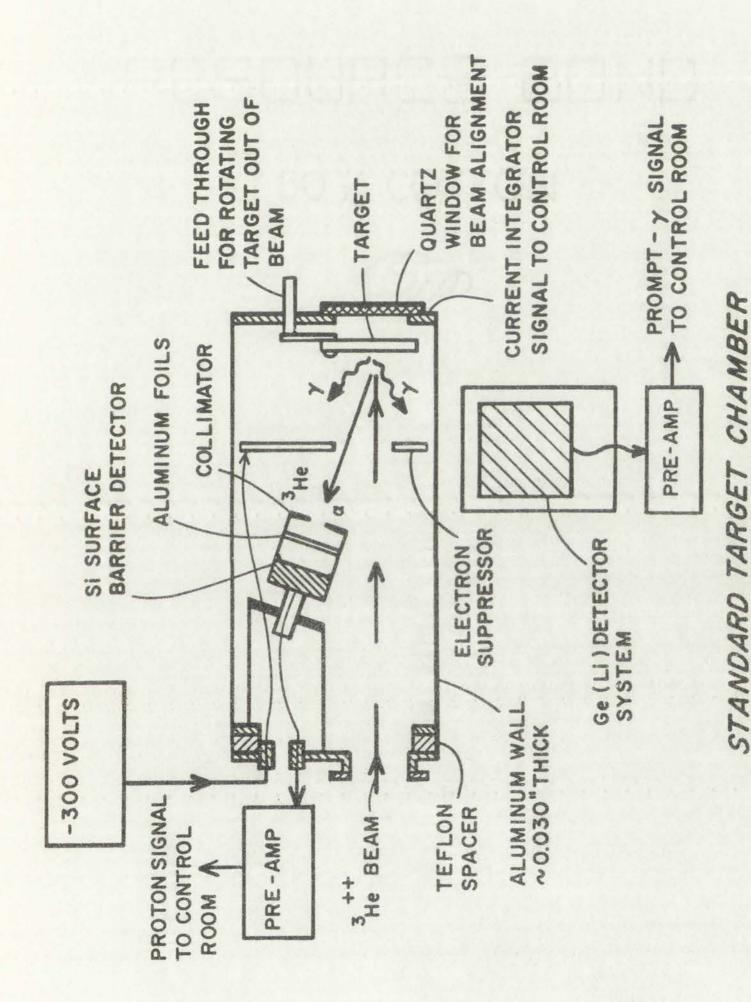


Fig. 8. Schematic drawing of the standard target chamber.

SCHEMATIC OF ACCELERATOR ELECTRONICS

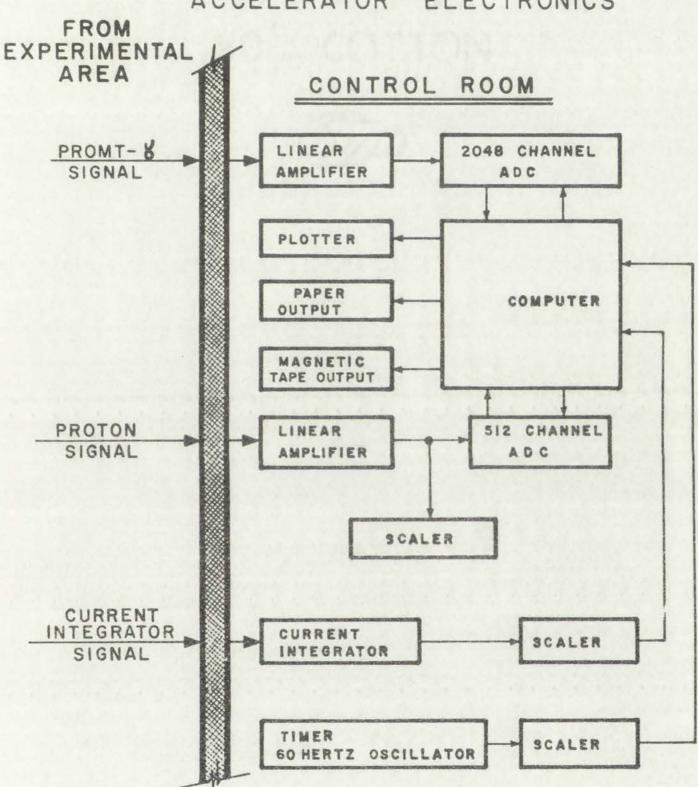
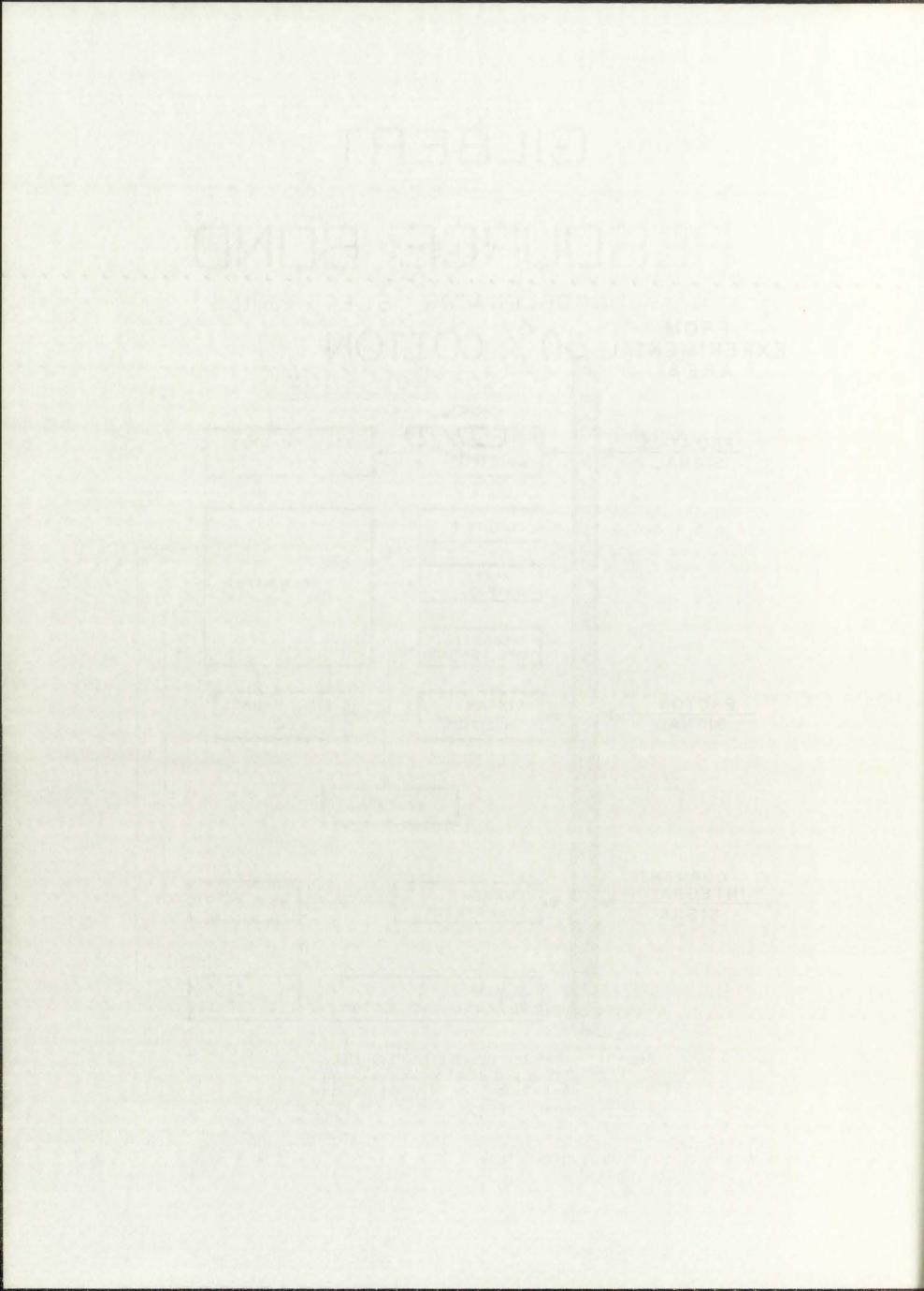


Fig. 9. Schematic drawing showing the wiring and electronic equipment used in the Van de Graaff control room.



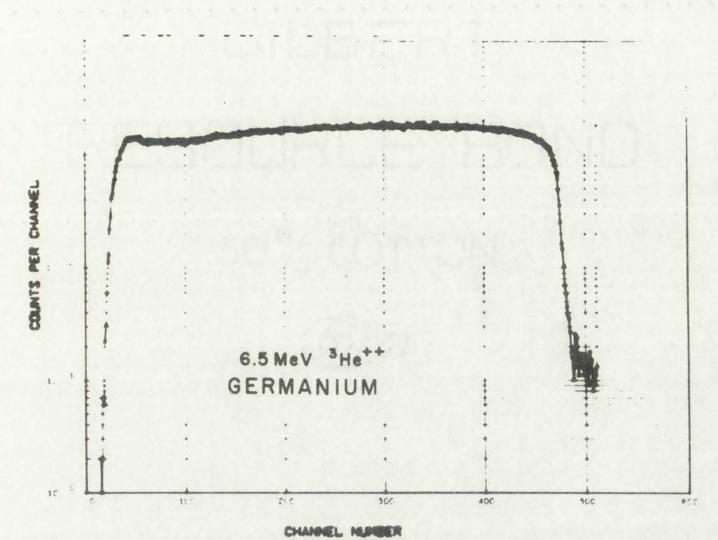


Fig. 10. Plot of the backscattered <sup>3</sup>He pulse-height distribution from the irradiation of a germanium crystal in a nonchanneling orientation.

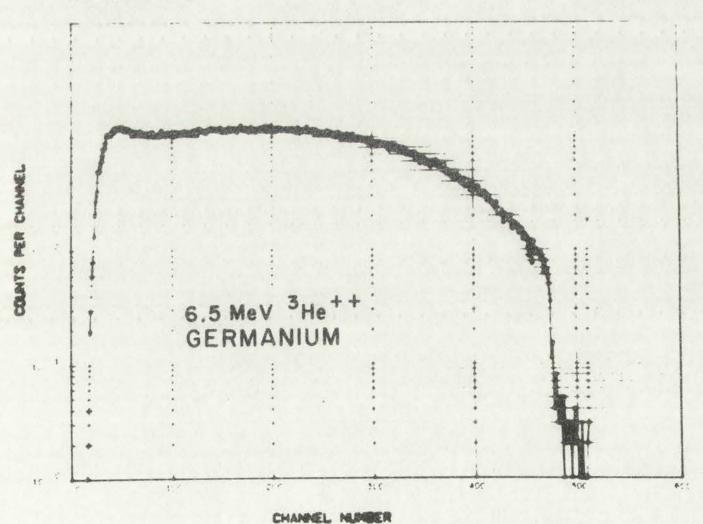
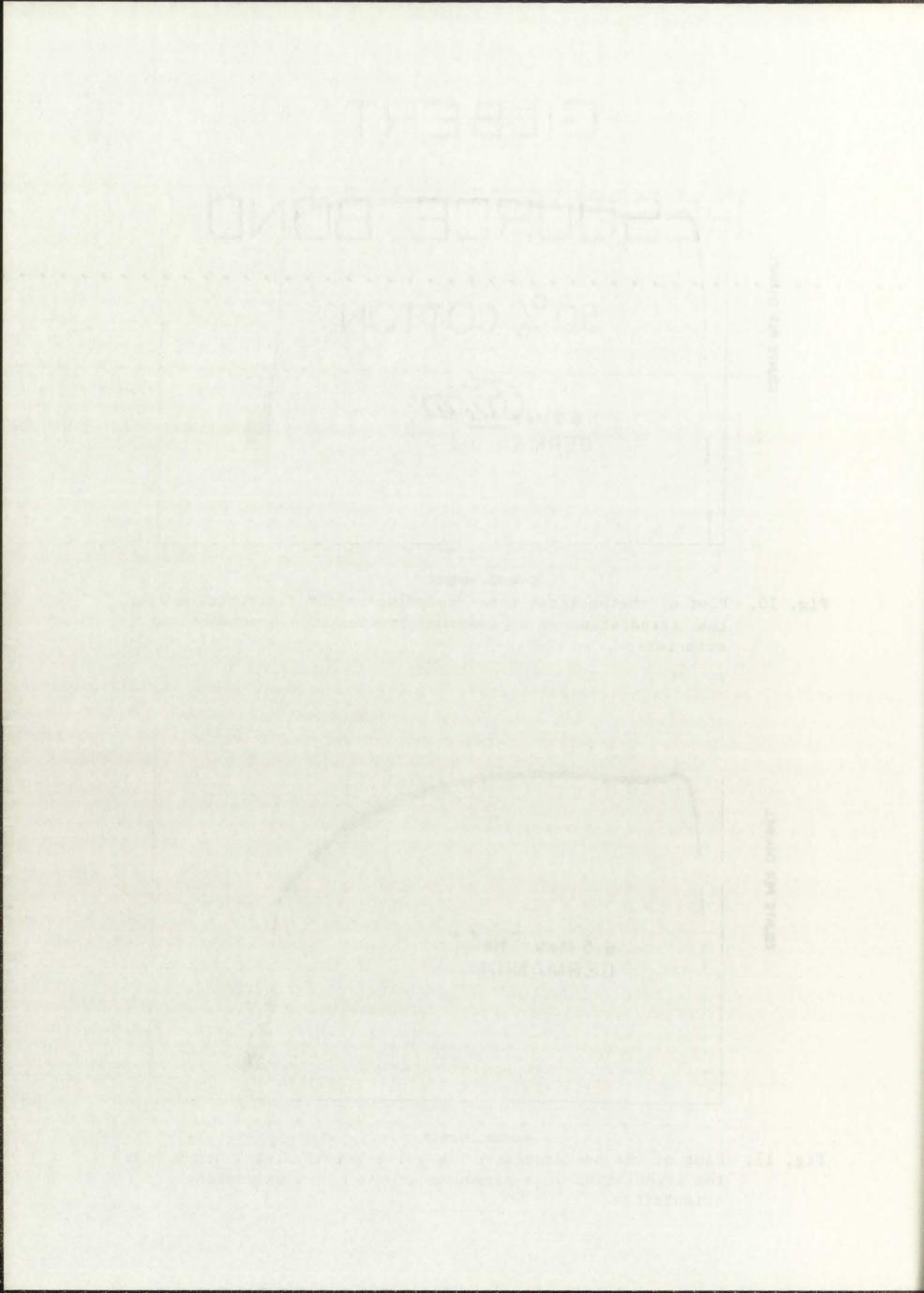


Fig. 11. Plot of the backscattered <sup>3</sup>He pulse-height distribution from the irradiation of a germanium crystal in a channeling orientation.



was oriented in the <11> direction. The channeling spectrum has fewer counts than the nonchanneling spectrum. This deviation is particularly evident at the high-energy end of the spectrum which corresponds to back-scatters from near the surface. The effect of multiple hard scatters, as the <sup>3</sup>He particles penetrate deeper into the crystal, decreases the effect of channeling on the low-energy portion of the spectrum.

The alignment procedure for the channeling irradiations consisted of using a single-channel analyzer and scaler to record the count rate in the high-energy portion of the 3He backscatter spectrum at various goniometer settings. The single-channel analyzer was set so that only pulses with amplitudes corresponding to energies from about 1 MeV below to slightly above the maximum backscatter energy produced an output pulse to the scaler. A set of data that was obtained during the alignment of a sample for a channeling irradiation along the (111) axis is shown in Fig. 12. The backscatter dips are shown for each of the {110}-type planes. One limitation of the goniometer used in these experiments was the lack of ability to rotate the samples about the incident 'He beam. Therefore, it was impossible to rotate the sample about an axis parallel with the channeling plane and minimize the angular half width of the backscatter dips. The differences in the widths of the backscatter dips shown in Fig. 12 are due to the differences in the angles of the planes relative to the two axes about which the goniometer was rotated to cross the plane.

Experimental <sup>4</sup>He channeling data from Ref. 16 were extrapolated to compare with the above data. It was assumed that the channeling characteristics of <sup>3</sup>He ions are similar to those for <sup>4</sup>He and that the width

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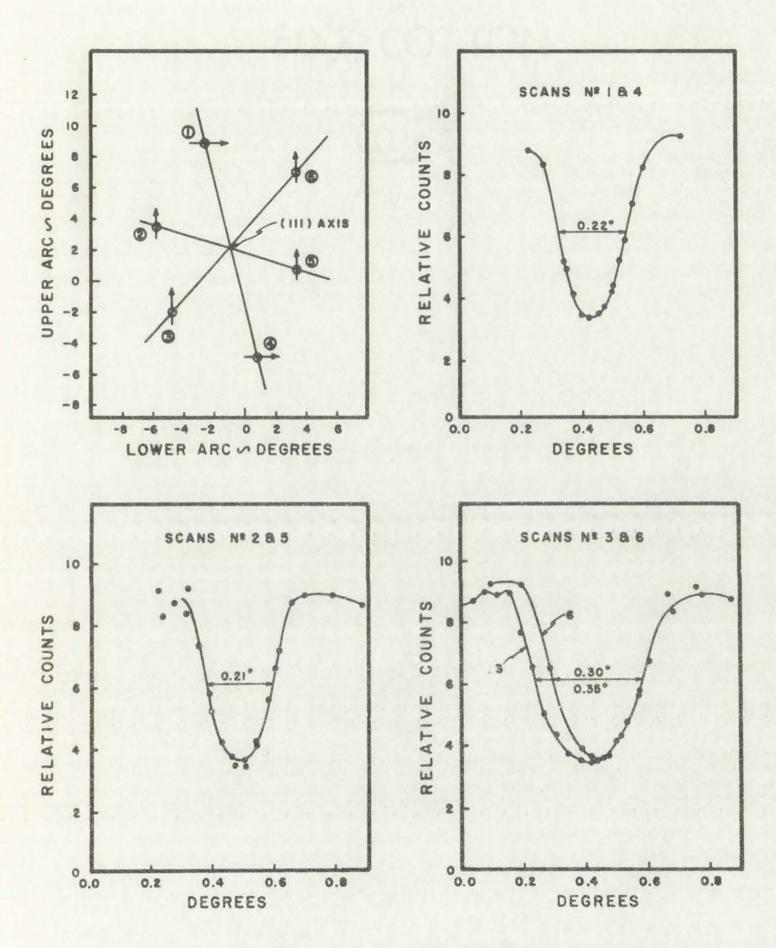
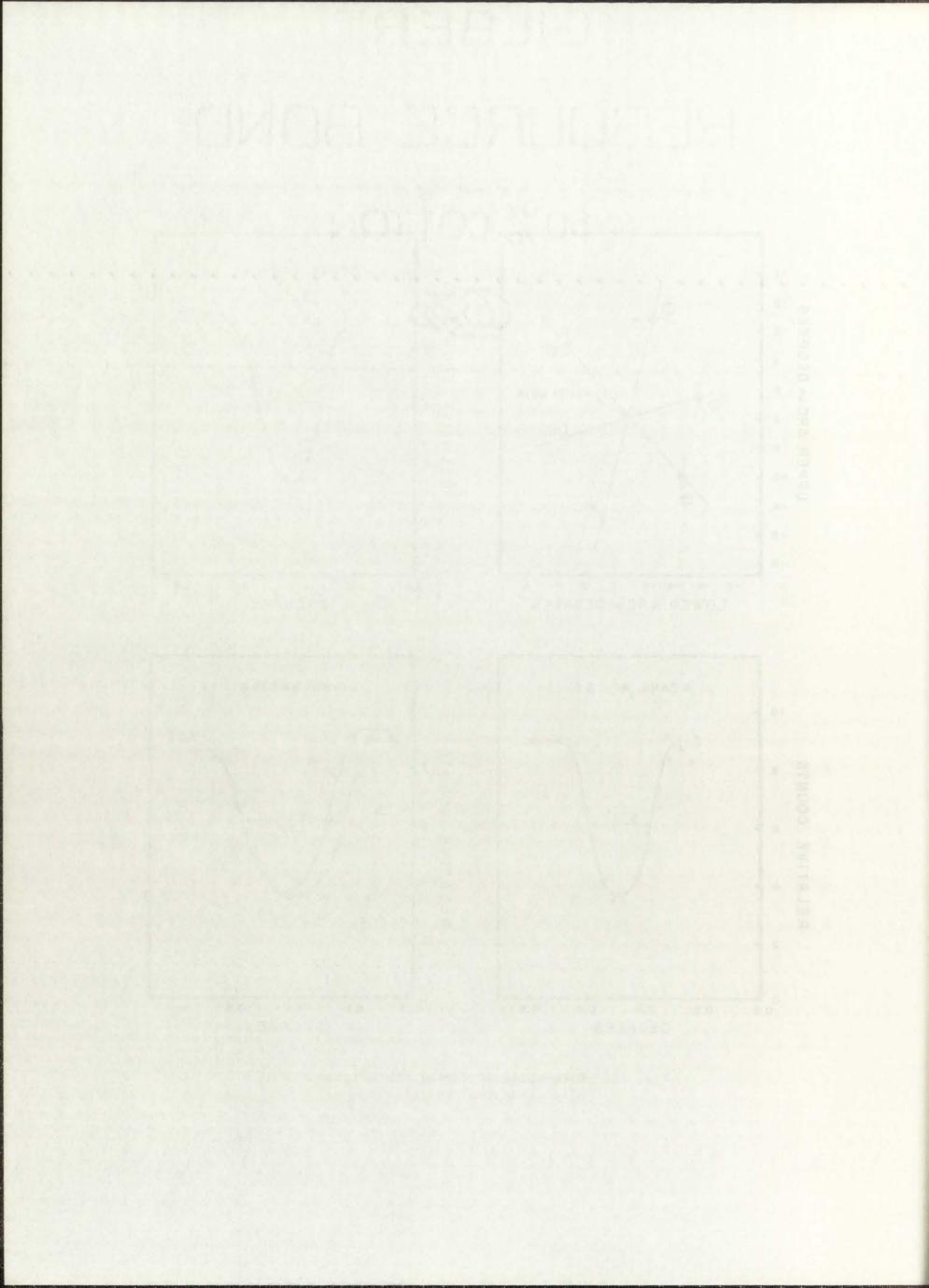


Fig. 12. Data obtained during the alignment of a germanium crystal.

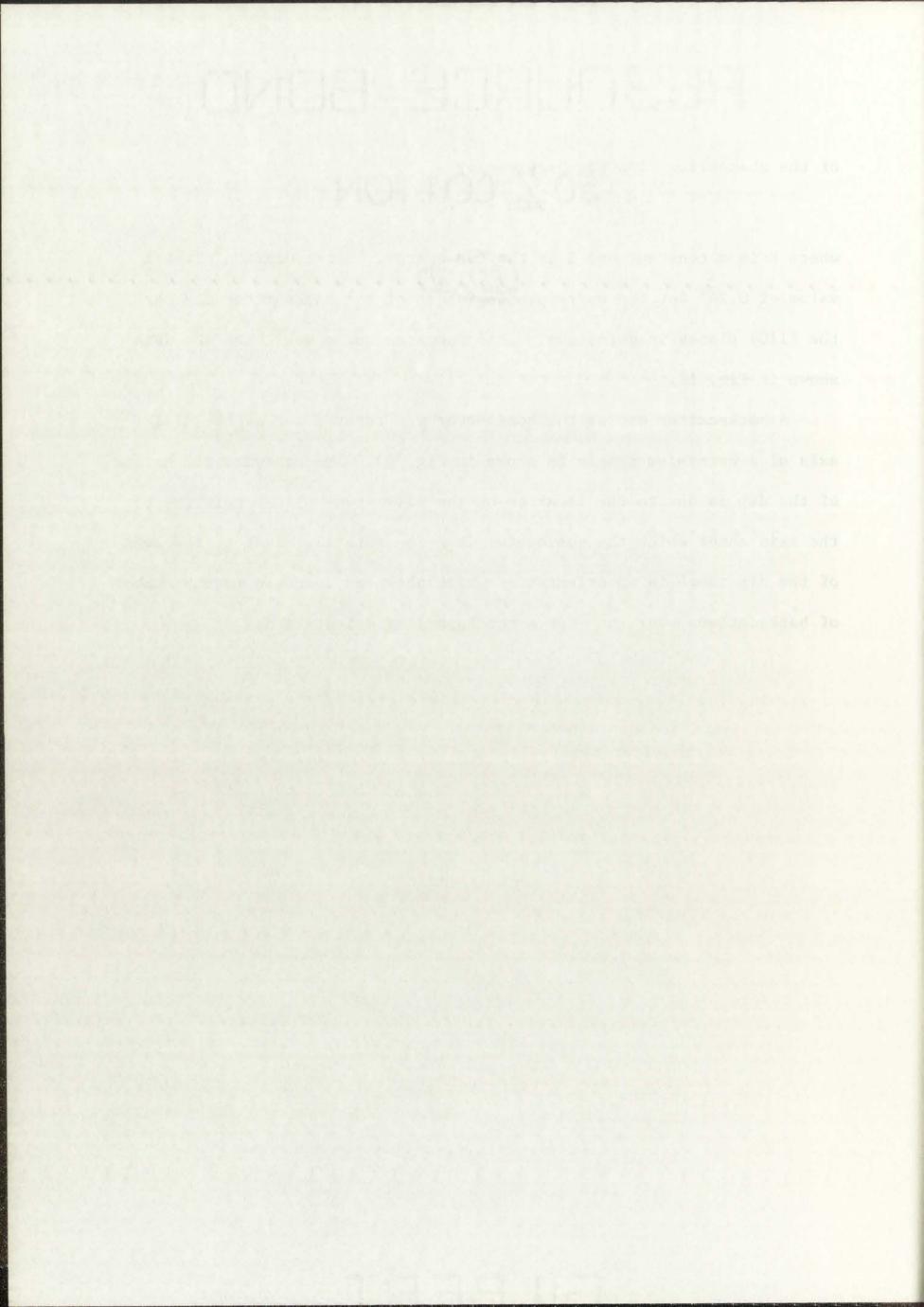


of the channeling dips can be given by

 $FWHD = K/\sqrt{E}$ 

where K is a constant and E is the ion energy. Extrapolation gives a value of 0.24° for the corresponding width of the backscatter dip for the {110} planes in germanium. This compares quite well with the data shown in Fig. 12.

A backscatter dip as the goniometer was rotated across the <11\$\Delta\$ axis of a germanium sample is shown in Fig. 13. The nonsymmetric nature of the dip is due to the location of the {110}-type planes relative to the axis about which the goniometer is being rotated. Just to the left of the dip there is an orientation which shows an increase in the number of backscatters over that for a nonchanneling orientation.



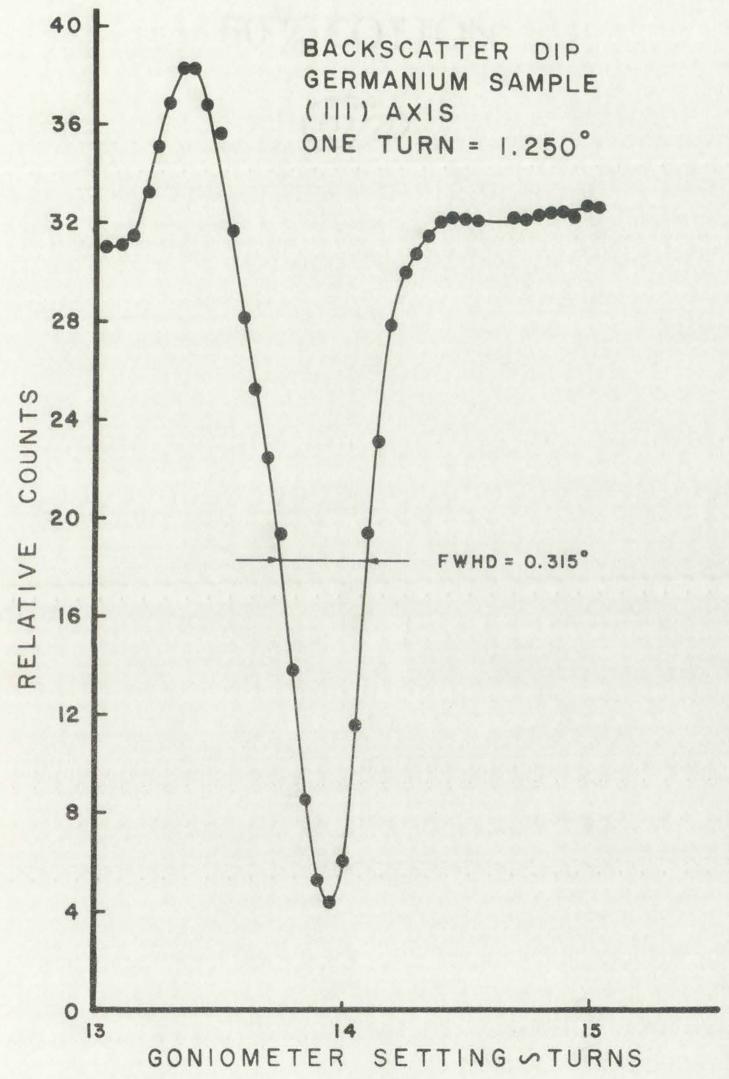
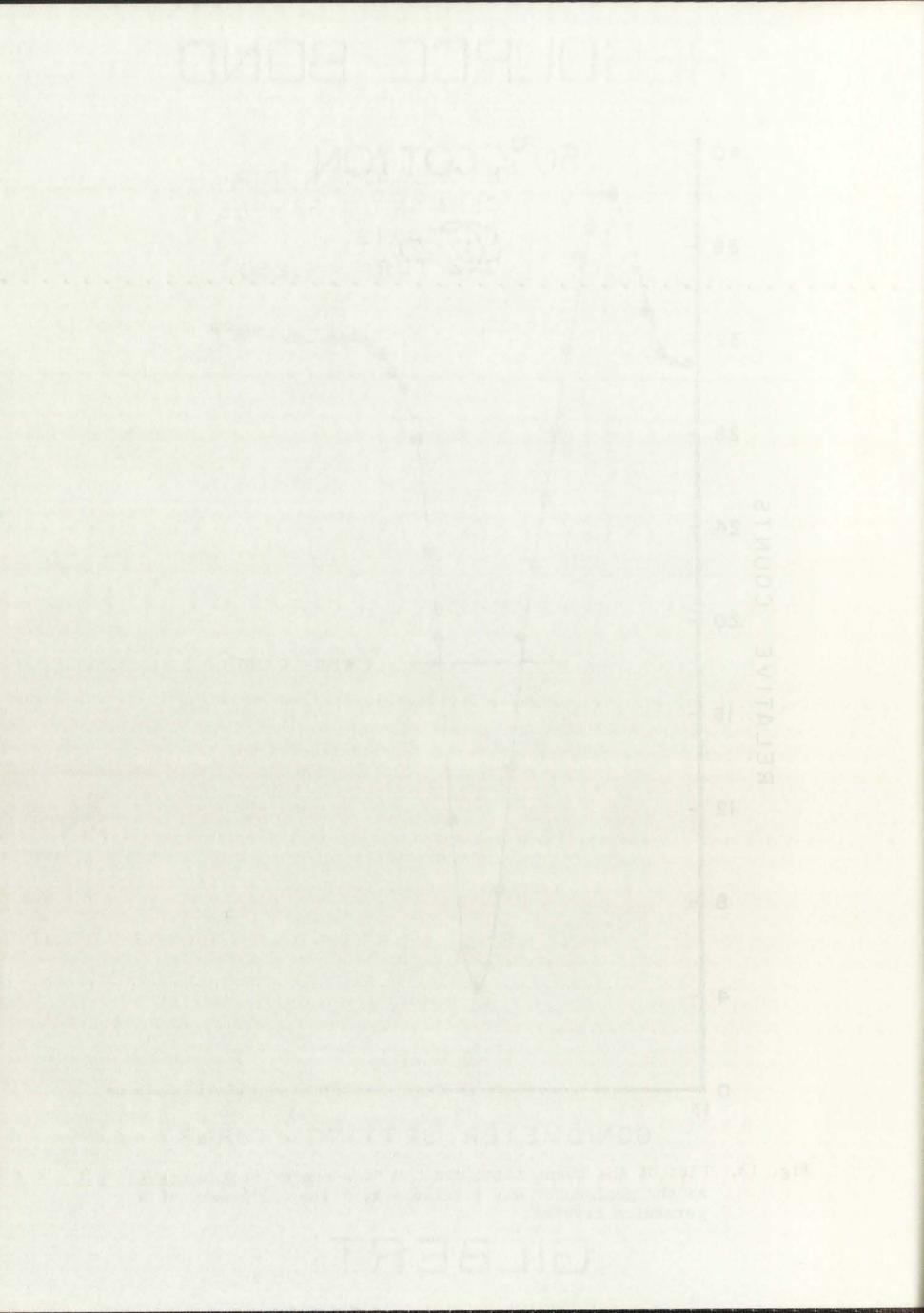


Fig. 13. Plot of the count rate from the high-energy backscattered <sup>3</sup>He as the goniometer was rotated across the (111) axis of a germanium crystal.



### CHAPTER III

## CALIBRATION USING PASSIVE ANALYSES

# Introduction

Thin carbon and oxygen targets were irradiated with 8.6 MeV  $^3$ He ions in the standard target chamber. The proton spectra were recorded during the irradiations. After the irradiations, the samples were counted in a  $^4\pi$  NaI detector system and their decay histories were recorded. The main activation products were  $^{11}$ C from the  $^{12}$ C( $^3$ He, $\alpha$ ) $^{11}$ C reaction and  $^{18}$ F from the  $^{16}$ O( $^3$ He,p) $^{18}$ F reaction. Half-life data and Q values for these and a few other reactions of interest are given in Table 1.

TABLE 1

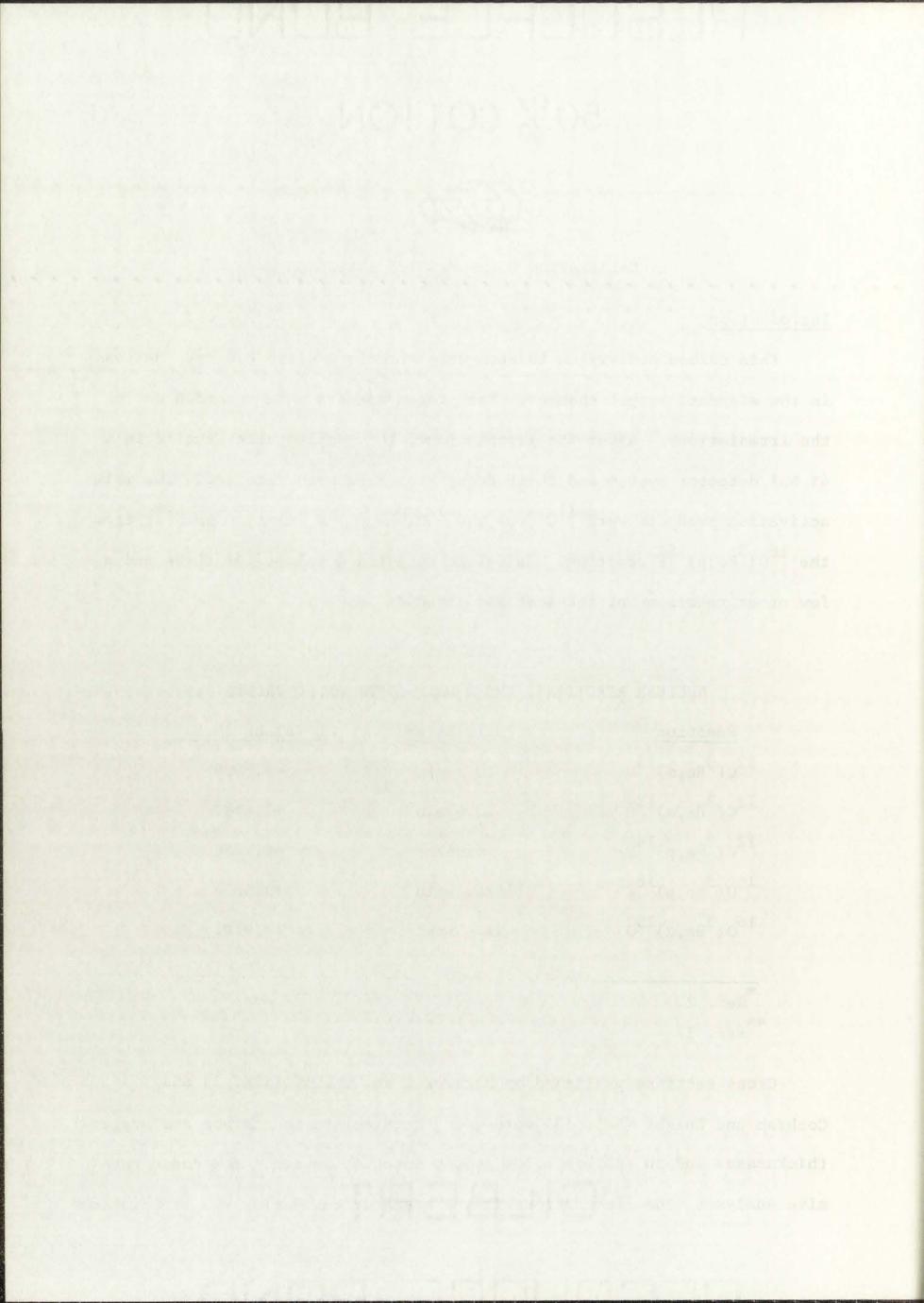
NUCLEAR REACTIONS, THEIR HALF-LIVES AND Q VALUES

Reaction	Half-Life*	Q Values (MeV)**
$^{12}$ C( $^{3}$ He,d) $^{13}$ N	10.1 min	-3.5498
$^{12}$ C( $^{3}$ He, $\alpha$ ) $^{11}$ C	20.4 min	+1.8582
$^{12}$ C( $^{3}$ He,p) $^{14}$ N	stable	+4.7786
<sup>16</sup> 0( <sup>3</sup> He,p) <sup>18</sup> F	110. min	+2.0334
$^{16}_{0(^{3}\text{He},\alpha)}^{15}_{0}$	124. sec	+4.9101

<sup>\*</sup>Ref. 2

Cross sections published by Markowitz and Mahony (Ref. 2) and Cochran and Knight (Ref. 18) were used to calculate the carbon and oxygen thicknesses and to calibrate the proton detector system. For these passive analyses, the fluctuations in the beam current during the irradiations

<sup>\*\*</sup> Ref. 17



were large enough to influence the results. Therefore, the currents on the targets were recorded at 10-sec intervals during the irradiations so that corrections could be made for these fluctuations. The on-line computer system at the accelerator was used for this recording.

The carbon sample was irradiated for approximately 24 min at an average beam current of 83 nA. The oxygen sample was irradiated for approximately 28 min at an average current of 143 nA.

# Data Acquisition

After the irradiation, each sample was counted in a 4 $\pi$  detector system and its spectral history was recorded. The detector system is shown in Fig. 14. It consisted of two optically isolated 13.5-in.-diam by 6-in.-thick NaI(T1) cylinders with a  $2\frac{1}{2}$ -in.-diam hole between them for sample insertion. The NaI(T1) was shielded with 6 in. of low-background TADANAC lead. The coincident and the single spectra were simultaneously recorded using a 4096-channel analyzer. The spectra were recorded at 100-sec intervals on a magnetic tape. These data were later used with computer codes that analyzed the spectra and unfolded the complex decay curves.

A schematic diagram of the electronics is shown in Fig. 15. The pulses from each half of the detector were fed into a mixer and summed. In addition, the output from a 60-Hz pulser was routed into the mixer so that the dead time of the system could be calculated. The mixer summed the simultaneous input pulses. This summed pulse was routed to the input to the ADC of the pulse-height analyzer and was digitized to a maximum of 2048 channels. Each half of the detector was checked for coincident output pulses. If a coincidence occurred, a pulse was sent from the coincidence unit to the address register of the analyzer, causing

# Large 4m NaI(T1) detector system. SEPARATING 2 (131/2"DIA.x6"LONG) No I DETECTORS PHOTO TUBE LEAD SHIELDING LARGE NaI (T I ) DETECTOR Fig. 14. THE THE PARTY OF T SAMPLE

# SCHEMATIC DATA SYSTEM FOR 4Π COUNTING

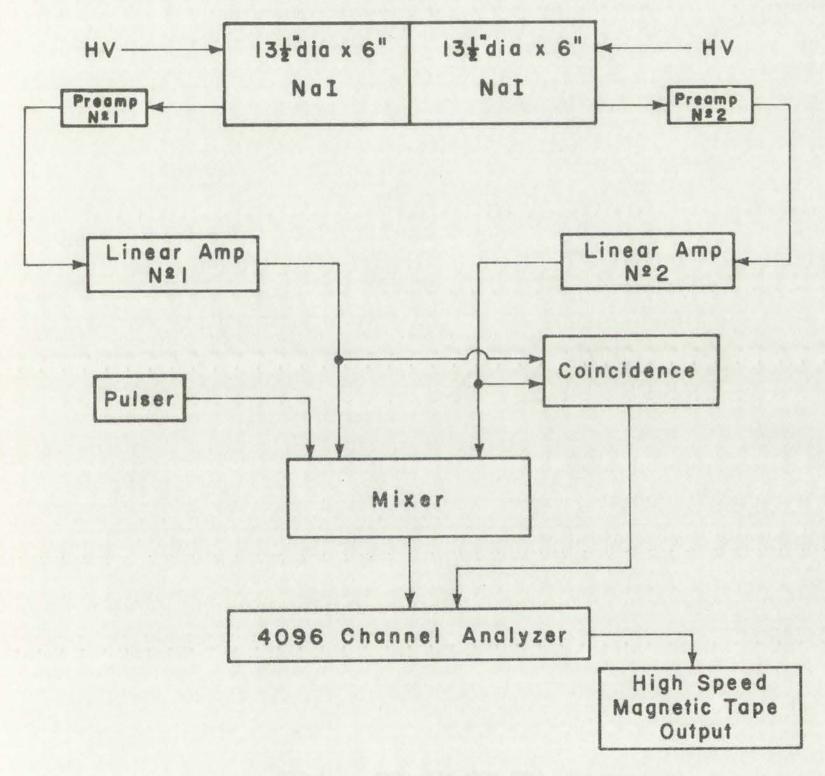
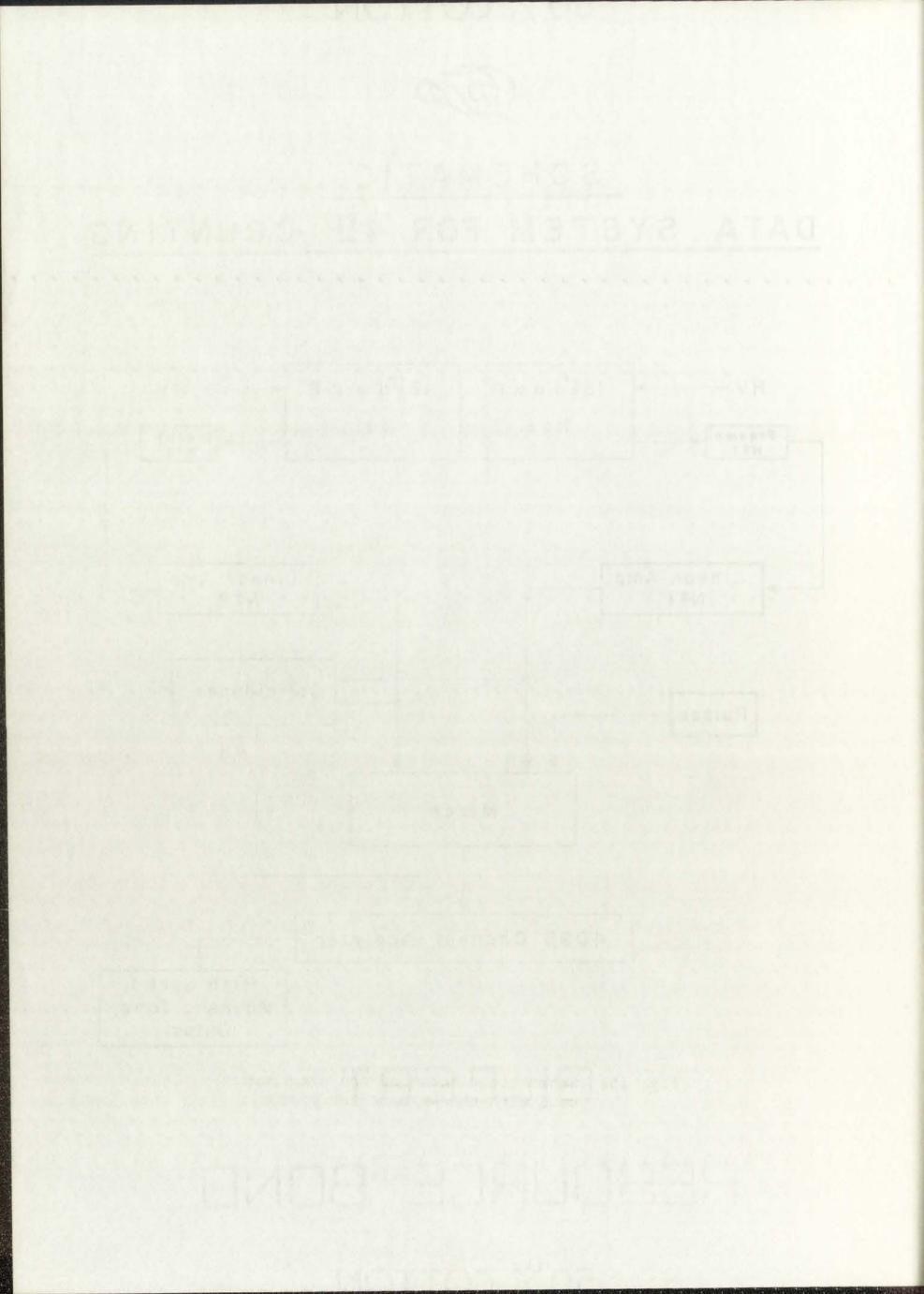


Fig. 15. Schematic diagram of the electronics used with the 4π detector system.



the digitized data to be stored in the upper 2048 channels. Otherwise, the pulse was stored in the lower 2048 channels.

Data were accumulated for intervals of 100 sec (clock time), and then the spectral data were recorded on a magnetic tape. The 4096 20-bit data words were recorded on the tape, the analyzer cleared, and accumulation of the next set of spectral data started in 2.14 sec.

A 60-Hz pulser was used to determine the live time during the count intervals. The output of the pulser was adjusted so that the pulser peak occurred near the upper end of the lower 2048 channels. This type of live-time determination was satisfactory at the count rates encountered (less than 1.5 x 10<sup>4</sup> counts/sec). At count rates higher than this, random coincidences between the pulser and the detectors would remove counts from the pulser peak. This would give a smaller live time than was actually present. At higher count rates, where the dead time becomes significant, the statistical variation of the number of counts in the pulser peak becomes significant. At these higher count rates, a higher frequency pulser would have been used to obtain the necessary accuracy.

A background spectrum from a 1000-sec count is shown in Fig. 16.

The background count rate was higher than usual at the time these experiments were conducted due to the presence of a highly radioactive reactor fuel element in a nearby gamma-ray scanning cave. The singles background rate, integrated over the energy region indicated in the left-hand spectrum of Fig. 16, was 366 counts/sec. The corresponding coincident background count rate was 25.9 counts/sec.

Figure 17 shows the pulse-height distribution obtained from the carbon sample approximately 15 min after the irradiation stopped. The pulser peak and important gamma-ray peaks are labeled. The small broad

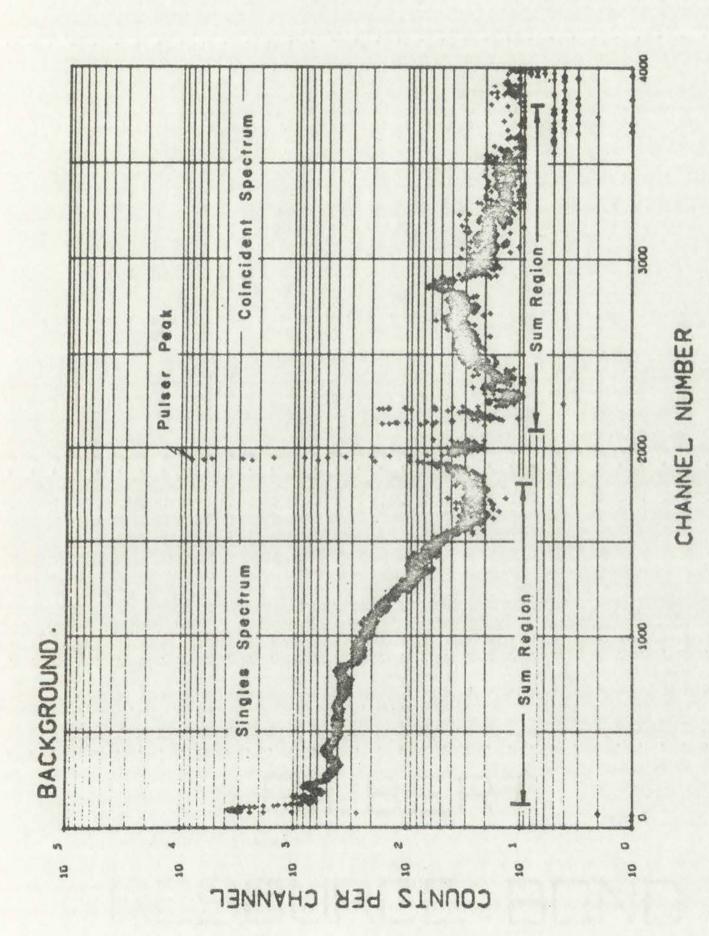


Fig. 16. Background from the 4T detector system.

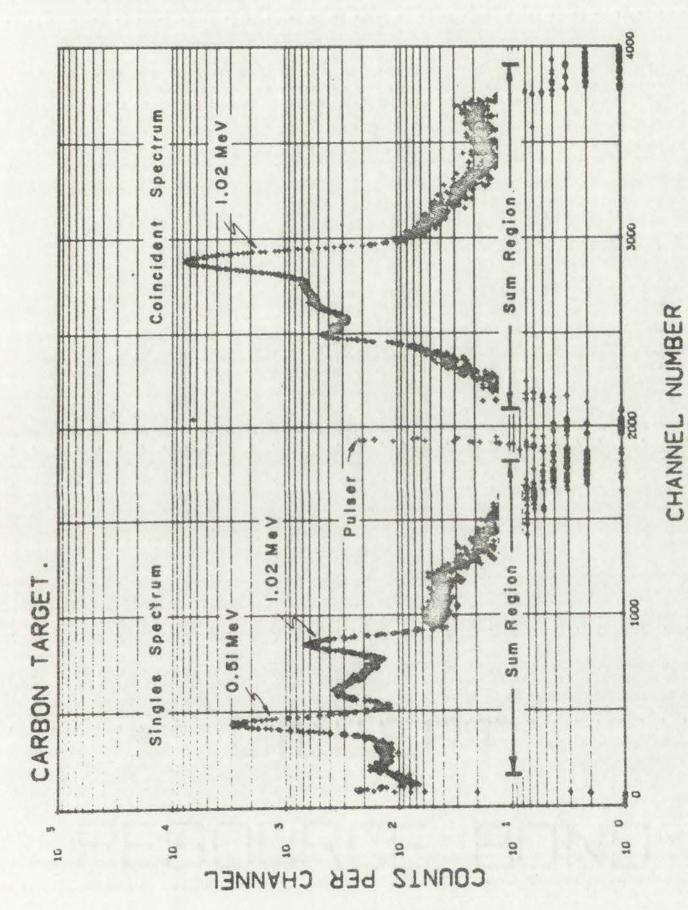
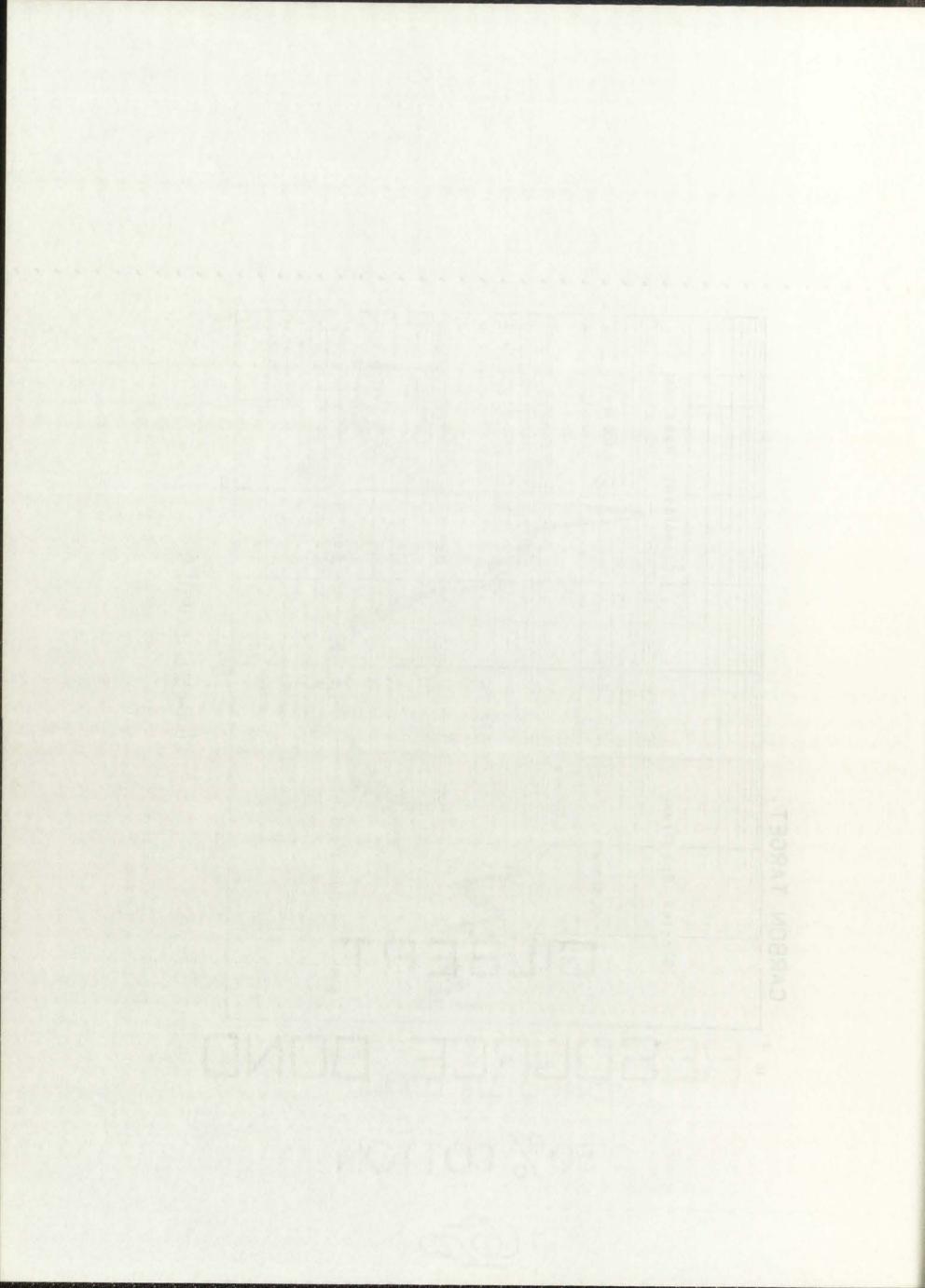


Fig. 17. Spectrum from <sup>3</sup>He irradiated carbon sample placed in the 4T detector system.



peak between the 0.51 MeV peak and the 1.02 MeV peak in the singles spectrum is from 3-quanta annihilation where one of the quanta escaped detection (e.g., Ref. 19). In fine-grained MgO power, the probability for 3-quanta annihilation can be as large as 20 to 25% (Ref. 20).

The carbon decay curve was constructed from 85 sets of spectral data. The singles spectra were integrated from 145 keV to 1230 keV. The coincident spectra were integrated from 115 keV to 1240 keV. The sum of these two numbers was then used to construct the decay curve because the total efficiency of the detector system was better known than the coincident efficiency.

The decay curve from the oxygen sample was constructed from 143 sets of spectral data. Because both <sup>11</sup>C and <sup>18</sup>F do not have a coincident gamma ray associated with their decay, the shape of the oxygen spectra was quite similar to that of the carbon data shown in Fig. 17.

# Decay Curve Analysis

Since the activation products from <sup>3</sup>He irradiations are usually neutron deficient, they normally decay by positron emission. Many of the activation products are pure positron emitters as in the case of <sup>18</sup>F and <sup>11</sup>C. One way to determine the amounts of these isotopes present in a sample is by counting the 0.51 MeV annihilation radiation for various time intervals and unfolding the complex decay curve into its components. The DEcay CURve Analysis code, DECURA, was written to analyze complex decay curves obtained during <sup>3</sup>He activation analysis studies. The function

$$Y(J) = P(1)*\sum_{I=1}^{NOI} P(I*2)*EXP(P(I*2+1)*X(J))$$

is fitted to the decay curve data using least-squares techniques. The J subscript refers to the Jth data point, and the I subscript refers to the Ith exponential or component. The best least-squares value can be obtained for each of the P(I) variables in the equation. Y(J) is the decay rate in counts/sec that is obtained by integrating the pulse-height spectra. X(J) is the elapsed time since the irradiation stopped. No provision is made for correcting for decay during the counting interval.

The code uses pulser data to determine the live time during the counting interval.

The output that is used from this code is the counts/sec for each isotope extrapolated to the time the irradiation stopped. Figure 18 shows the analysis of the complex decay curve from the carbon data. The experimental data are analytically represented by four exponentials. These four exponentials, their sum, and the experimental data points are shown on the plot. The main component, with a 20.3-min calculated halflife, is from  $^{11}$ C, the reaction product from the  $^{12}$ C( $^{3}$ He, $\alpha$ ) $^{11}$ C reaction. The analysis indicates the presence of a component with a 7.7-min halflife. This is probably mostly due to the presence of 13N from the 12<sub>C</sub>(3<sub>He,d</sub>)<sup>13</sup>N reaction, but the calculated number could also be influenced by the presence of  $^{15}$ 0 from the  $^{16}$ 0( $^{3}$ He, $\alpha$ ) $^{15}$ 0 reaction at the very early times. The presence of a small amount of 18 from the 160(3He,p)18 reaction from body and surface oxygen associated with the tantalum is also indicated. The half-life of this component was fixed during the calculation at 110 min. The presence of a small amount of long half-lived products is indicated from the fit. The uncertainty associated with the results of this fit are probably an upper limit as calculated in the leastsquares code. This is from the rather large variance due to statistical

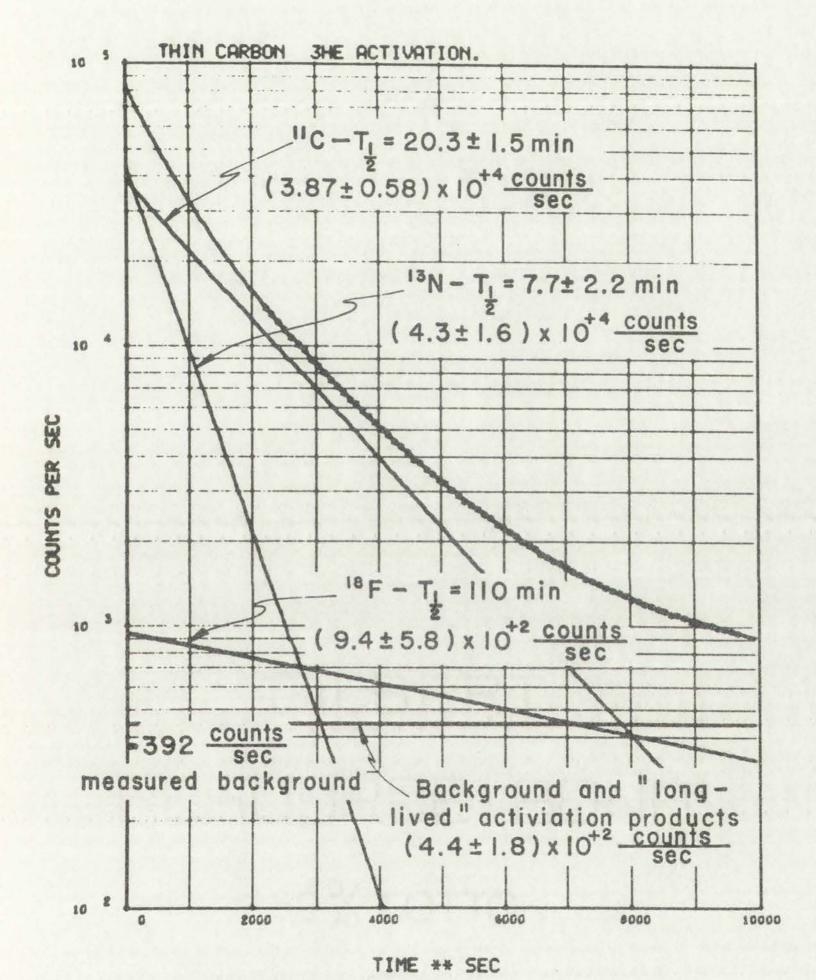
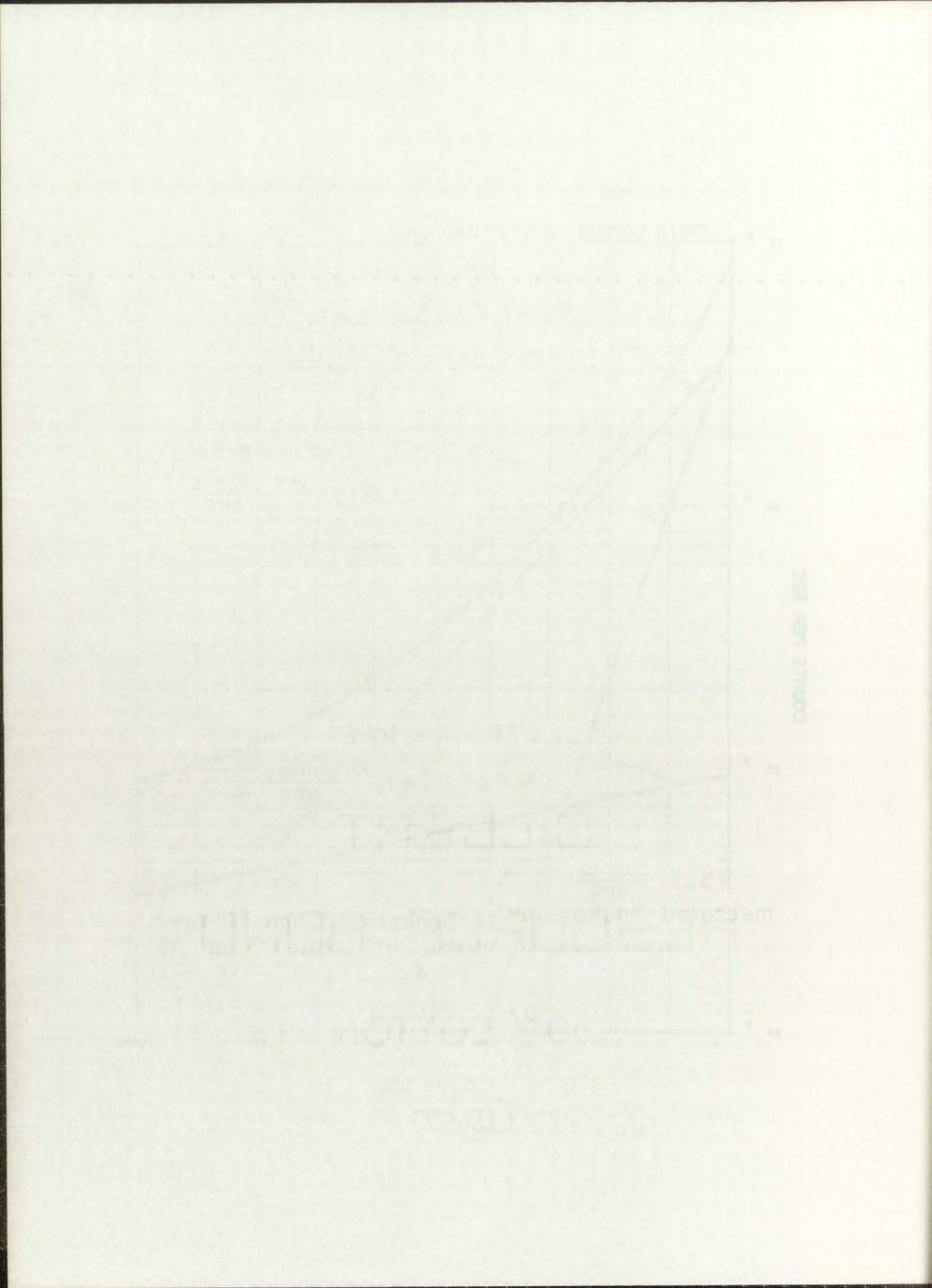


Fig. 18. Unfolded complex decay curve from activated carbon sample.



fluctuation in the live-time determination. The results of this analysis are given in Table 2.

Code DECURA is discussed in Appendix A.

TABLE 2
RESULTS FROM ANALYSIS OF CARBON ACTIVATION SAMPLE

Isotope Assigned	Half-Life Calculated (min)	Relative Decay Rate at Time Zero (counts/sec)
11 <sub>C</sub>	20.3 <u>+</u> 1.5	$3.8 \pm 0.6 \times 10^4$
13 <sub>N</sub>	7.7 <u>+</u> 2.2	$4.3 \pm 1.6 \times 10^4$
18 <sub>F</sub>	110. (fixed see above)	$9.4 \pm 5.8 \times 10^2$
	long-lived	$0.5 \pm 0.2 \times 10^2$

# Calculation of the Target Thicknesses

A computer code, SVCCPA (Surface and Volumetric Concentrations from Charged Particle Activations), was written to determine the volumetric and corresponding surface concentration of the activation product from the unfolded decay curve data. This code is discussed in Appendix B.

The beam current history tape generated during the irradiation is used to correct for fluctuations in the beam current during the irradiation. Analytical representation of the  $^3$ He cross-section data of Markowitz and Mahony (Ref. 2) and Cochran and Knight (Ref. 18) are used in the code. The cross section as a function of  $^3$ He energy is fitted with a combination of Gaussians and exponentials. This code, GHLET (Gaussian with High and Low Energy Tails), is discussed in Appendix C. It has been quite useful in the analysis of cross-section data and other experimental data where the distributions are basically of a Gaussian or Lorentzian shape. The analytical representation of the  $^{12}\text{C}(^3\text{He},\alpha)^{11}\text{C}$  cross section is shown in Fig. 19.

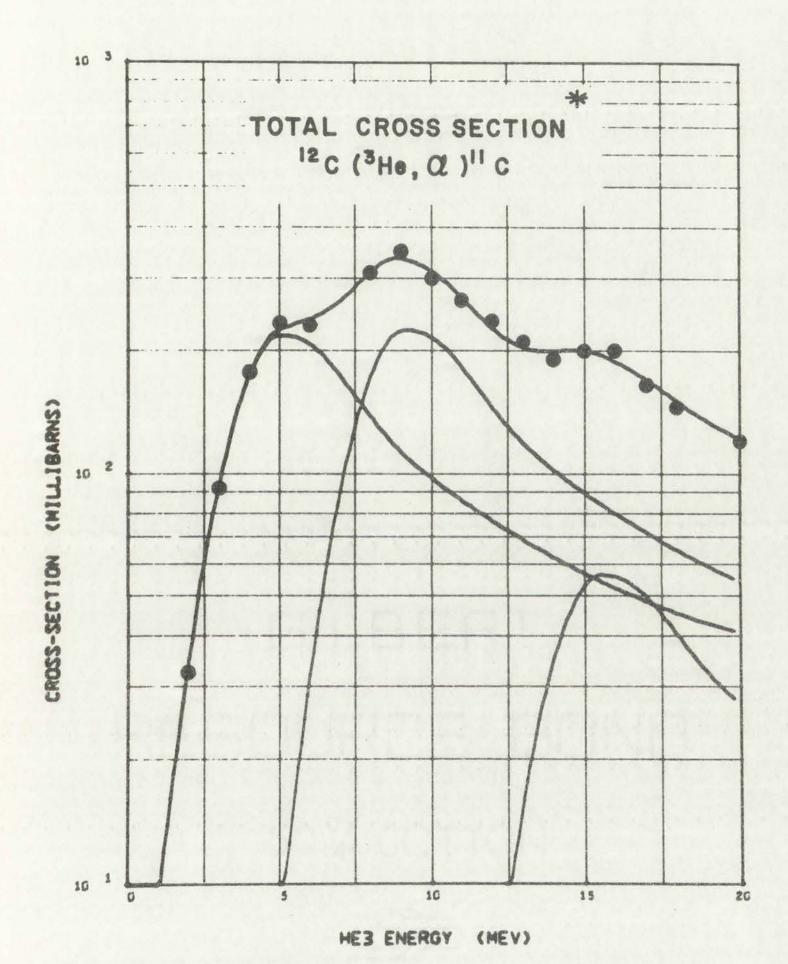
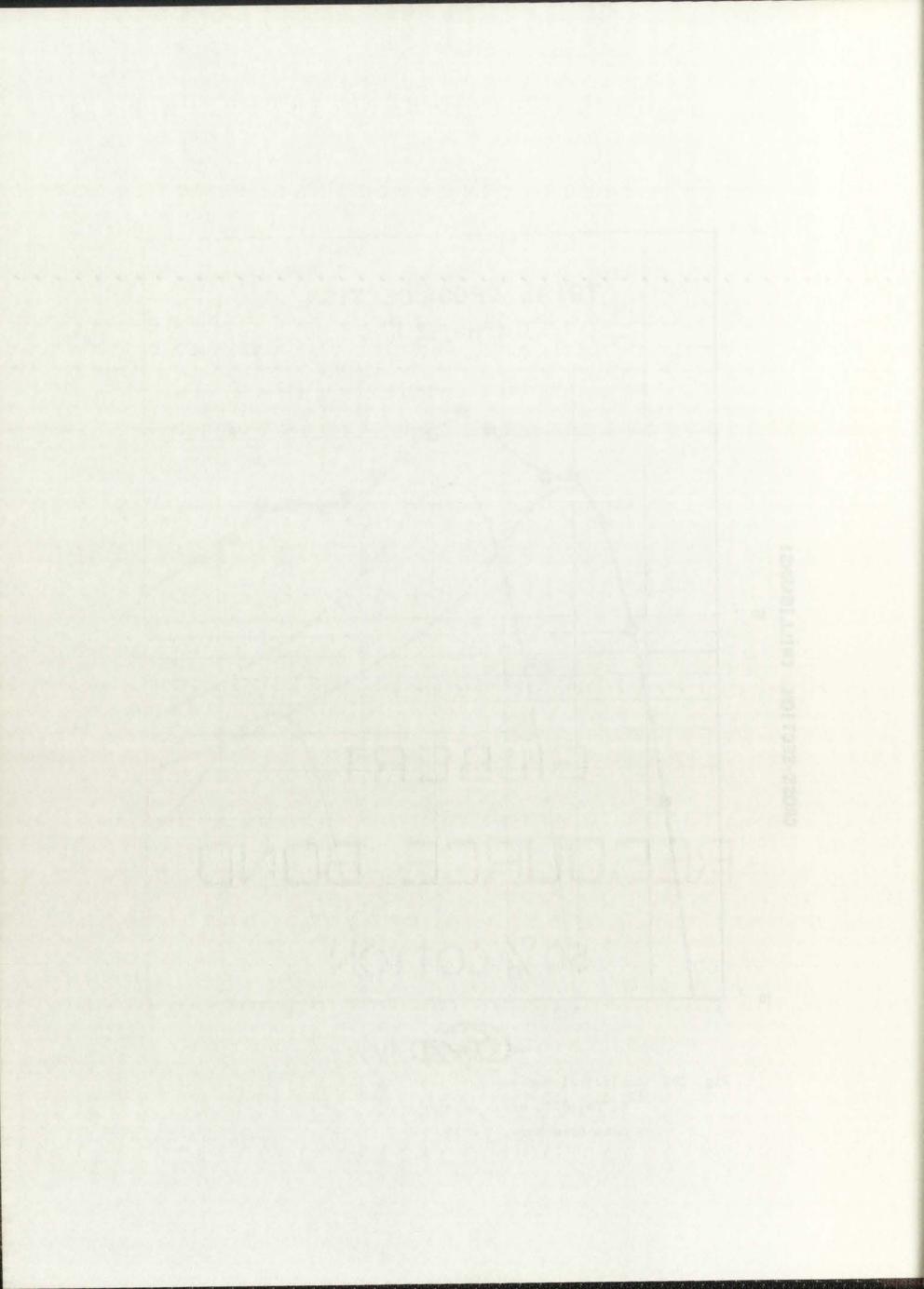


Fig. 19. Analytical representation of the  $^{12}\text{C}(^3\text{He},\alpha)^{11}\text{C}$  cross section. \* Data from Refs. 2 & 18.



Corrections are made in SVCCPA for detector efficiency and branching ratios. In this experiment, the detector efficiency was approximately 100% due to the size of the detector system and the fact that there are two photons per positron decay. The branching ratio used for <sup>18</sup>F was 97% (Ref. 21) and for <sup>11</sup>C was 100% positron decay.

Concentrations of the impurity atoms are calculated assuming that they are all on the surface and also assuming a homogeneous volumetric concentration. Of interest in this calibration data was the surface concentration since both samples had thin layers deposited on their front surfaces. In the volumetric calculation, the position of the <sup>3</sup>He particle is determined as it penetrates the sample from the dE/dx data for each 0.01 MeV energy increment.

$$\frac{dE}{dx} = s(E)$$

$$\Delta x = x_2 - x_1 = \int_{E_1}^{E_2} \frac{1}{s(E)} dE$$

The integral  $\int_{E_1}^{E_2} \frac{1}{s(E)} dE$  is determined numerically from the integration of the cubic spline interpolation function of  $\frac{1}{s(E)}$ . The use of the interpolatory cubic spline functions and the stopping power data used in this experiment are discussed further in Chapter IV.

The average cross section between  $\mathbf{E}_1$  and  $\mathbf{E}_2$  for each energy step is given by

$$\int_{0}^{E_{2}} \sigma(E) dE$$

$$\bar{\sigma} = \frac{E_{1}}{E_{2} - E_{1}} .$$

The integral,  $\int_{E_1}^{E_2} \sigma(E) \ dE$ , is evaluated by numerical methods. The cross section as a function of energy,

$$\sigma(E) = g(E)$$
,

is the analytical representation of the experimental cross section obtained from GHLET.

In these calculations, it is assumed that the number of particles in the beam remains constant as it penetrates the sample. This is to say that energy losses are due primarily to ionization and that reaction and other hard cross sections are small. In the above calculations, the cross sections become small enough at low energies that the calculation can be terminated once the <sup>3</sup>He energy reaches 1 MeV.

# Prompt Proton Data

The prompt proton data from these samples were recorded during the irradiations using a silicon surface barrier detector, a 512-channel analyzer, and ancillary electronics. Reaction alphas and backscattered  $^3\mathrm{He}$  particles were absorbed in three 25  $\mu$  aluminum foils between the detector and target to prevent their energy deposition in the detector. The detector was located at 160° from the incident beam direction. The proton spectrum from the carbon irradiation are shown in Fig. 20, and the corresponding data from the oxygen irradiation is shown in Fig. 21. Detailed analyses of these data and the techniques used to analyze the proton spectra are presented in Chapter IV. The total  $^3\mathrm{He}^{++}$  charge collected during the carbon irradiation was 1.2 x 10 $^{-4}$  C and during the oxygen irradiation was 2.4 x 10 $^{-4}$  C.

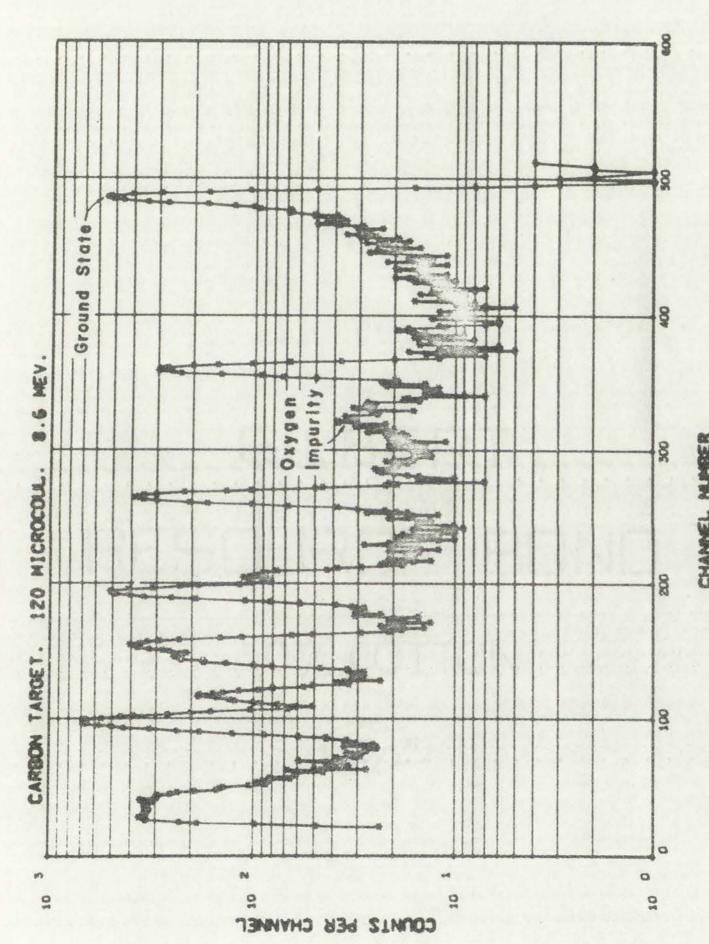
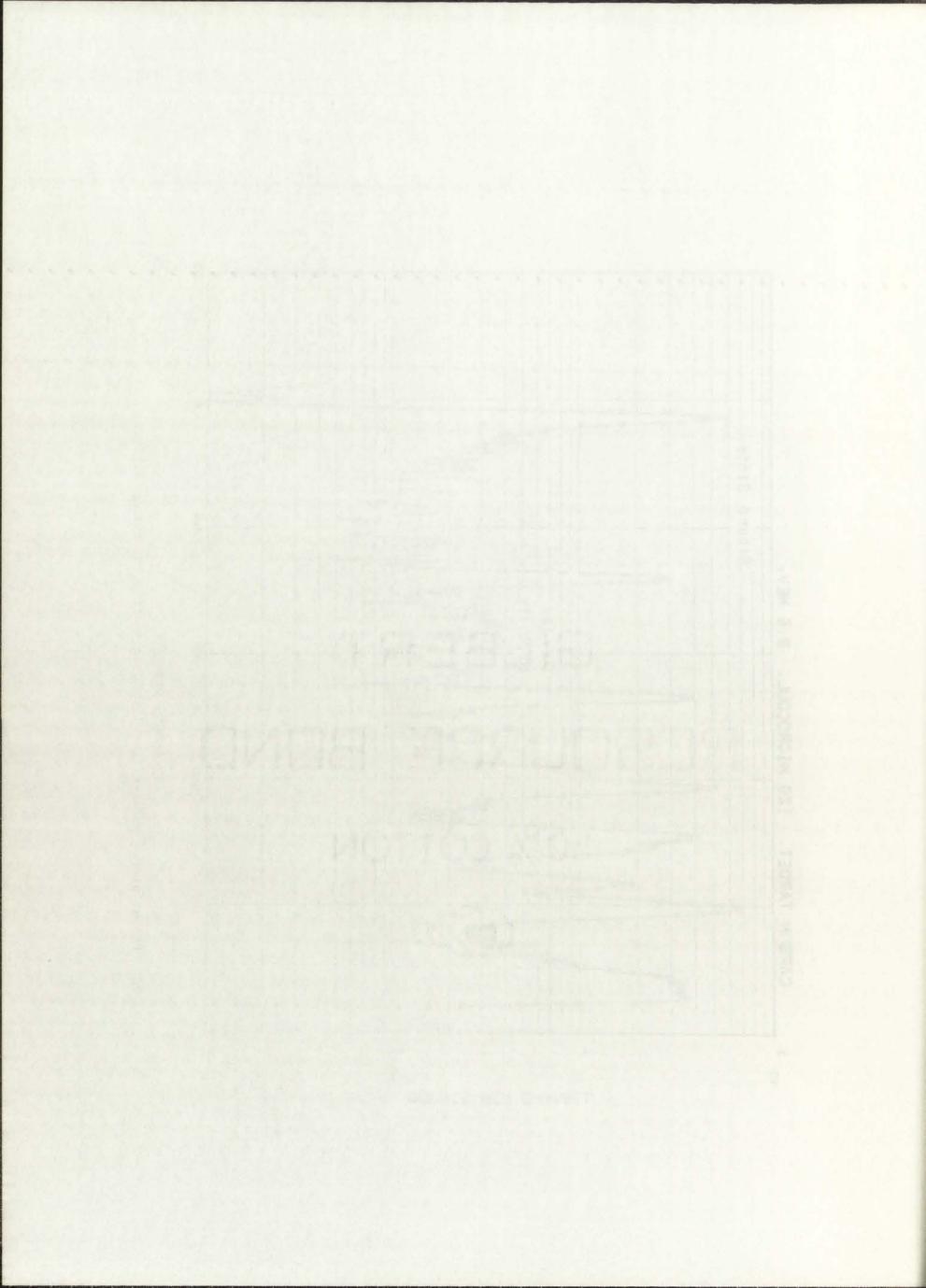


Fig. 20. Prompt proton pulse-height distribution from the carbon activation,



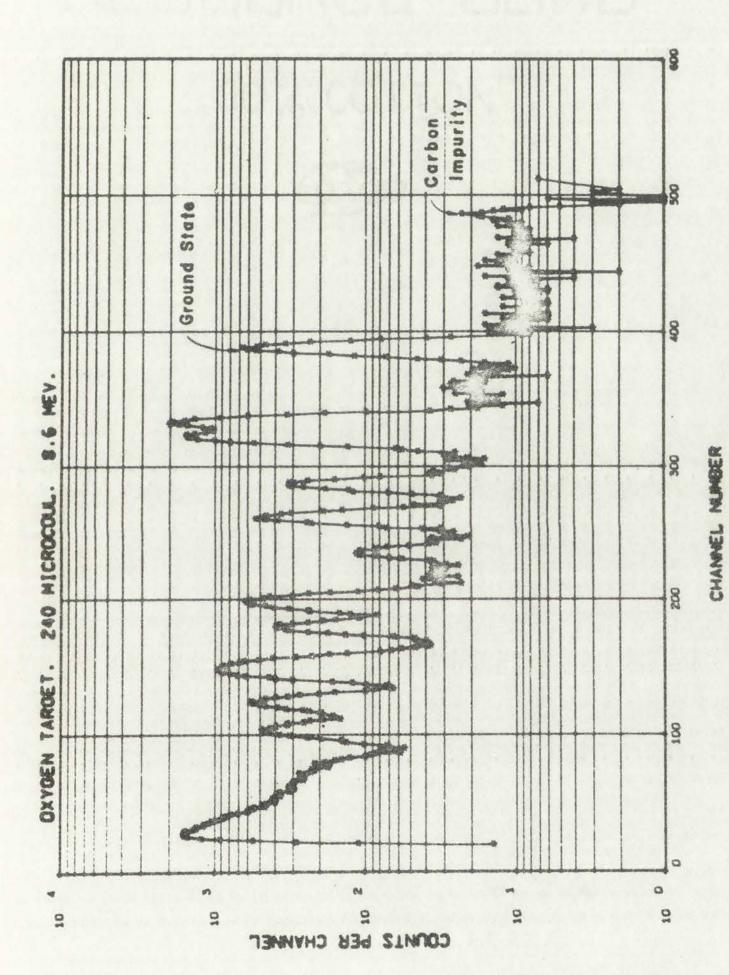
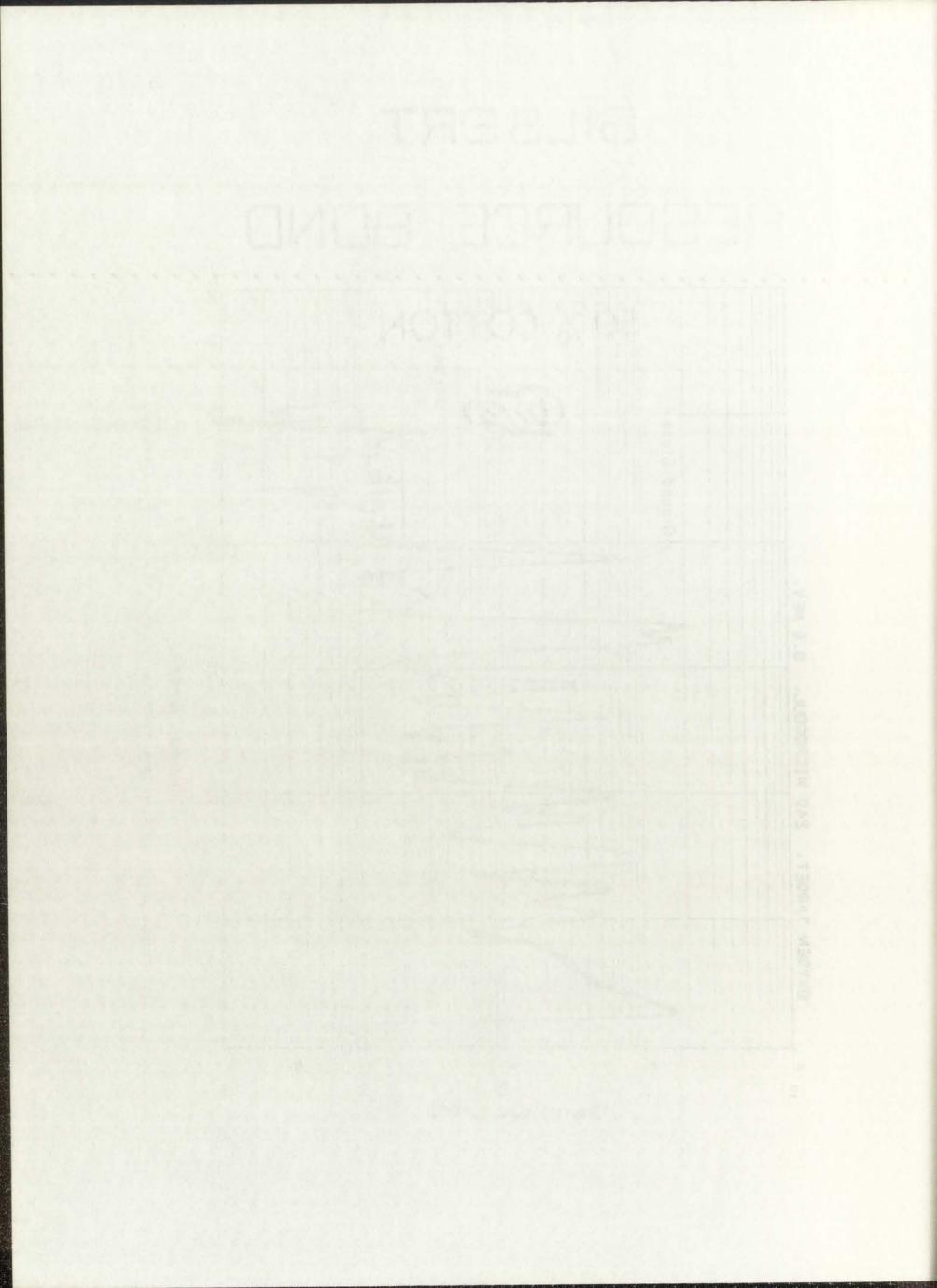


Fig. 21. Prompt proton pulse-height distribution from the oxygen activation.



## Results

The thickness of the carbon layer on the carbon target was calculated to be  $15.9 \pm 0.9 \, \mu \mathrm{g/cm}^2$ . The thickness of the  $\mathrm{Ta_2^0}_5$  layer on the oxygen target was calculated to be  $47.6 \pm 2.8 \, \mu \mathrm{g-oxygen/cm}^2$ . This latter value is 20% lower than that calculated from data presented by Kover and Musselin (Ref. 22). However, a direct comparison probably **should** not be made since the variations of layer thickness with temperatures and current densities are significant. There were insufficient data to make these corrections; however, the 20% lower thickness is an indication of the higher current density and higher temperature used in this experiment. Davies et al. (Ref. 23) report a 10% decrease in the oxide layer thickness as the current densities were increased from 0.1 mA to 10 mA. The peak current density used in this experiment was approximately 100 mA. A summary of these results is given in Table 3.

TABLE 3

RESULTS OF PASSIVE CALIBRATION<sup>†</sup>

	Carbon	<u>Oxygen</u>	Ta205
Thickness (µg/cm <sup>2</sup> )	15.9 ± 0.9	47.6 <u>+</u> 2.8	263.1
He energy loss (keV)* in layer at 8.6 MeV	6.9		54.1
Proton energy loss (keV)* in layer at 5.0 MeV	small		9.4

<sup>\*</sup>Calculated using dE/dx data from Ref. 24

 $<sup>^{\</sup>dagger} The \ corresponding \ thicknesses$  that are consistent with the thick target data are 18.8 and 33.6  $\mu g/cm^2$  .

#### CHAPTER IV

#### CALCULATIONS AND DATA ANALYSIS

#### Introduction

One of the objectives of this experiment was to determine the body concentrations of carbon and oxygen impurities in various materials including germanium, which is used in the manufacture of Ge(Li) detectors. In addition to the body concentrations, the surface concentrations of oxygen had to be determined because these materials readily oxidize when exposed to air. Some experimenters have bombarded the sample to be investigated with charged particles and then have removed the surface in small amounts. The amount of material removed and the activities present in this material are determined. These techniques can be used if the range of the bombarding particle is large compared to the recoil ranges of the reaction products; however, the short range of the 3He particles used in this experiment and the large positive Q of the reactions cause ranges for the recoil atoms that are large enough to give erroneous results. This is particularly true for the bombardment of crystalline materials where channeling of the recoil atoms can greatly increase their range. These problems do not exist with the prompt activation analysis techniques that were used in this experiment.

Experiments using anodizable materials and controlled anodizing with chemical etching techniques to remove thin layers from the surface of the material have been quite successful (Ref. 9) in determining the recoil ranges of heavy ions incident on amorphous, polycrystalline, and single-crystalline materials.

The thin target excitation functions were determined with good resolution so that the various proton groups could be unfolded from the complex spectra. These complex proton spectra were unfolded using least-squares techniques similar to those presented in Ref. 25. The differences and additions to the code in order to unfold the proton spectra, instead of high-resolution gamma-ray spectra, are presented in Appendix D.

The thin carbon targets were approximately 19  $\mu g/cm^2$ , and the thin oxygen targets were approximately 34  $\mu g/cm^2$ . The solid angle of the silicon surface barrier detector was 3.08 x  $10^{-3}$  sr.

### Energy Loss Calculations

The energy of the <sup>3</sup>He particles versus distance traversed in the target and the energy of the reaction protons at the detector were determined using numerical techniques and stopping-power data from Refs. 26 and 24. The data from these references were based on observed experimental measurements and simple theoretical extrapolations guided by theoretical expectations.

The stopping-power data,

$$\frac{dE}{dx} = s(E) ,$$

were interpolated using cubic spline functions. The cubic splines as they were used in the numerical representation of the stopping-power data are discussed in Appendix E. The objective of the numerical manipulation of the stopping-power data was to obtain the function  $\mathbf{x} = \mathbf{f}(\mathbf{E})$  and the inverse function  $\mathbf{E} = \mathbf{F}(\mathbf{x})$  for a 12-MeV particle incident on the material. Twelve MeV was chosen for the upper energy because it represented an upper bound for the particle energies of interest.

Figure 22 shows E = F(x) for  $^3$ He particles and protons in germanium. The energy losses of the  $^3$ He particles as they traversed the target material and the energy losses of the protons in the target and in the backscatter absorber foil were determined using the E = F(x) and x = f(E) interpolation functions in the following manner. All of the thick target energy loss data start with a particle energy of 12 MeV and stop when the particle energy reaches 1 MeV. These energies represented the upper and lower bounds on the particle energies of interest. If we were to determine the energy loss of an 8-MeV proton as it passes through a  $100-\mu$  germanium foil, the function x = f(8.0) would be evaluated to determine the initial x displacement,  $x_0$ , that gave an energy of 8.0 MeV. Then, the function  $E = F(x_0 + 0.01)$  would be evaluated to determine the proton energy after passing through the foil. These and similar calculations are performed for all energy loss calculations. The x displacements are in cm and the particle energies are in MeV.

# Thin Target Excitation Functions

The thin target excitation functions for the various excited states from the  $^{12}\text{C}(^3\text{He,p})^{14}\text{N}$  and  $^{16}\text{O}(^3\text{He,p})^{18}\text{F}$  reactions were determined over the  $^3\text{He}$  energy range of 2.5 to 9.0 MeV using thin oxygen and carbon targets. A computer code was then used to unfold the complex pulse-height distributions that were obtained from the reaction protons. This code was referred to as C24HE3P and is discussed in Appendix D. The results of the spectral unfolding of the carbon and oxygen spectra from the calibration irradiations discussed earlier are shown in Fig. 23 for carbon and in Fig. 24 for oxygen. The proton spectra were obtained at a  $^3\text{He}$  particle energy of 8.6 MeV and a detector angle of  $160^\circ$ . The spectra are shown after the protons had passed through a  $76.2-\mu$  aluminum foil

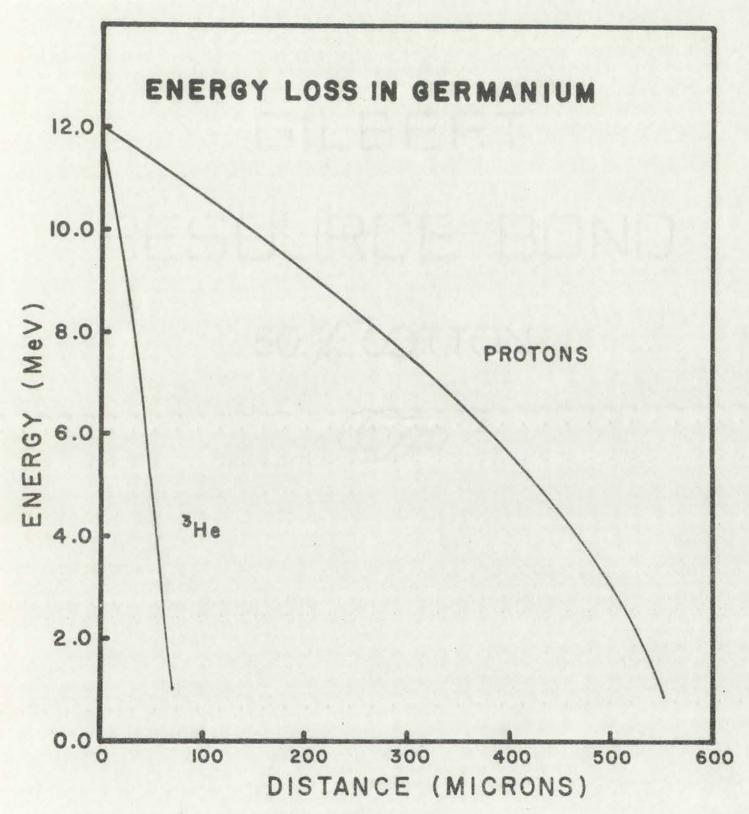
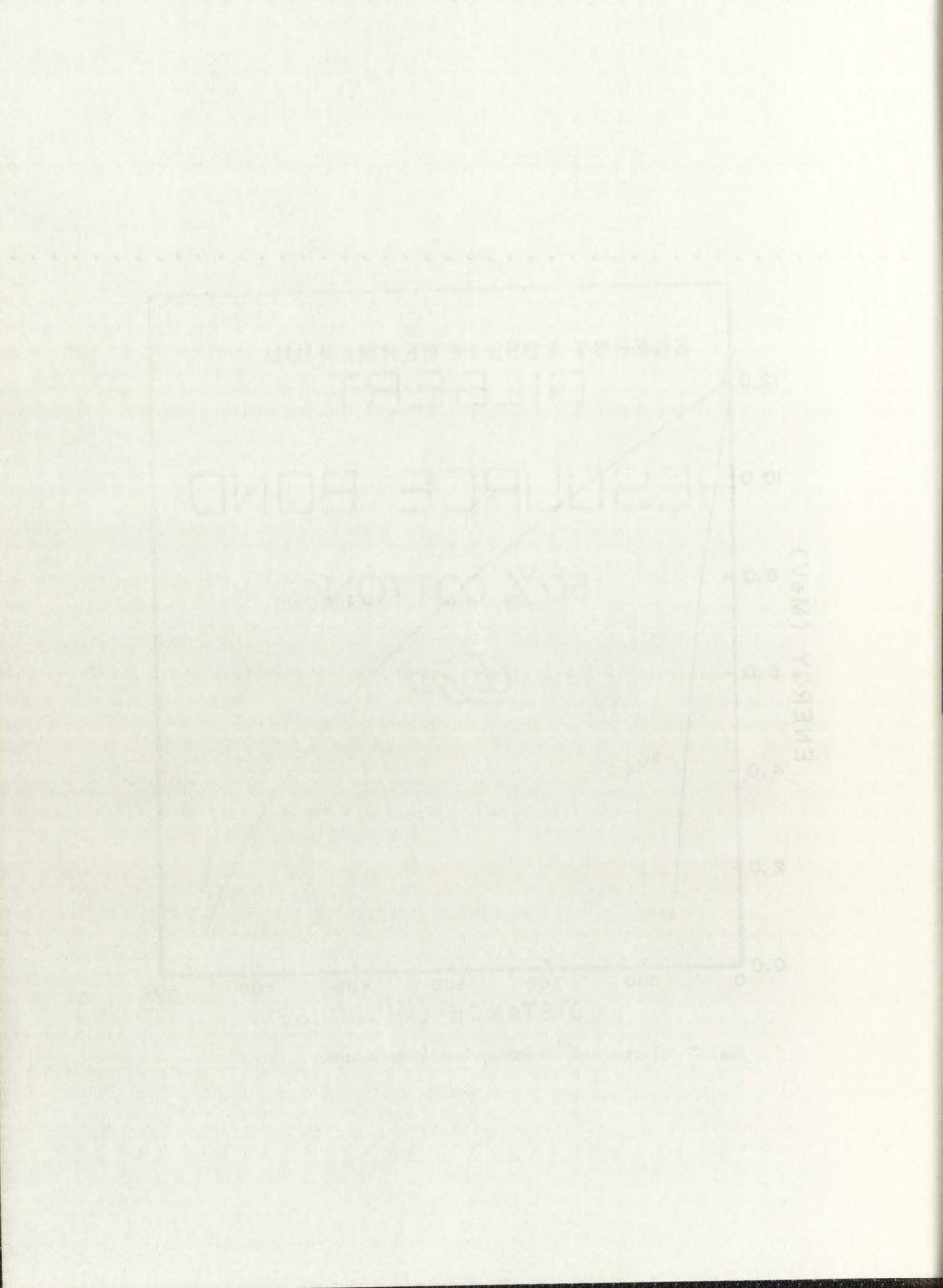
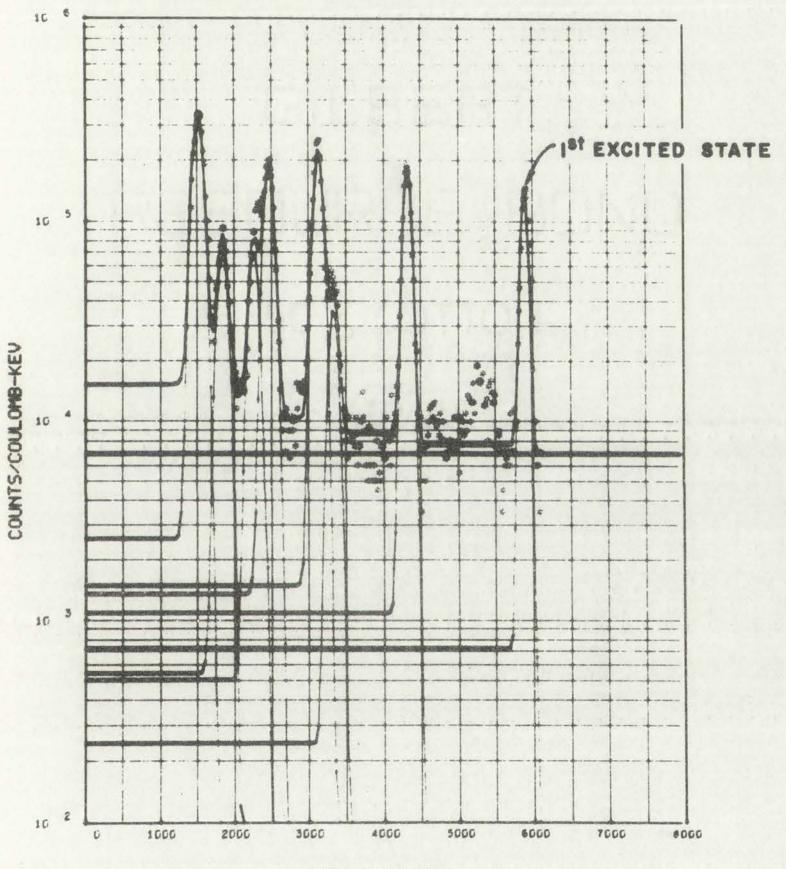


Fig. 22. Proton and <sup>3</sup>He energy loss in germanium.

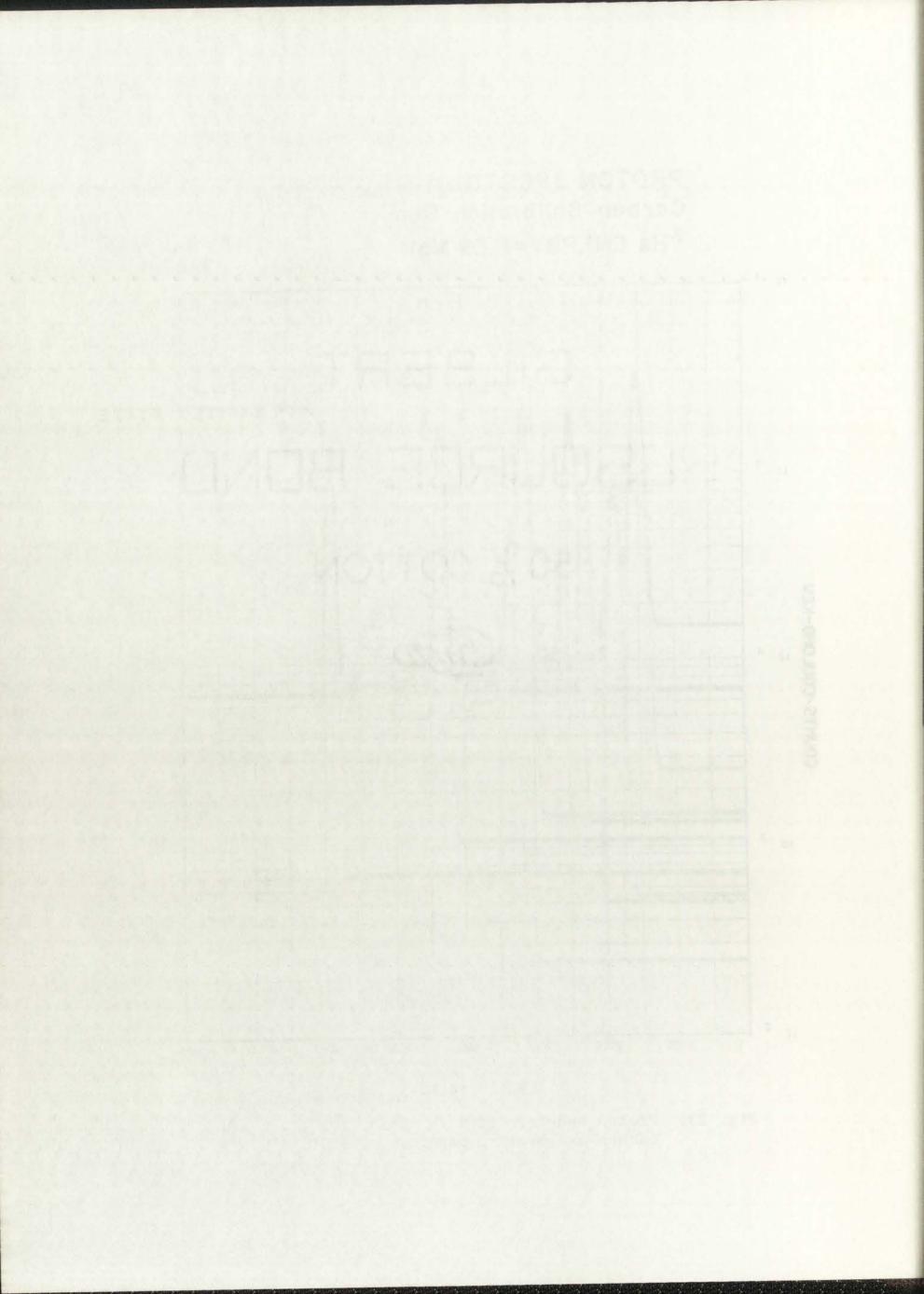


# PROTON SPECTRUM Carbon Calibration Run 8 He ENERGY = 8.59 MeV



ENERGY \*\* KEV

Fig. 23. Proton spectrum from the thin carbon calibration sample.



# PROTON SPECTRUM Oxygen Calibration Run 3 He ENERGY = 8.54 MeV

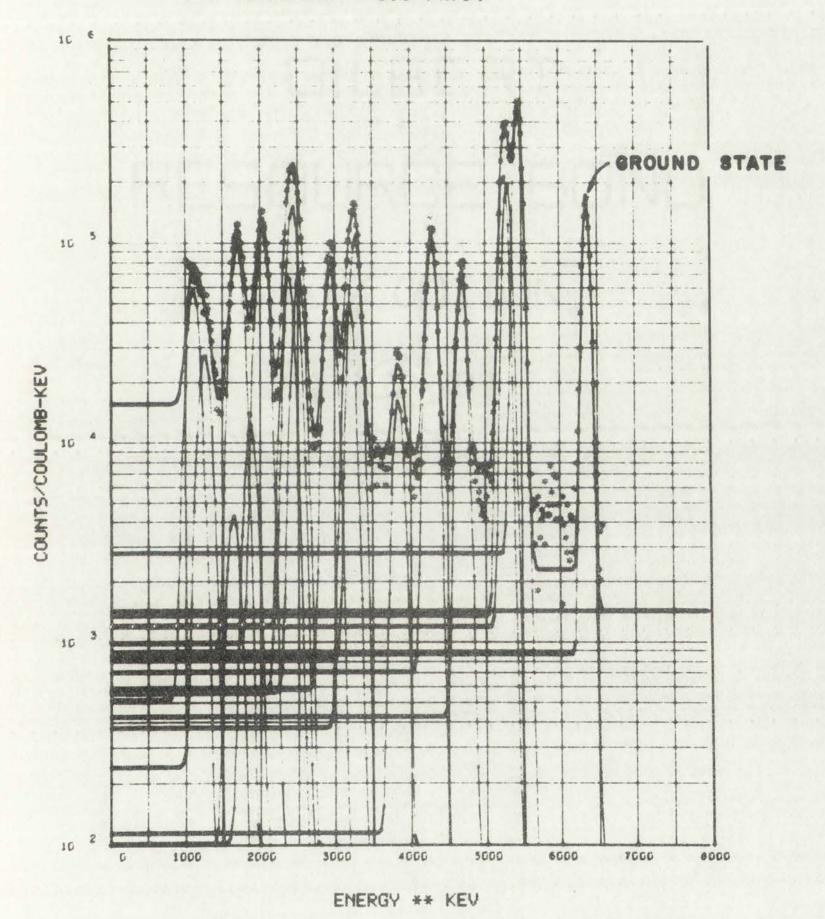
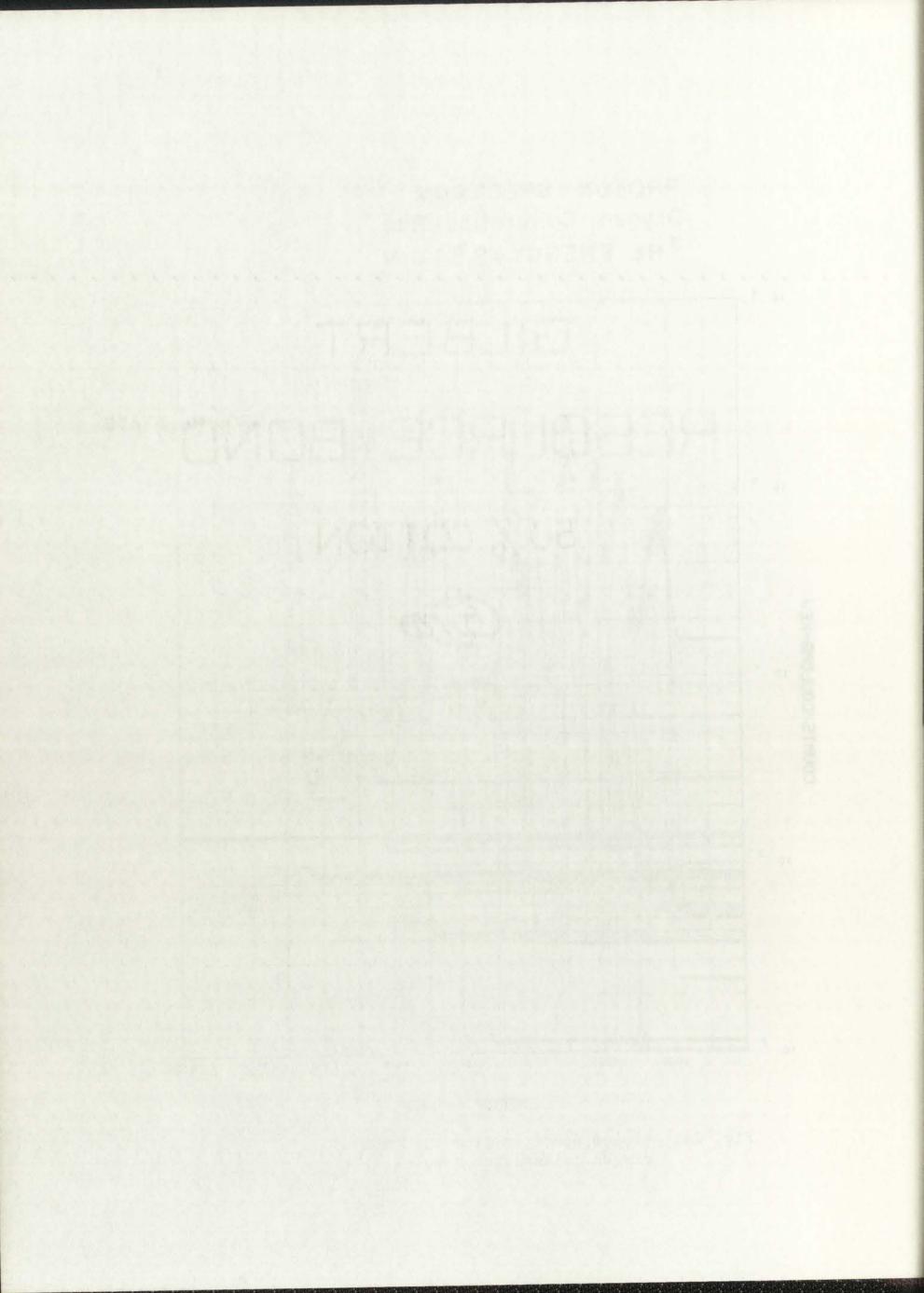


Fig. 24. Proton spectrum from the thin oxygen calibration sample.

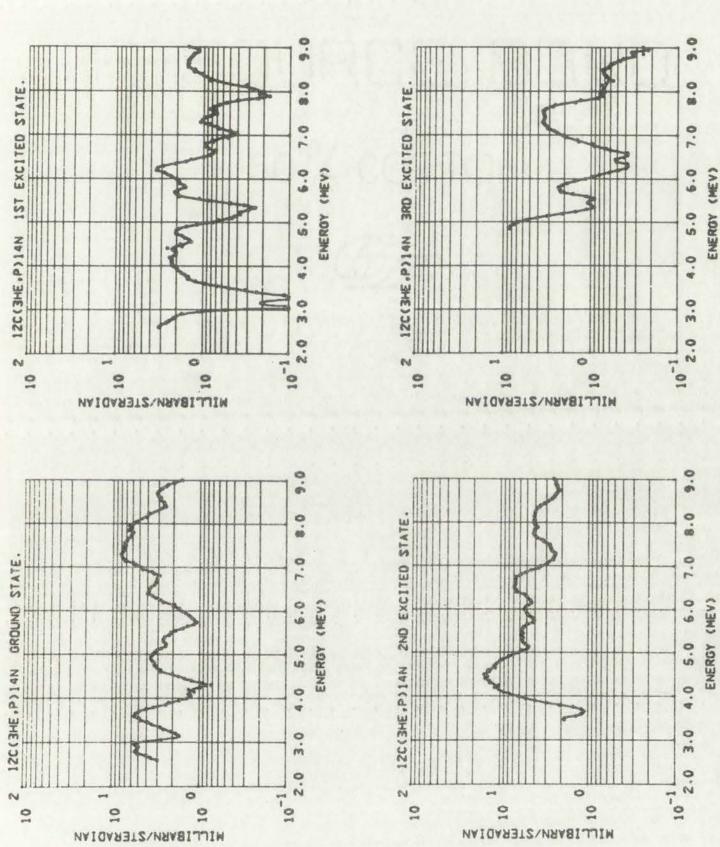


that was used to prevent the backscattered <sup>3</sup>He particles from striking the detector. These proton spectra were unfolded from about 1 MeV to slightly above the ground-state peak. The proton spectrum for carbon shown in Fig. 23 is one of the few exceptions. In this case, the range of the ground-state proton exceeded the depletion depth of the detector and caused this peak to appear at a lower energy than expected. Therefore, it has not been considered in this analysis.

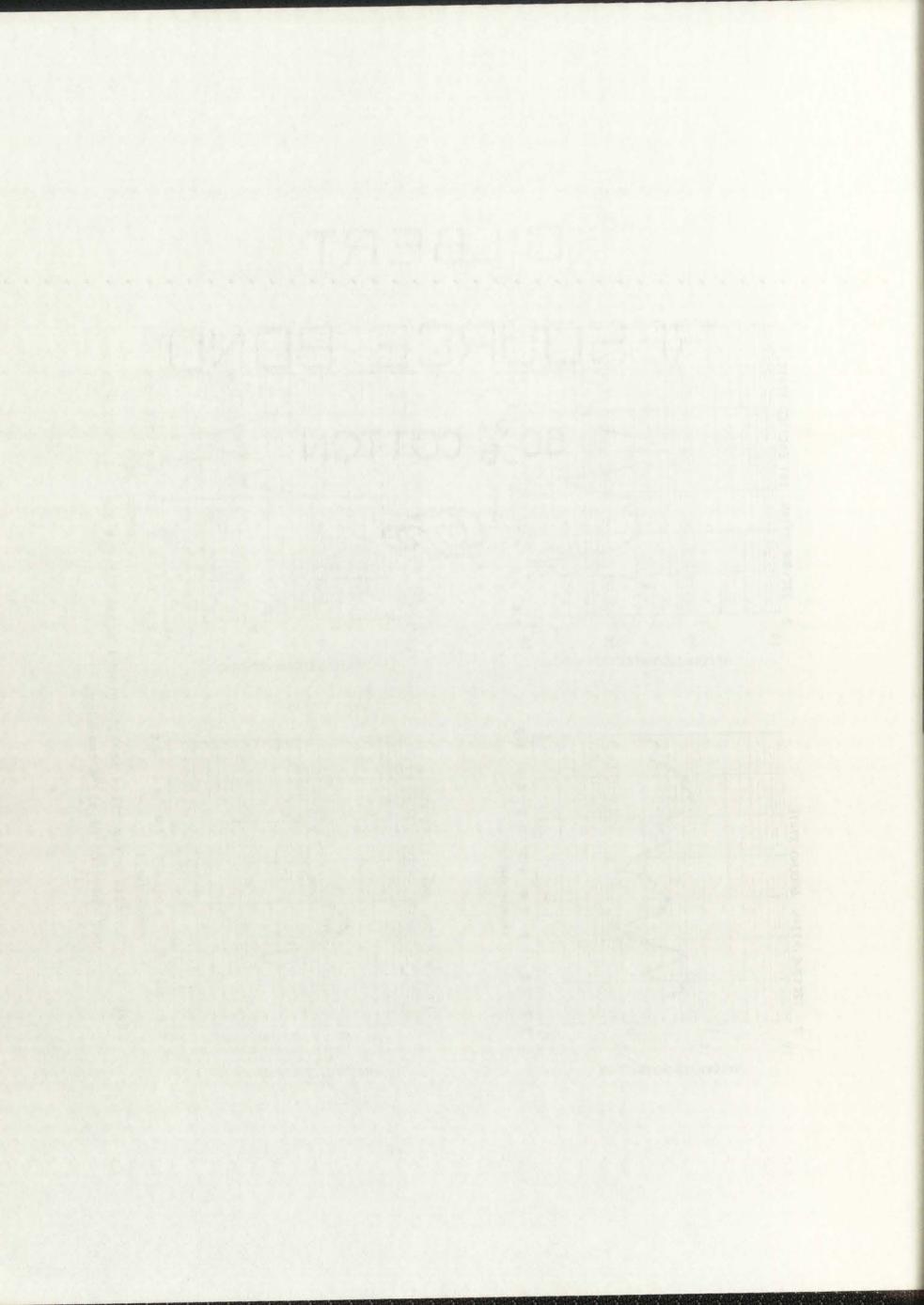
The thin target excitation functions for the first ten energy states of the  $^{12}\text{C}(^3\text{He,p})^{14}\text{N}$  reactions are presented in Figs. 25 through 27. The thin target excitation functions for the first twenty energy states of the  $^{16}\text{O}(^3\text{He,p})^{18}\text{F}$  reactions are presented in Figs. 28 through 32. The smooth lines through the data were obtained using cubic spline smoothing techniques. Resonance effects from the virtual energy levels in the compound nuclei are quite evident.

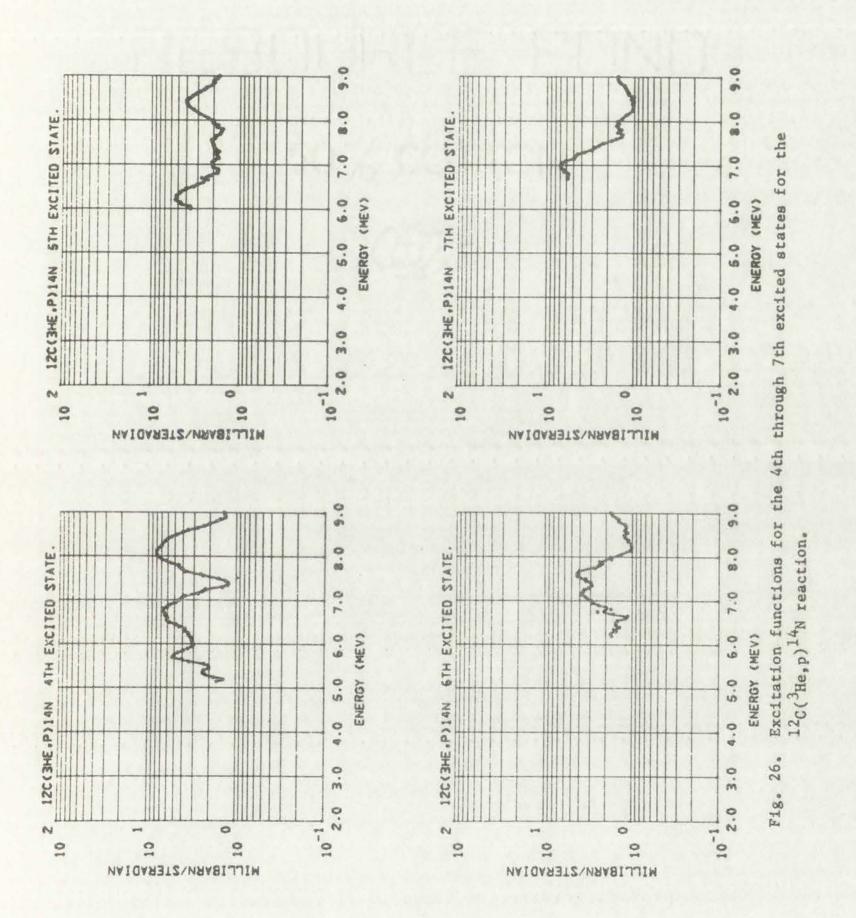
#### Nuclear Energy Levels

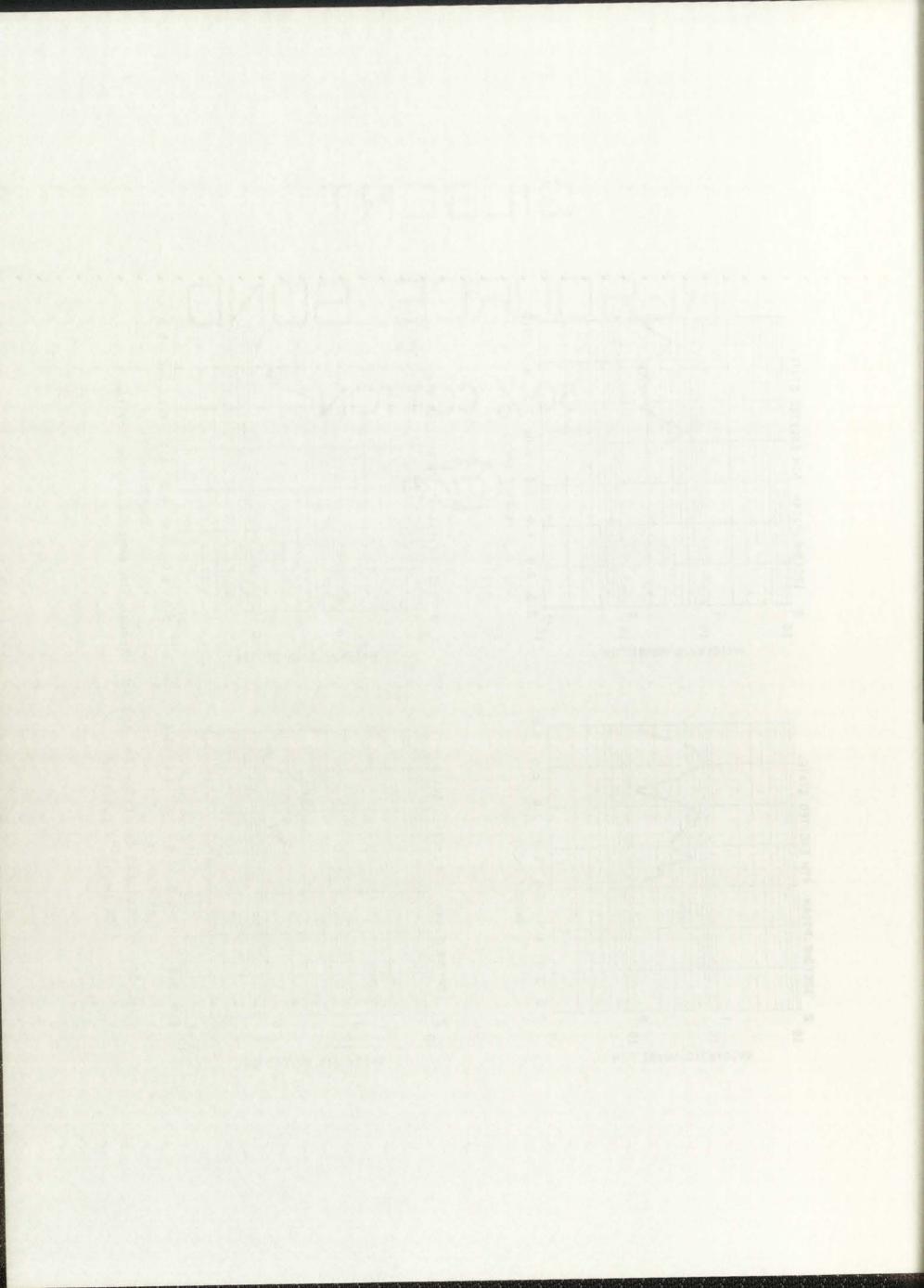
The reaction products, <sup>14</sup>N and <sup>18</sup>F, are sometimes left in an excited state and decay to the ground state by gamma-ray emission. Before kinematics can accurately calculate the proton energies, an accurate knowledge of these prompt gamma-ray energies is necessary. At the time the excitation functions were measured, published values for these gamma-ray energies were not well known. Therefore, the prompt gamma-ray spectra were recorded for many of the bombardments using a Ge(Li) detector system. The standard target chamber was designed so that such a detector could be placed close to the target (approximately 1 in. from the irradiated area) but outside the accelerator vacuum system with a minimum amount of absorbing material between the target and the detector. Typical pulse-height distributions from the prompt gamma rays are shown in Fig. 33 for a carbon irradiation



Excitation functions for the ground state through the 3rd excited state for the 12C(3He,p)14N reaction. Fig. 25.







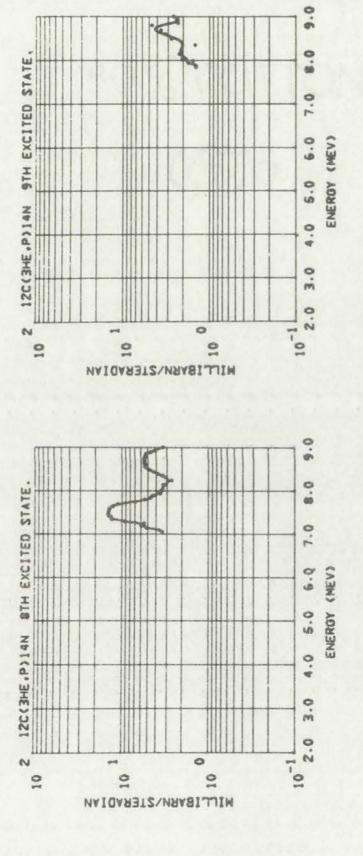
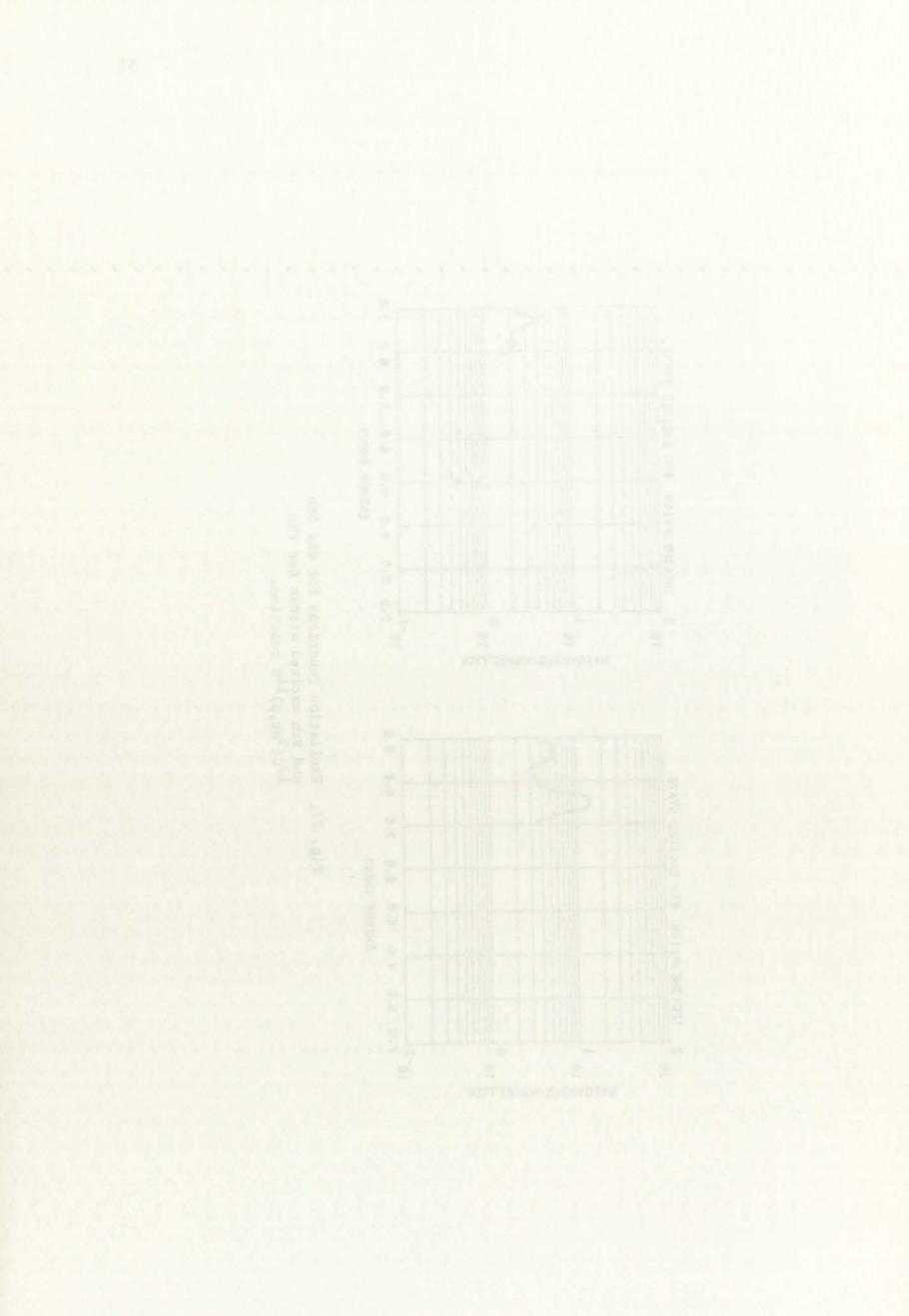
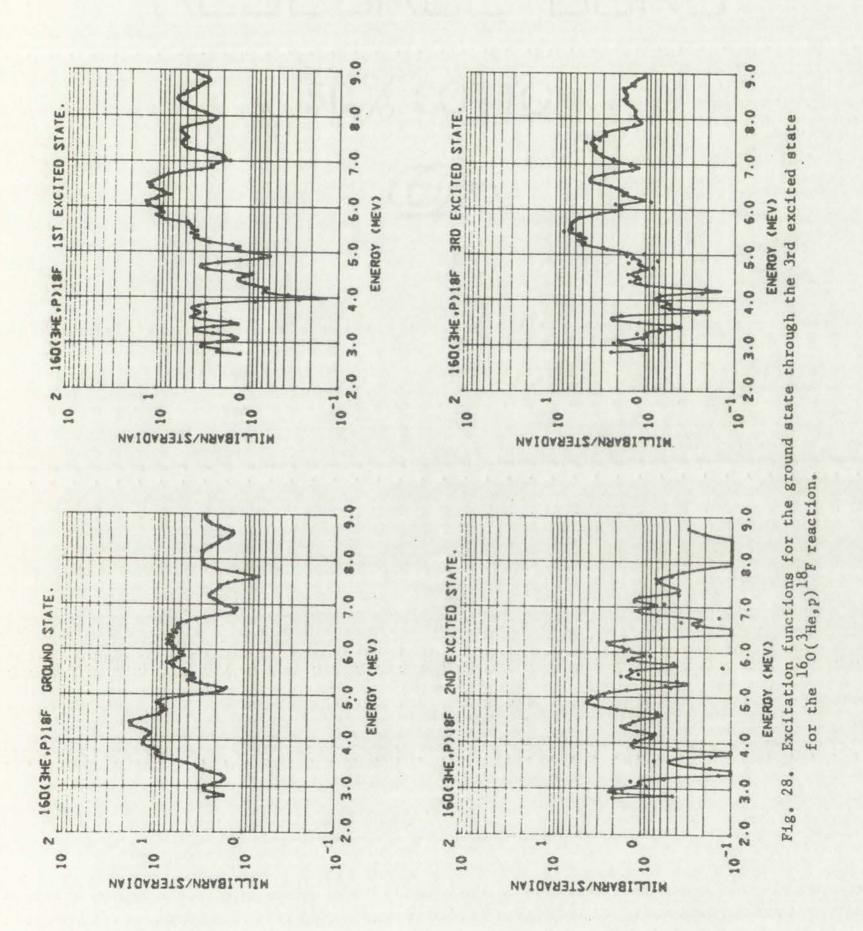
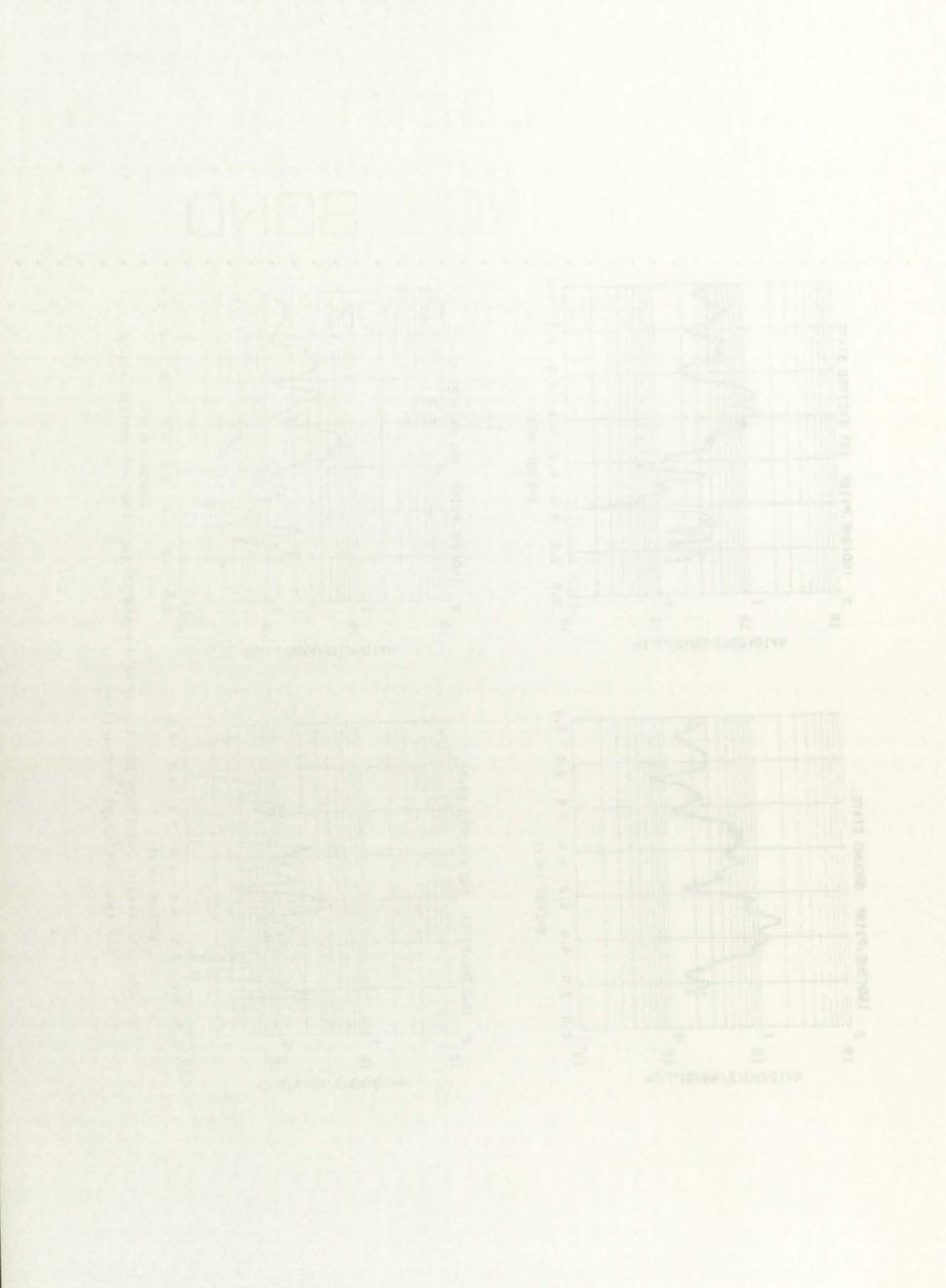
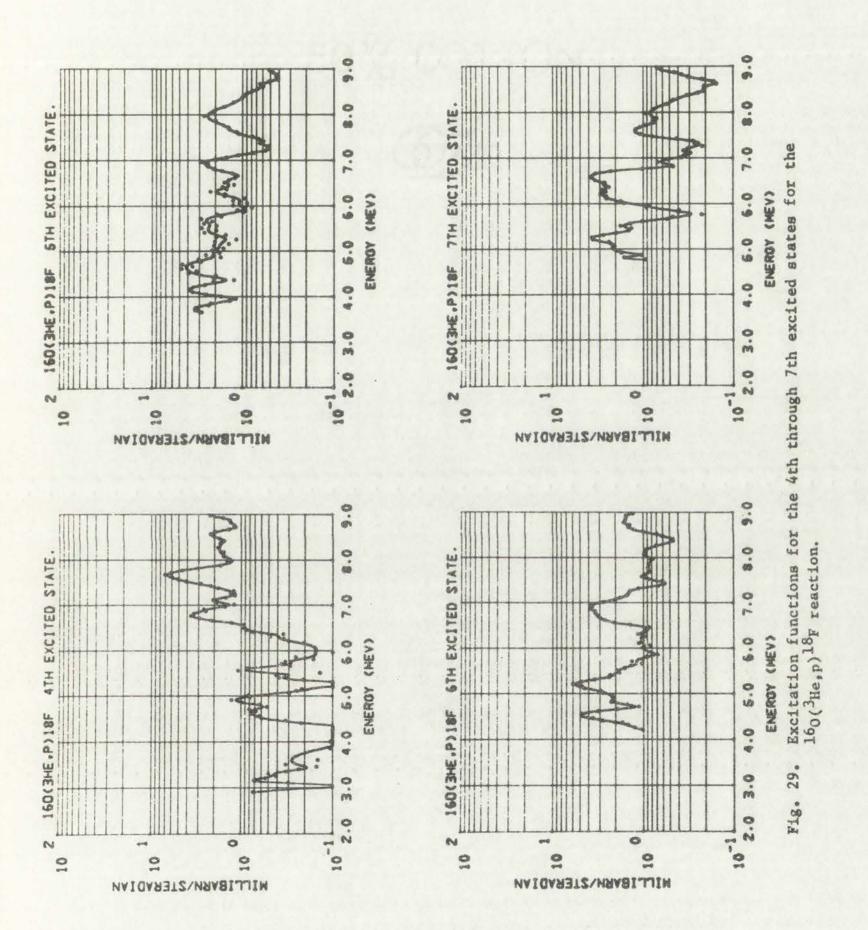


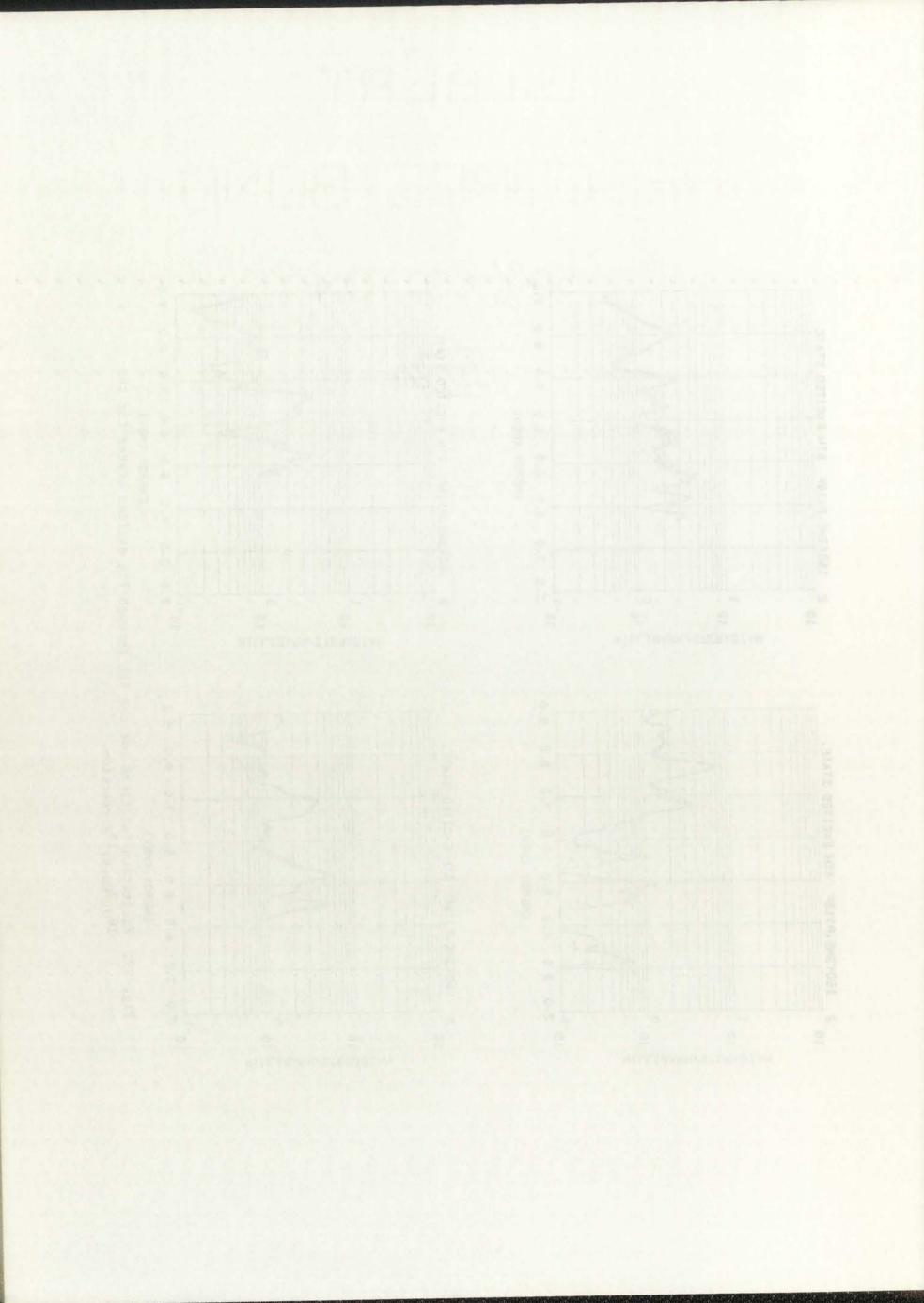
Fig. 27. Excitation functions for the 8th and 9th excited states for the 12C(3He,p)14N reaction.

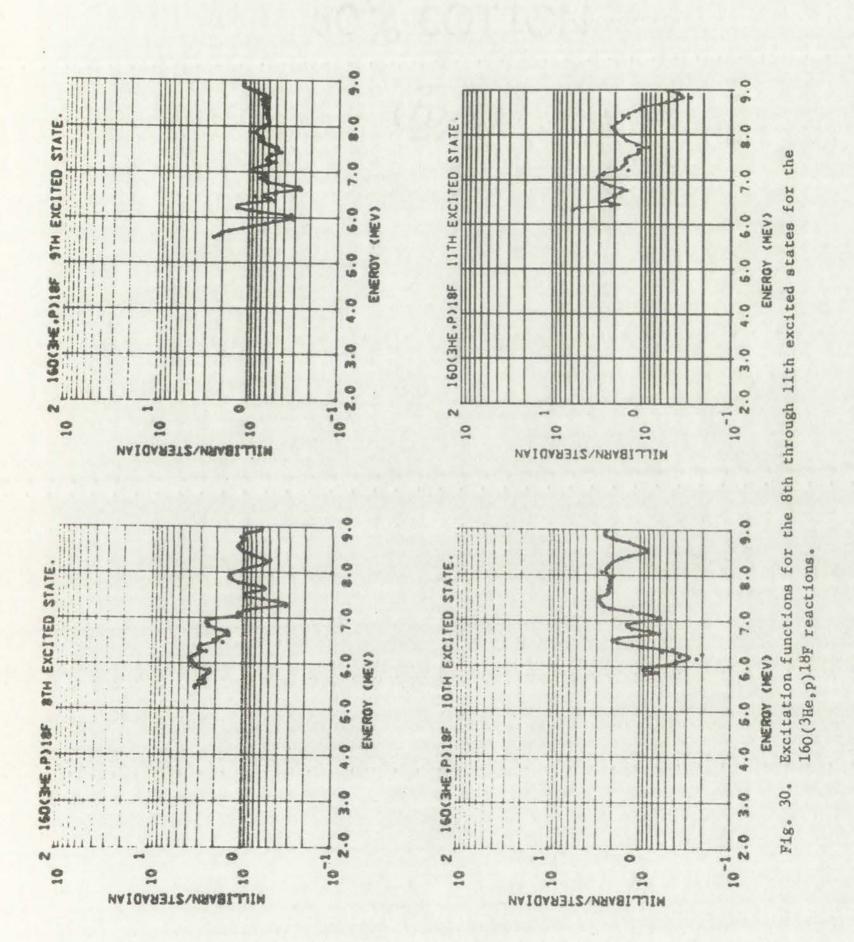


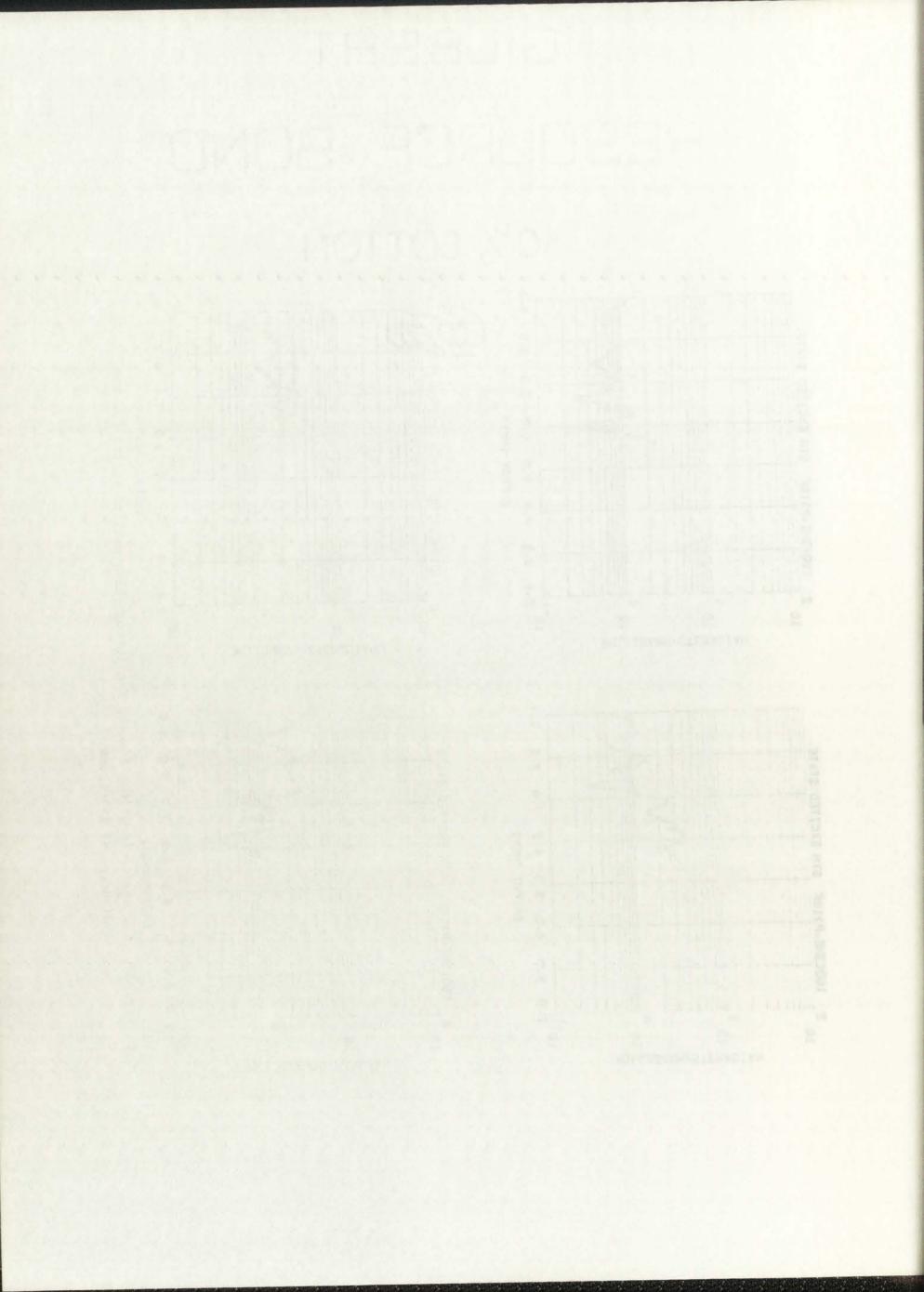


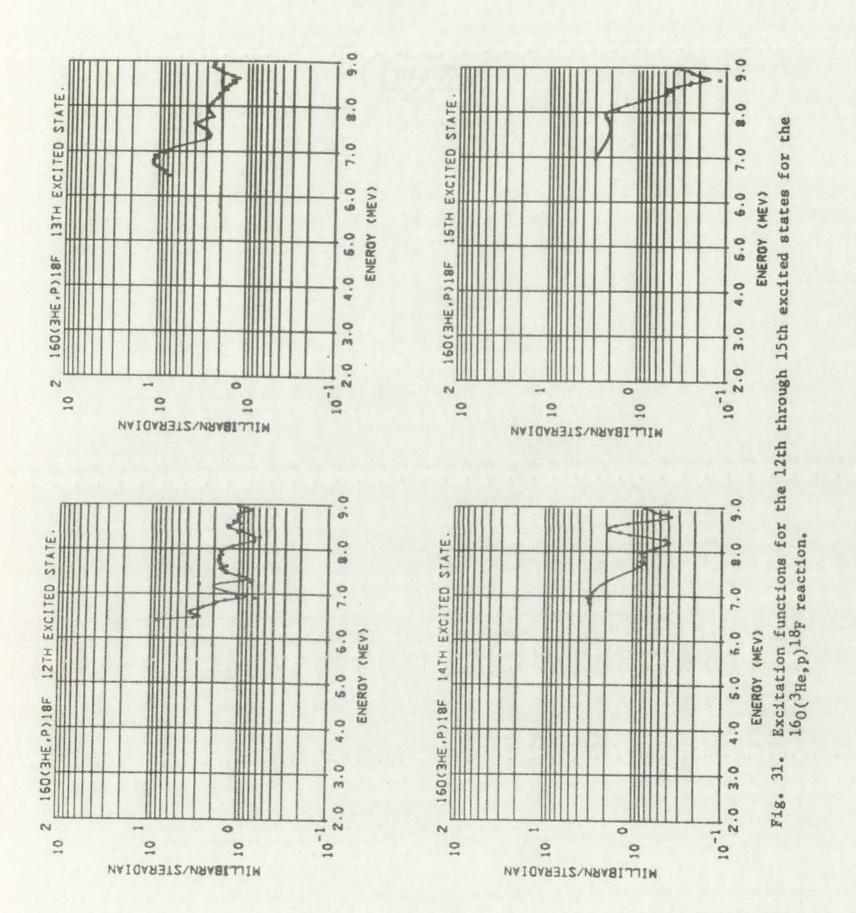


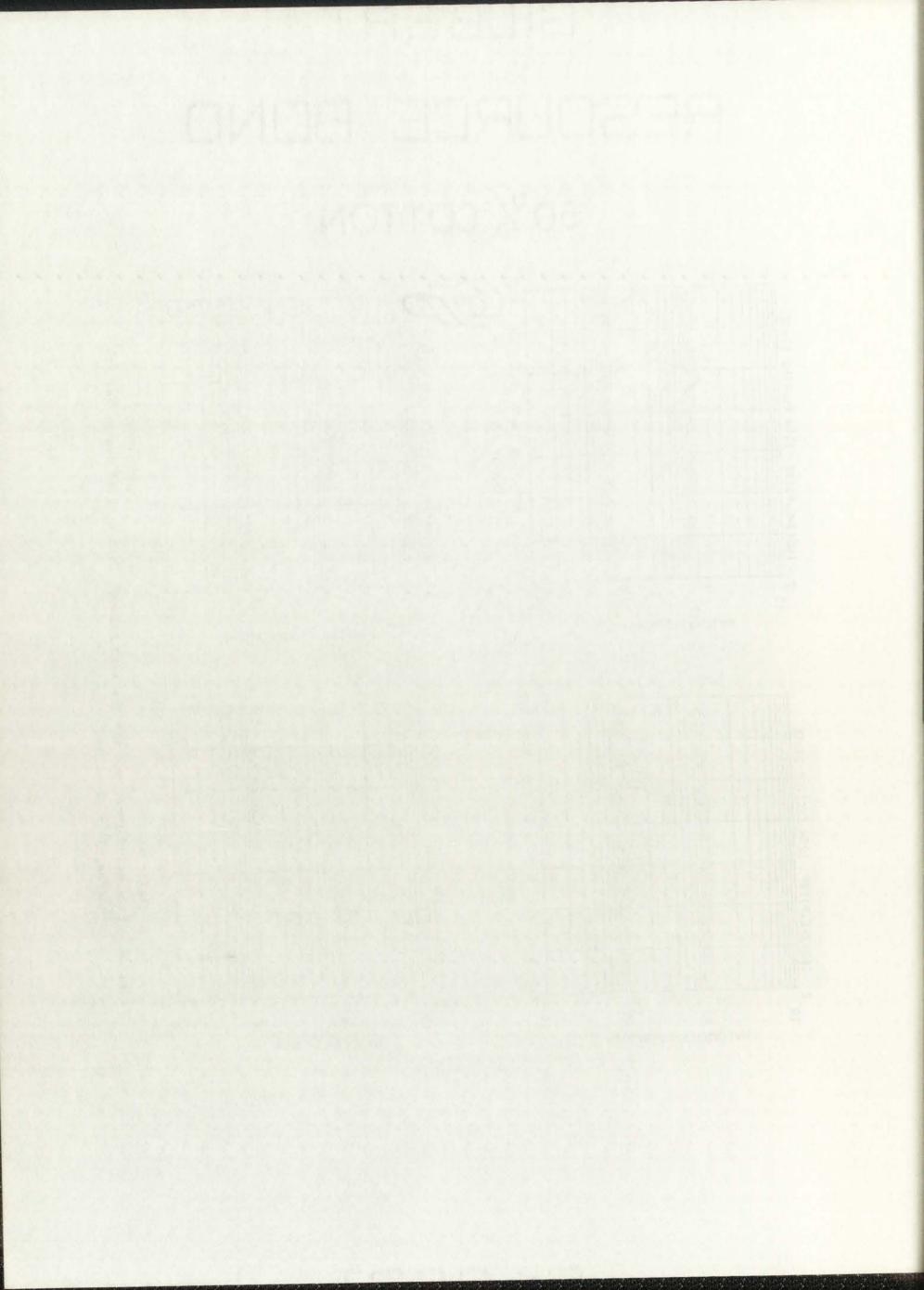


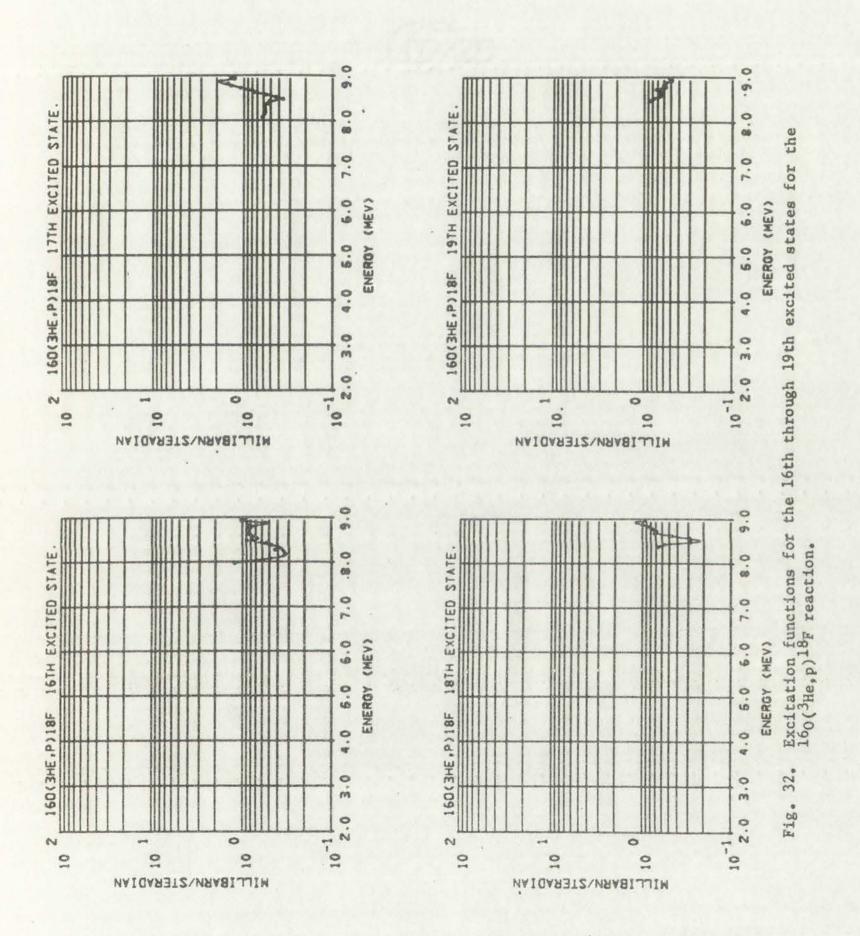


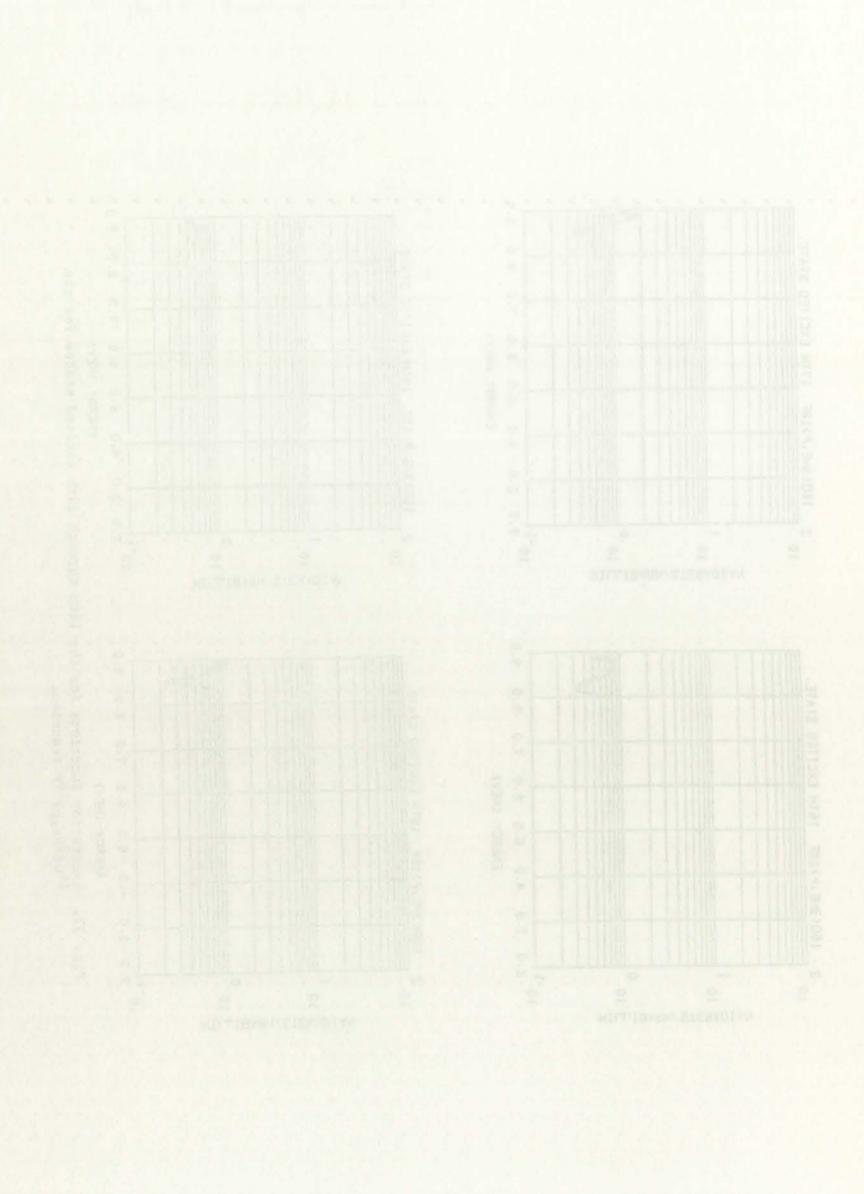












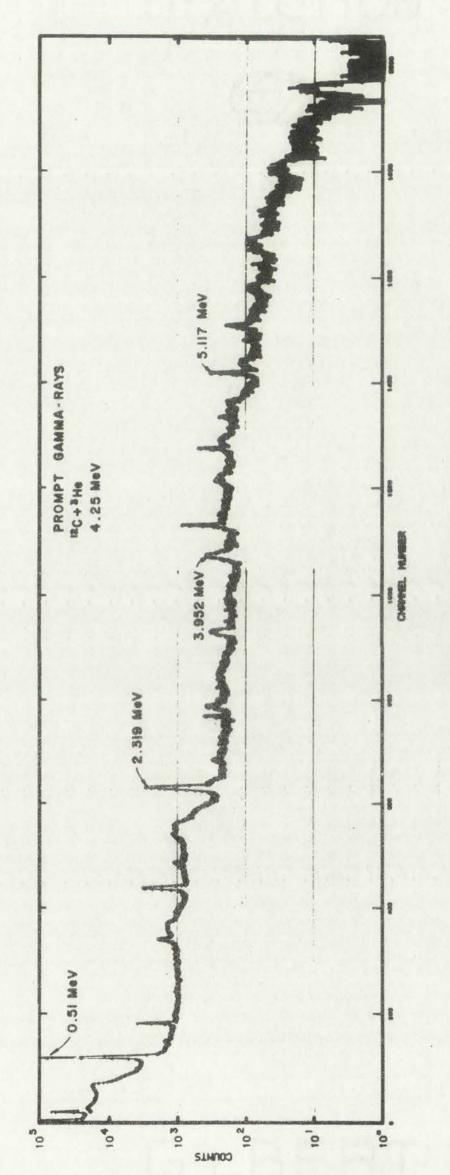
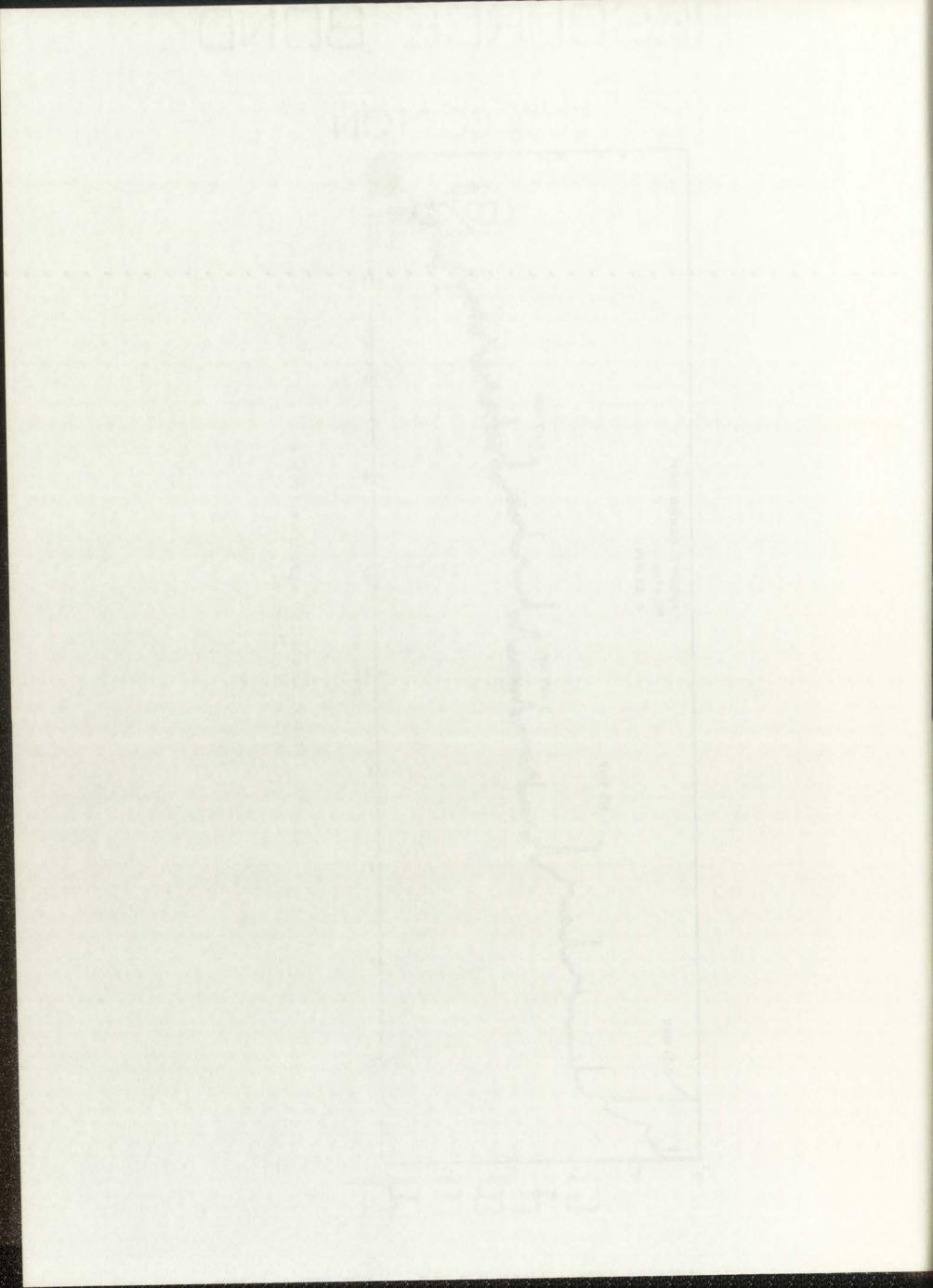


Fig. 33. Prompt gamma-ray spectrum from a carbon irradiation.



and in Fig. 34 for an oxygen irradiation. The resolution of the detector system (normally 5.0 keV FWHM for 1.33 MeV gamma rays) is degraded some by the high count rate. The full-energy peak intrinsic efficiency of the detector was 4.5% at 1.33 MeV. The total  $^3\text{He}^{++}$  charge for these data was  $4.0 \times 10^{-5}$  C.

Recent publications, Refs. 27 and 28, give values for these energy levels that are consistent, within the experimental limits, with the proton spectra and also with the prompt gamma-ray data obtained in this experiment. The energy levels used in the unfolding of the proton spectra are listed in Table 4.

TABLE 4

NUCLEAR LEVELS IN 14N AND 18F

14 <sub>N Levels</sub> (MeV)	18 <sub>F</sub> Levels <sup>b</sup> (MeV)
0.0	0.0
2.319	0.937
3.952	1.043
4.927	1.081
5.117	1.131
5.713	1.701
5.885	2.101
6.224	2.524
6.468	3.060
7.036	3.134
	3.358
	3.724
	3.790
	3.839
	4.115
	4.231
	4.361
	4.400
	4.651
	4.741

aRef. 27 bRef. 28

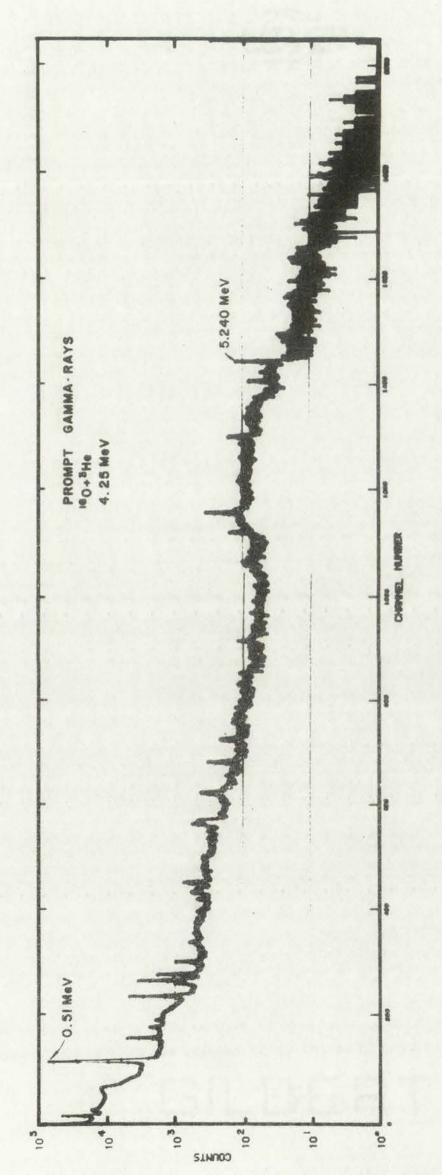
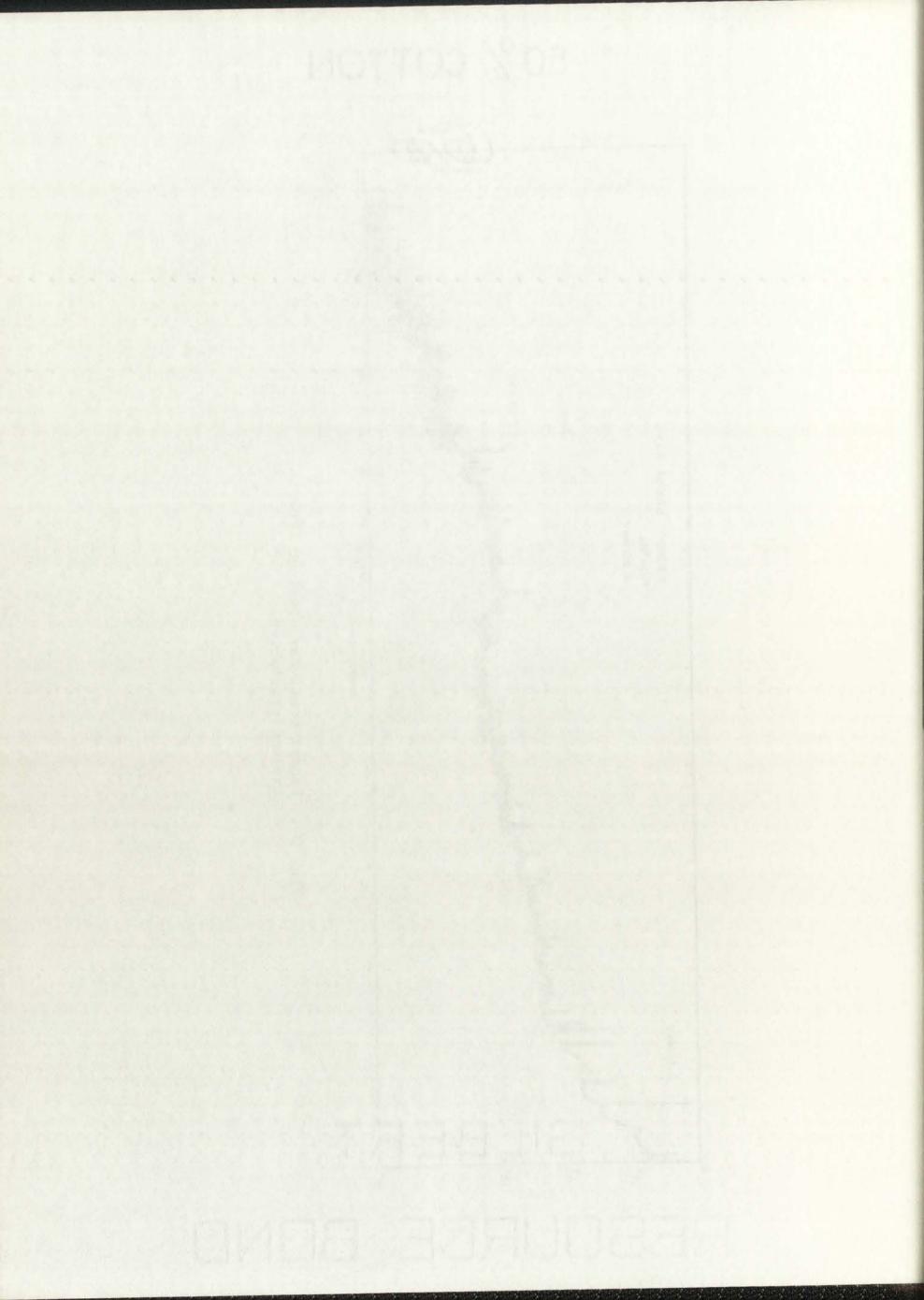


Fig. 34. Prompt gamma-ray spectrum from an oxygen irradiation.



### Interpolation and Smoothing with Cubic Splines

Cubic splines have been used to interpolate and also to smooth the experimental data. A derivation of the cubic spline function, as it was used in the codes presented in this paper, is given in Appendix E. A more detailed presentation can be found in several books that are published on the subject (e.g., Ref. 29). The cubic spline functions were used to analytically represent the energy of the charged particles versus depth of material penetrated, E = F(x), and the inverse of this function, x = f(E). These functions were used extensively to determine the charged-particle energy losses and the depth of material penetrated for a given reaction energy.

Interpolatory cubic splines in smoothing experimental data, e.g., to calculate a smooth line through a set of data containing statistical fluctuations, have been quite useful. The data is smoothed by interpolating a value  $(y_i^e)$  using an odd number of data points. The smoothed data point becomes

$$y_{i,j}^e = 2/3 y_{i,j-1}^e + 1/3 y_{i,j}^e$$
,

where the superscript refers to the smoothed data, the i subscript refers to the ith data point, and the j subscript refers to the number of times the data point has been smoothed. The smoothed function and the original data are shown in Fig. 35 for a small region of a 4096-channel gamma-ray spectrum. The data were smoothed ten times to give the smoothed function. This type of data smoothing is quite stable even with very poor statistics, does not produce the oscillations common in smoothing done with high-order polynomials, and does not smooth away small satellite peaks.

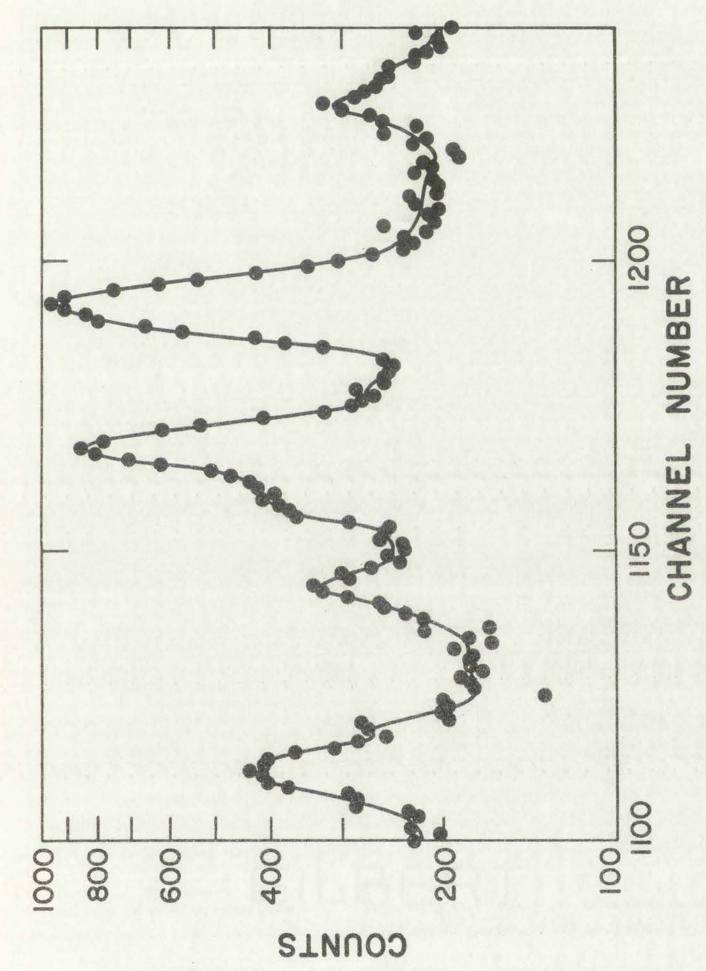
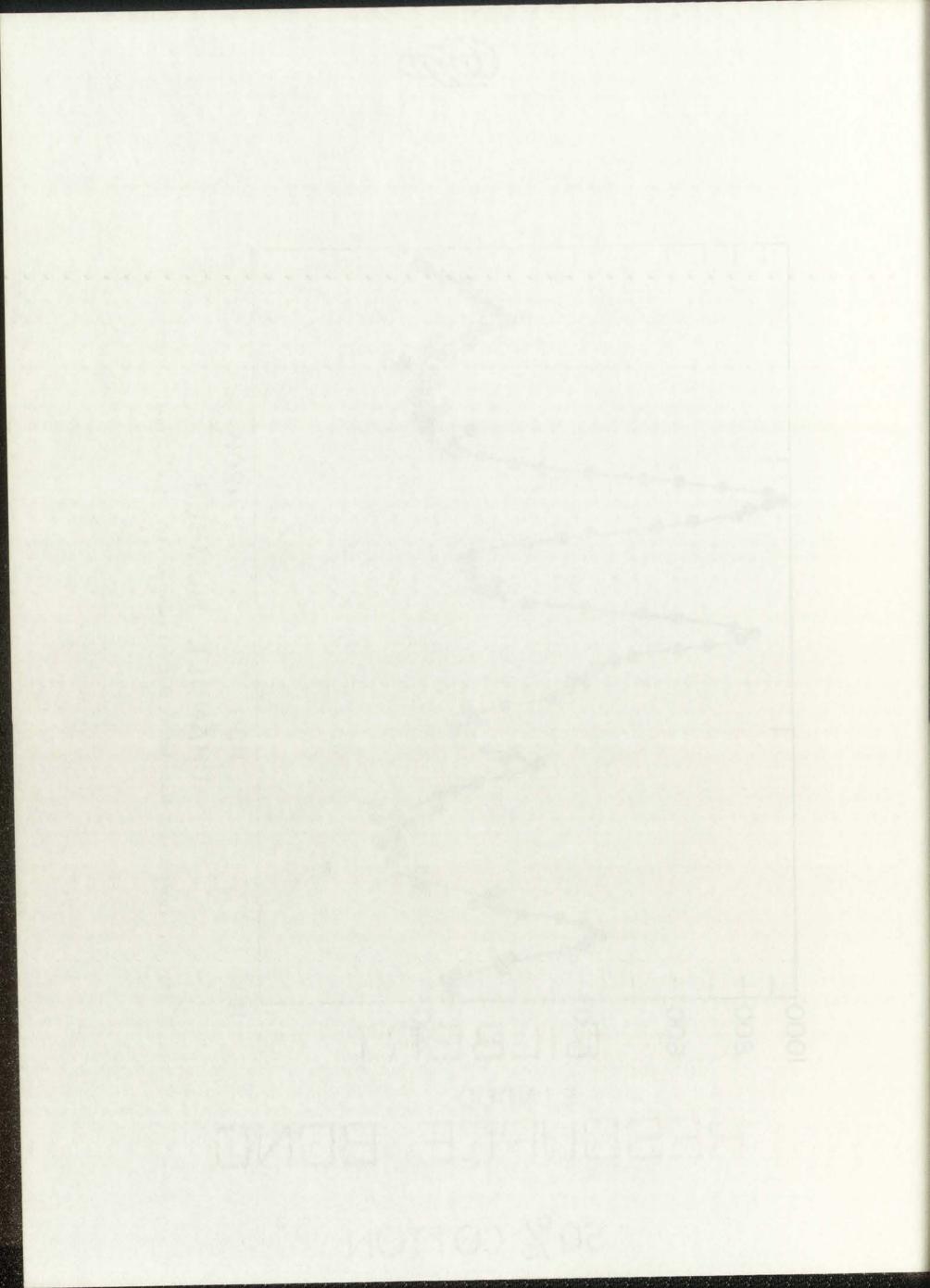


Fig. 35. Pulse-height distribution that was smoothed with cubic splines.



The excitation function data presented in Figs. 25 through 32 were smoothed using these techniques. These data were smoothed three times using seven data points. These smoothed spline functions were used to represent the excitation functions in the computer calculations of the impurity distributions in the thick targets.

### Nuclear Reaction Kinematics

The reaction kinematics are shown schematically in Fig. 36.  $M_1$  refers to the incident particle mass, which, for this experiment, was that of  $^3\text{He}$ ;  $M_2$  refers to the target mass, which, for this experiment, was that of either carbon or oxygen;  $M_3$  refers to the light reaction product, which, for this experiment, was a proton; and  $M_4$  refers to the heavy reaction product. Psi is the laboratory angle, and  $\theta$  is the center-of-mass angle of the light product.

The kinematics equations needed to calculate the energy of the reaction protons as a function of angle and <sup>3</sup>He energy are those of Jarmie and Seagrave given in Ref. 30. The expression used to calculate the proton energy was

$$E_3 = E_1 \cdot B[\cos \Psi + (D/B - \sin^2 \Psi)^{\frac{1}{2}}]^2$$
,

where

$$B = \frac{M_1 M_3 (E_1 / E_t)}{(M_1 + M_2) (M_3 + M_4)},$$

$$D = \frac{M_2 M_4}{(M_1 + M_2) (M_3 + M_4)} \left(1 + \frac{M_1 Q}{M_2 E_*}\right),$$

 $\Psi$  = laboratory angle of the light product,

 $E_3 = proton energy,$ 

 $E_1 = {}^{3}He \text{ energy,}$ 

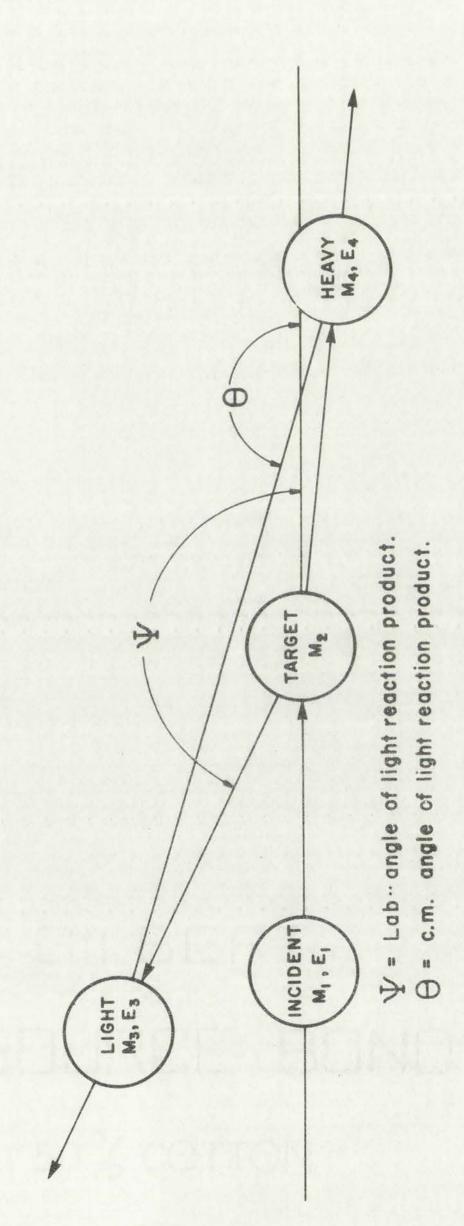
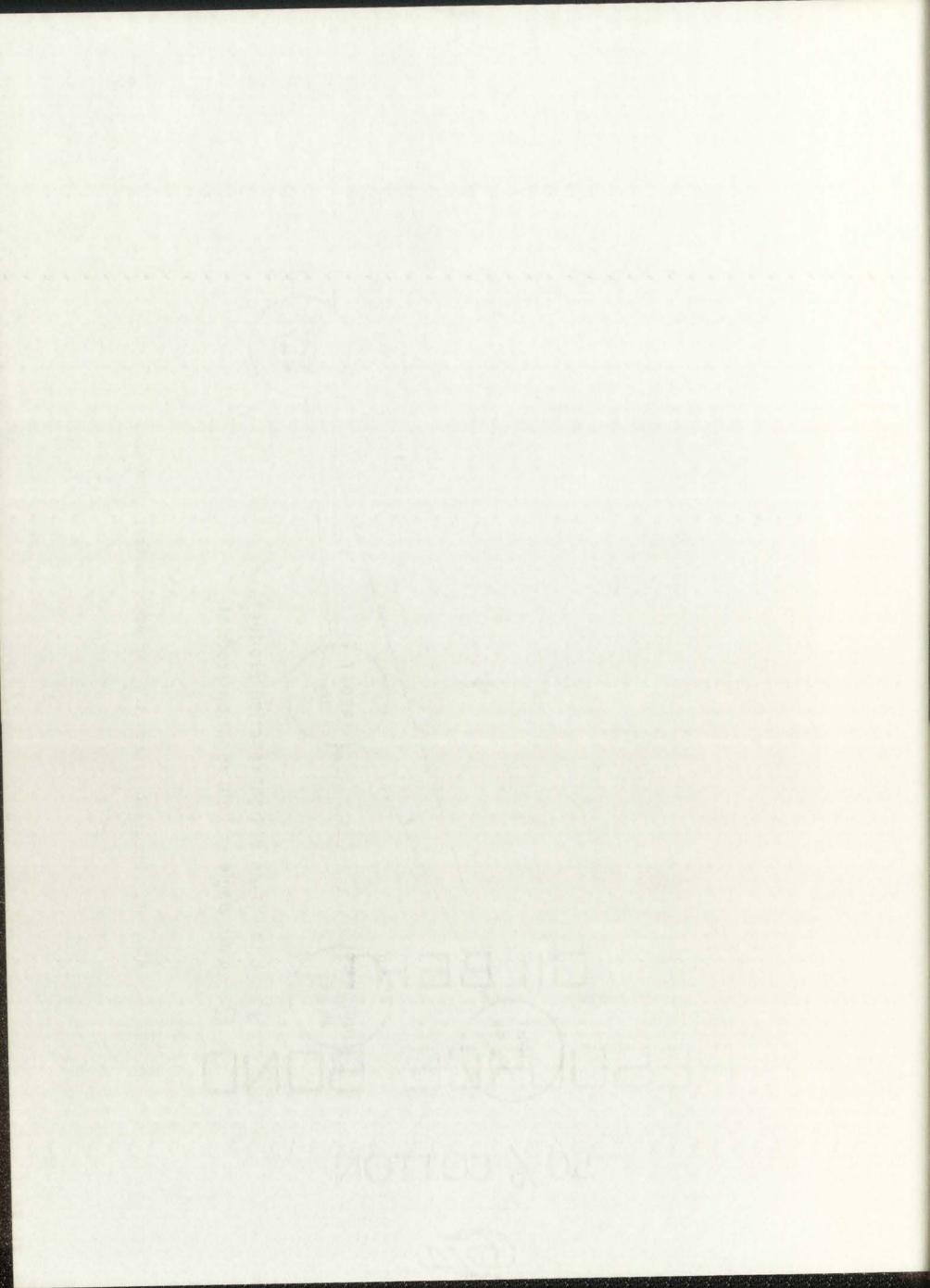


Fig. 36. Reaction kinematics for experimental geometry.



$$Q = Q_{gs} - E_{\gamma}$$
 $Q_{gs} = ground-state Q = 4.7786 MeV for carbon$ 
 $= 2.0334 MeV for oxygen,$ 

$$E_{\gamma}$$
 = prompt gamma-ray energy, and

$$E_{+} = E_{1} + Q.$$

Another expression from Ref. 30,

$$Q = \frac{M_3 + M_4}{M_4} E_3 - \frac{M_4 - M_1}{M_4} E_1 - \frac{2(M_1 M_3 E_1 E_3)^{\frac{1}{2}}}{M_4} \cos \Psi ,$$

was used to calculate the prompt gamma-ray energies from the iterated proton energies in the C24HE3P code, Appendix D.

It is helpful in understanding the kinematics of these reactions to be able to visualize the proton energies for the various states as a function of the incident  $^3$ He energy. These data are shown in Fig. 37 for several states of the  $^{12}\text{C}(^3\text{He,p})^{14}\text{N}$  reaction. Similar data are shown for the  $^{16}\text{O}(^3\text{He,p})^{18}\text{F}$  reaction in Fig. 38. These kinetmatics data coupled with the excitation function data and the stopping-power data were used to calculate the thick target response of the proton detector for various geometries.

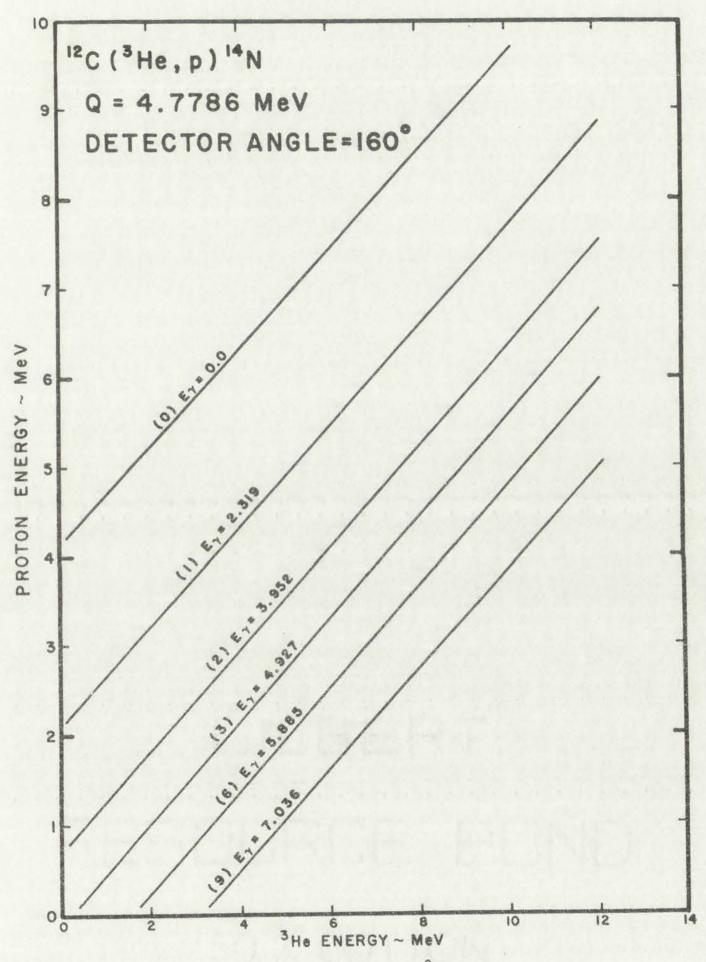
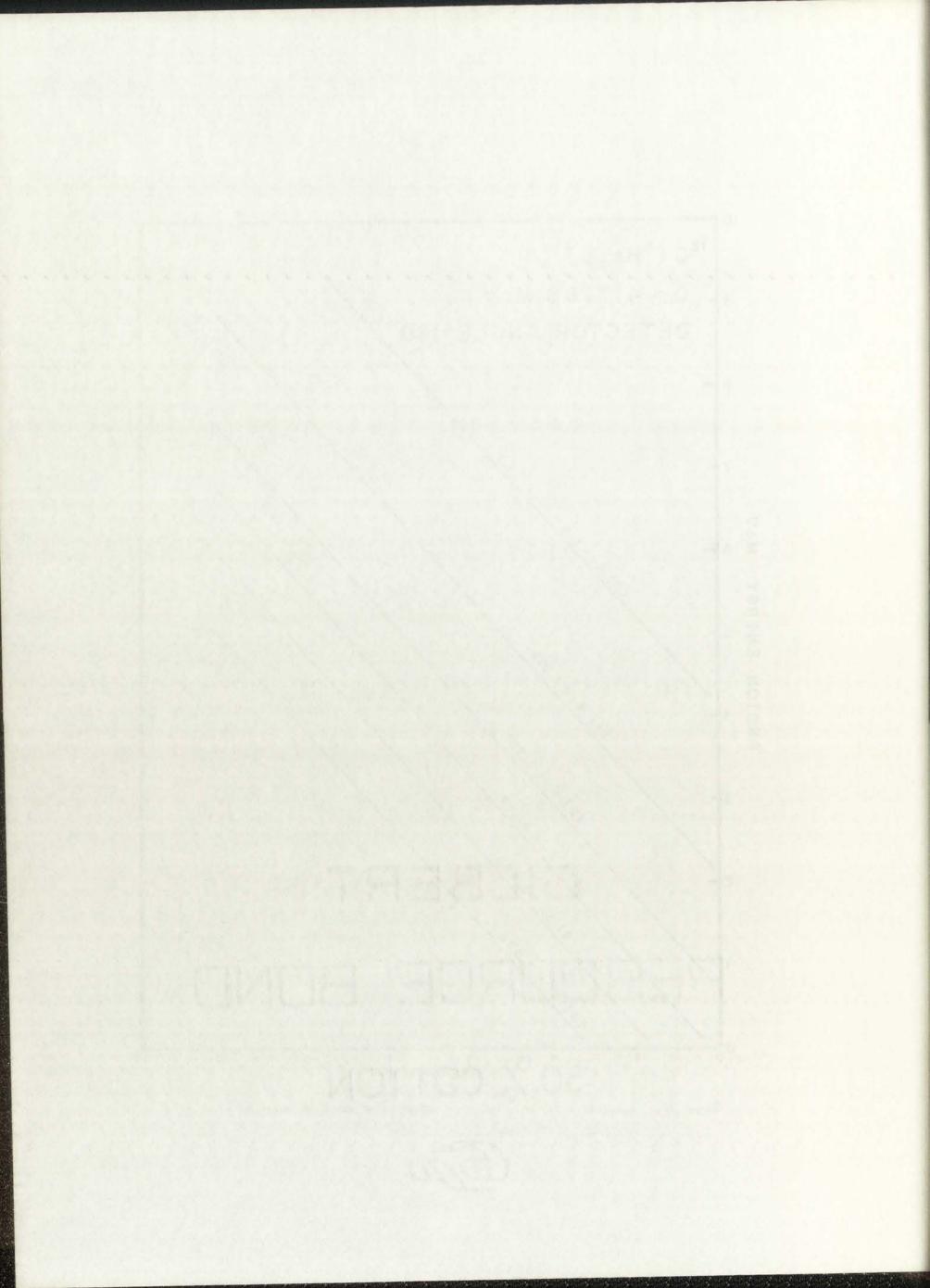


Fig. 37. Reaction proton energy versus  $^3{\rm He}$  energy for the  $^{12}{\rm C}(^3{\rm He},p)^{14}{\rm N}$  reaction at  $^{160}{\rm e}$ .



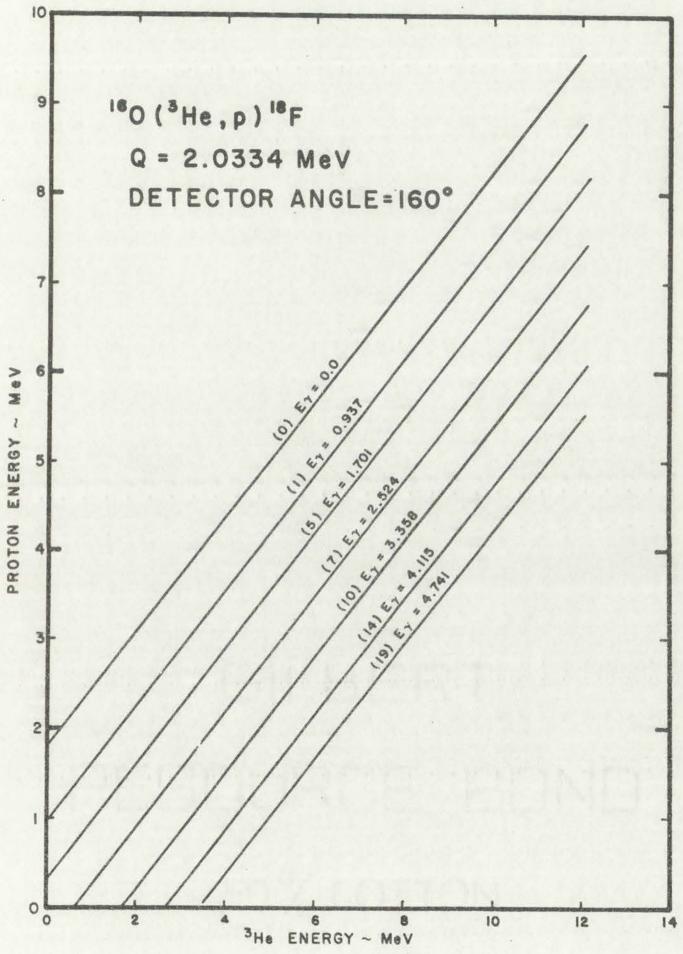
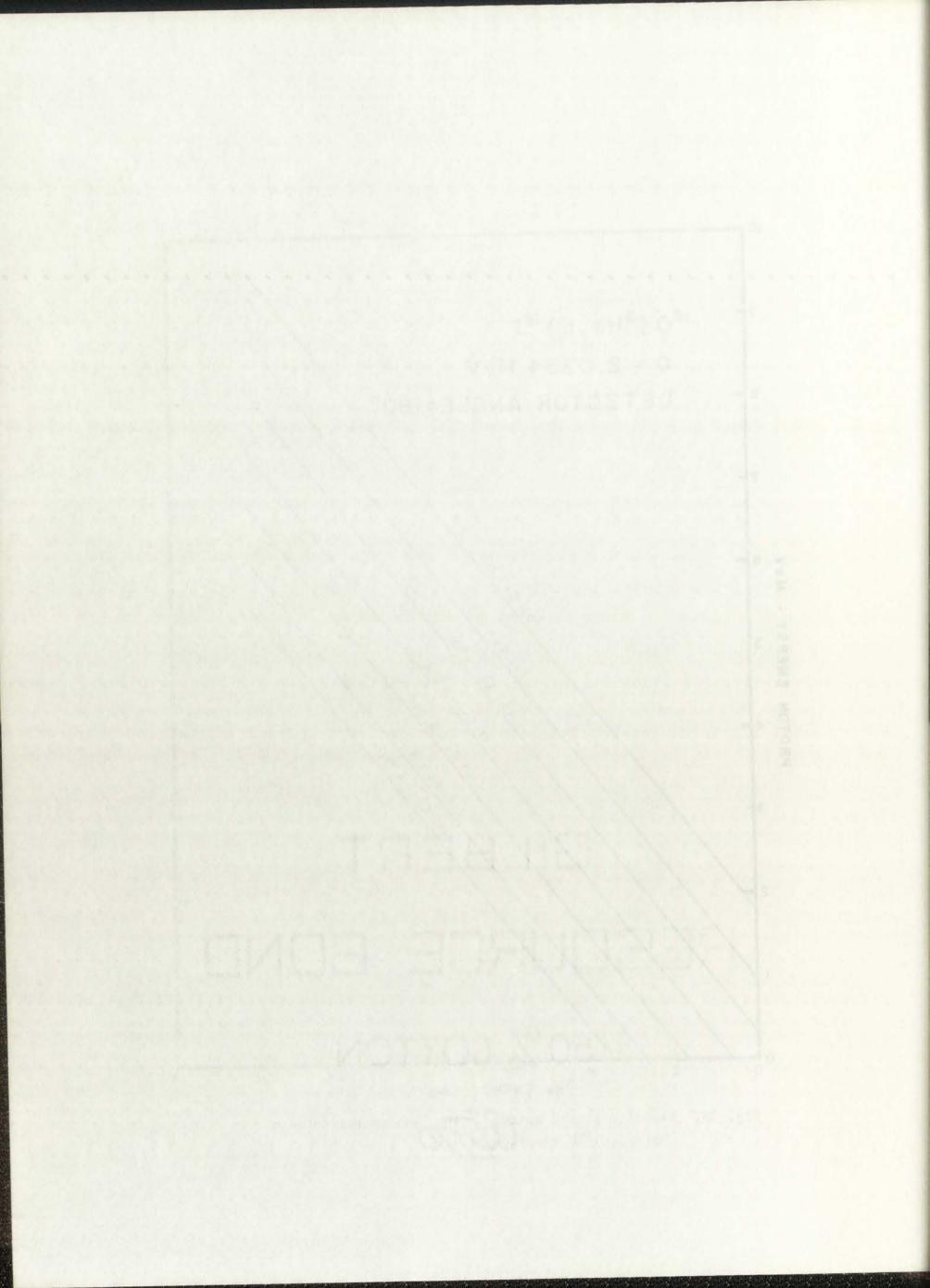


Fig. 38. Reaction proton energy versus  $^3{\rm He}$  energy for the  $^{16}{\rm O}(^3{\rm He},p)^{18}{\rm F}$  reaction at  $160^{\circ}$ .



### CHAPTER V

### CHANNELING

### Introduction

The concept of channeling dates back to 1912 when Johannes Stark contemplated the existence of open channels in crystalline materials and their possible effects on hydrogen ion bombardments. However, the experimental techniques of his day were not adequate to demonstrate channeling phenomena. It was not until 1963, after work on computer analyses of trajectories of energetic atoms in single crystals was published (Ref. 31), that there has been renewed interest in channeling phenomena. Since then, the theoretical and experimental studies on channeling have been extensive (Refs. 32 through 38).

Channeling can occur in either polycrystalline or single-crystal materials when the velocity of the particles is in a direction that is nearly parallel to one of the major crystal axes or planes. Repulsive coulomb forces can gently steer the particles between the rows or planes of nuclei and channeling effects become quite large. The channeled particles travel through regions of lower electron densities, and there are fewer ionizing collisions causing an increase in the particle range. This increase in the particle range can be quite significant for heavy ions. (Ref. 9) and is only about a factor of two for the lighter ions. The number of hard collisions and encounters that occur near the nuclei, such as large angle Rutherford scatter and nuclear reactions, are decreased for channeling trajectories. However, there is a transition region between the channeling trajectories and the nonchanneling

trajectories where the crystal nuclei are able to steer the incident particles so that the number of hard collisions and encounters that occur near the nuclei are increased. The particle trajectories for these three orientations are shown schematically in Fig. 39.

It is important that the experimentalist be aware of these phenomena if he is doing activation analyses of polycrystalline or single-crystal materials. For channeling orientations, the effective range of the incident particles is increased, and the activation of randomly located interstitial impurities will be increased. Similarly, if the impurities are substitutional, the number of activations will decrease if the sample is bombarded in a channeling direction. This decrease will be somewhat larger than the increase expected for interstitial impurities.

If the interstitial impurities are located in a unique location in the crystalline structure, bombardment in a direction parallel with one crystal axis might cause an increase in the number of activations, while bombardment in a direction parallel to another crystal axis might cause a decrease in the number of activations relative to a bombardment in a nonchanneling orientation. One of the objectives of this experiment was to irradiate crystalline materials in channeling and nonchanneling orientations with <sup>3</sup>He ions to determine the locations and amounts of carbon and oxygen impurities.

## Channeling Experiments with Single-Crystal Thoria

Channeling data were obtained from single-crystal thoria samples. Preparation of the single-crystal thoria samples is given in Ref. 39. These thoria channeling data show both the backscatter channeling effects discussed in Chapter II and also the effect that channeling has on the reaction protons from the  $^{16}$ O( $^{3}$ He,p) $^{18}$ F reaction. The high-energy

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# ION PATHS IN AN ORDERED LATTICE

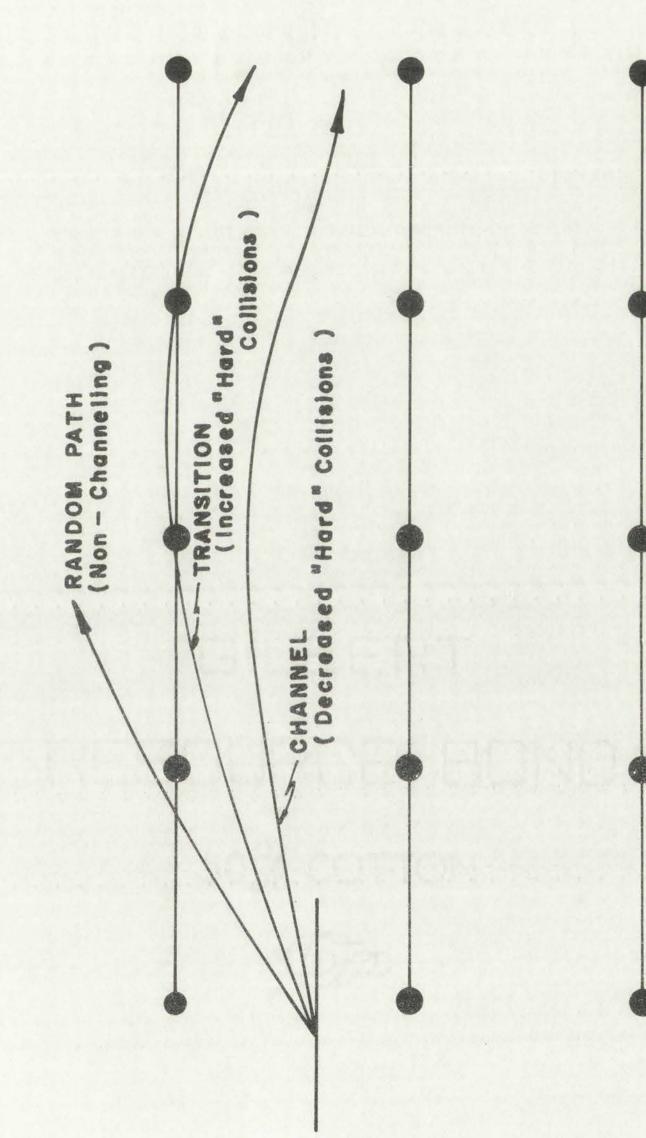


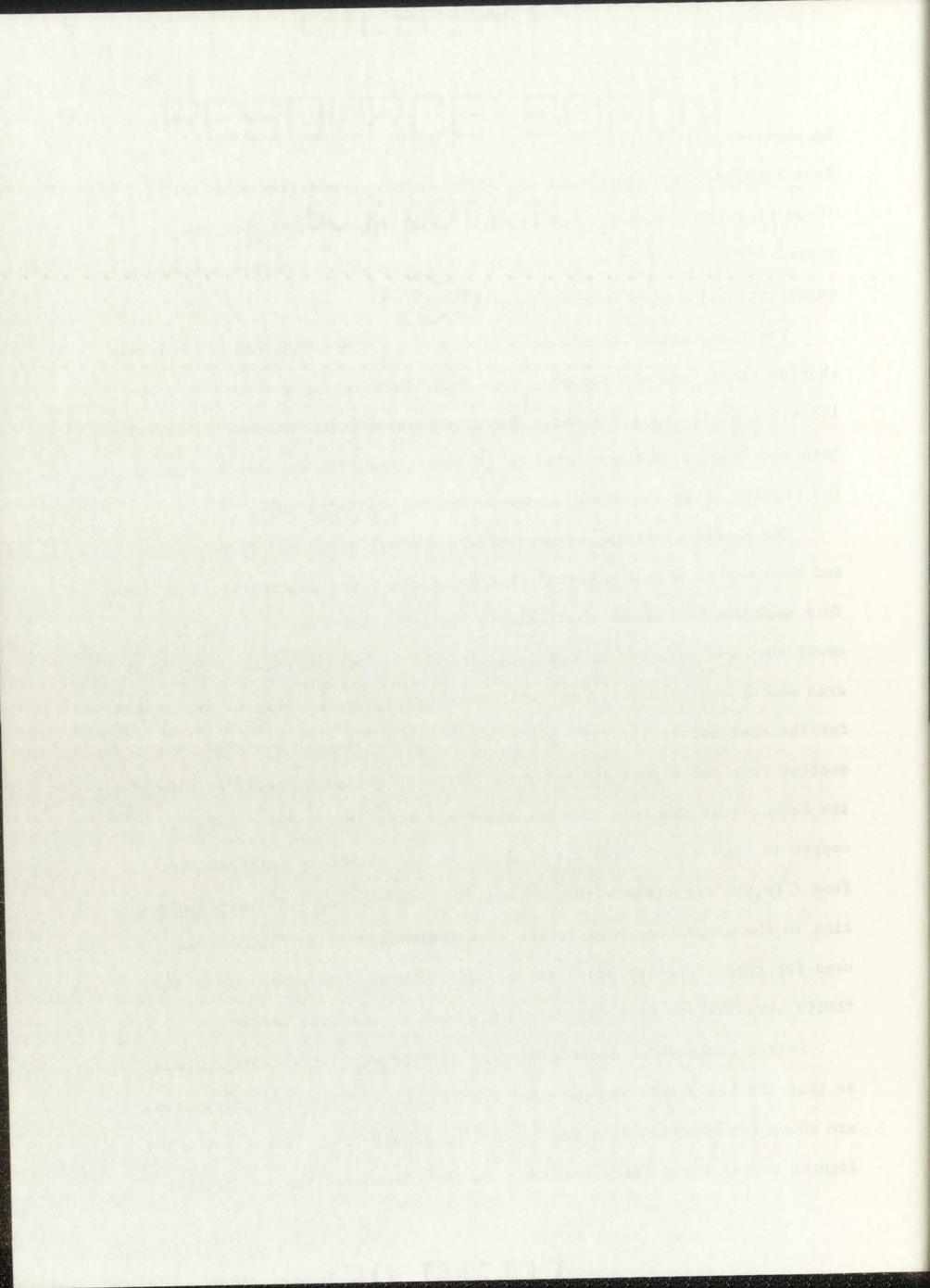
Fig. 39. Ion paths in an ordered lattice.

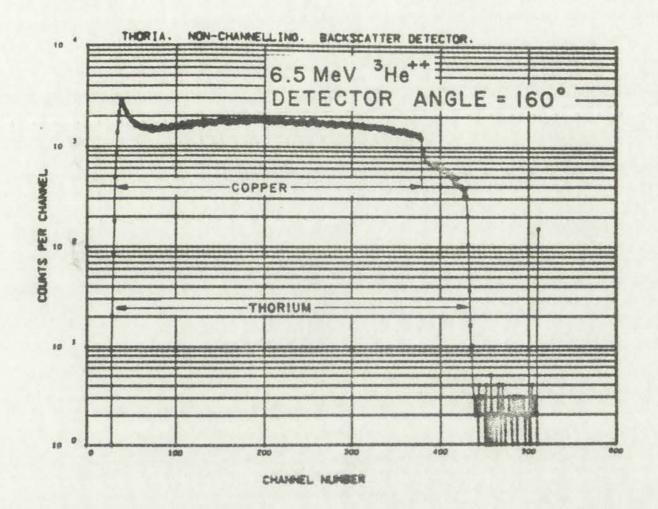
backscatter data is from the thorium atoms, and the reaction protons are from interactions with the oxygen atoms in the crystalline material. These reaction proton data show quite clearly the results that are expected from the oriented bombardments of a crystalline matrix containing substitutional oxygen impurity atoms.

The backscatter techniques can be used to study the locations of the thorium atoms, and the prompt proton techniques can be used to study the locations of the oxygen atoms. These techniques could be used to investigate the defects in the crystal or to investigate the displaced atoms in the crystal after radiation damage to the crystal structure.

The thoria crystals, because of their small size, had to be mounted and then masked with a material that would not cause interfering reactions. This mask was to prevent the incident <sup>3</sup>He particles from striking the epoxy that was used for mounting the crystal on the goniometer. The mask area was approximately 1.2 mm<sup>2</sup> and triangular in shape. Copper was chosen for the mask material. Its atomic weight was low enough that the back-scatter from the copper did not interfere with the high-energy portion of the backscatter spectrum from the thorium. Also, the atomic number of copper is high enough that its coulomb barrier prevented interference from (<sup>3</sup>He,px) reactions with the copper. Interference from low-Z impurities in the copper was negligible. The goniometer target chamber was used for these irradiations. All of the spectral data presented on the thoria irradiations were for the same number of incident particles.

Normal backscatter techniques were used to align the thoria crystal so that the <111> axis was parallel with the beam. Backscatter spectra are shown for nonchanneling and channeling orientations in Fig. 40. The lighter copper atoms contribute only to the low-energy region of these





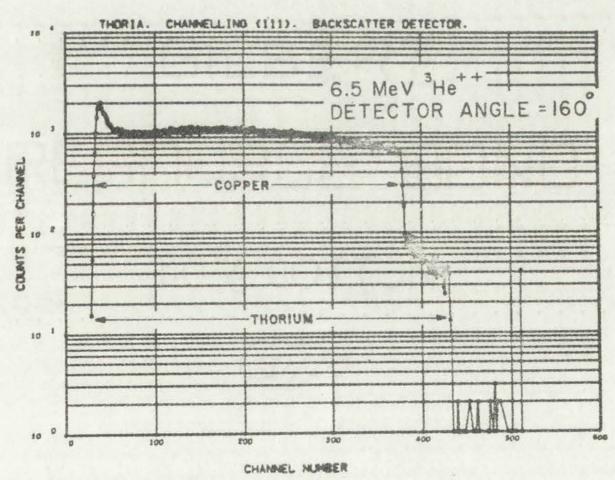
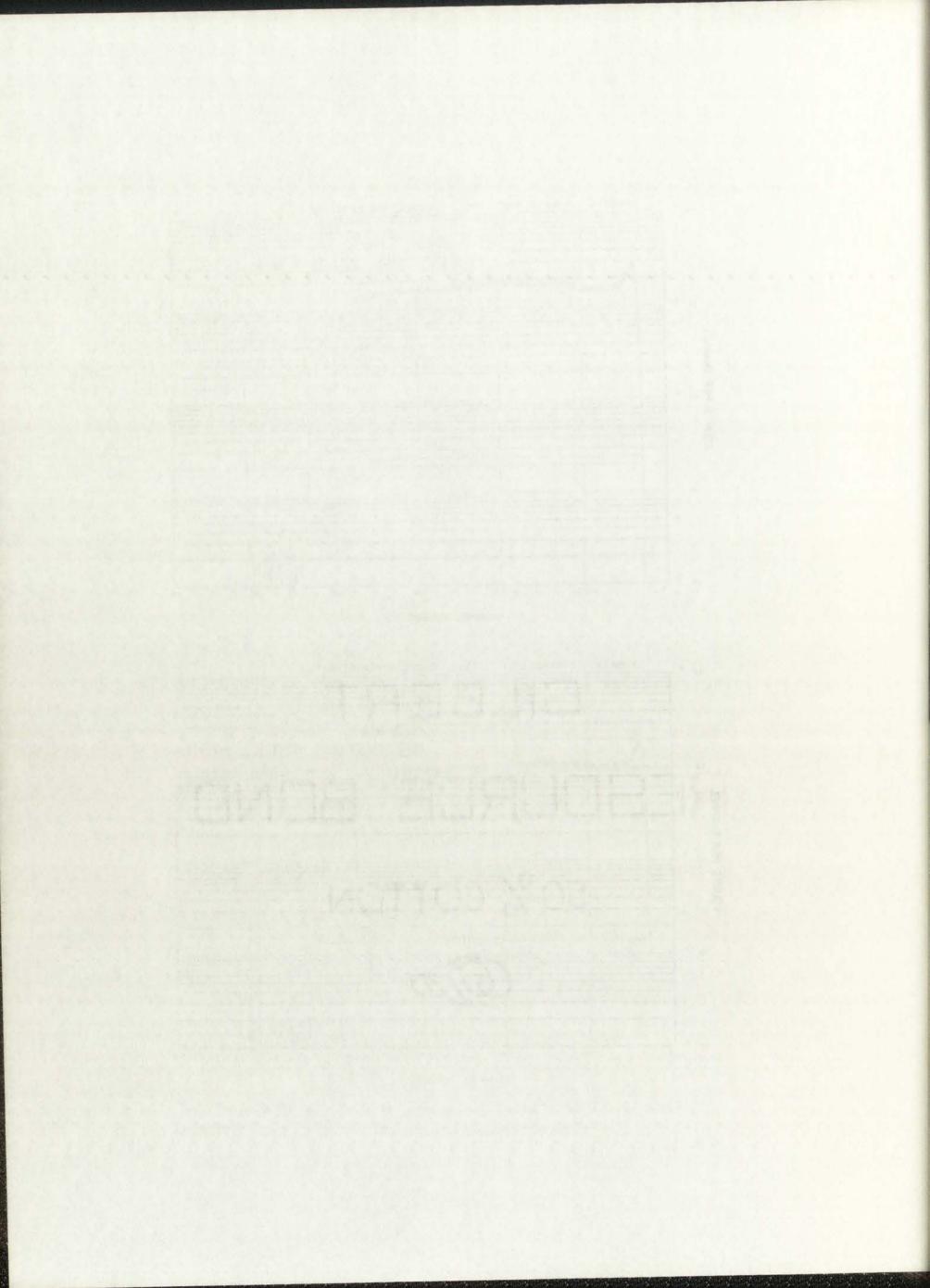


Fig. 40. Pulse-height distributions from <sup>3</sup>He particles backscattered by copper and oriented single-crystal thoria.



spectra, while the backscatter from the heavier thorium atoms extends to higher energies. The threshold of the counter that was used to record the backscatter data, from which the channeling orientation was determined, was adjusted so that only backscatters from the thorium atoms were counted. For the data presented in Fig. 40, the maximum backscatter energy from the copper atoms corresponds to channel 380, while the backscatter from the heavier thorium atoms extends up to about channel 430.

The backscatter data that were obtained as the upper arc of the goniometer was rotated across the <111> axis are shown in Fig. 41. The critical angle for channeling along the <111> axis of thoria is about 0.3° for 6.5 MeV <sup>3</sup>He particles. The location of the axis of rotation relative to the {110} planes of the crystal was not determined.

The critical angle is defined as the half-width at a level halfway between the normal and minimum yields. Usually only those encounters that take place near the surface are considered, so that complicating multiple scattering effects can be ignored. The critical angle for channeling is related to the crystal and particle parameters (Refs. 32 and 16).

$$\Psi_{\text{crit}} \propto \left(\frac{Z_1 Z_2}{d \cdot E}\right)^{\frac{1}{2}}$$
,

where

Z<sub>1</sub> is the atomic number of the incident particle,

 $Z_2$  is the average atomic number of the lattice atoms,

E is the particle energy, and

d is the lattice spacing.

The critical angle is also a function of the sample temperature.

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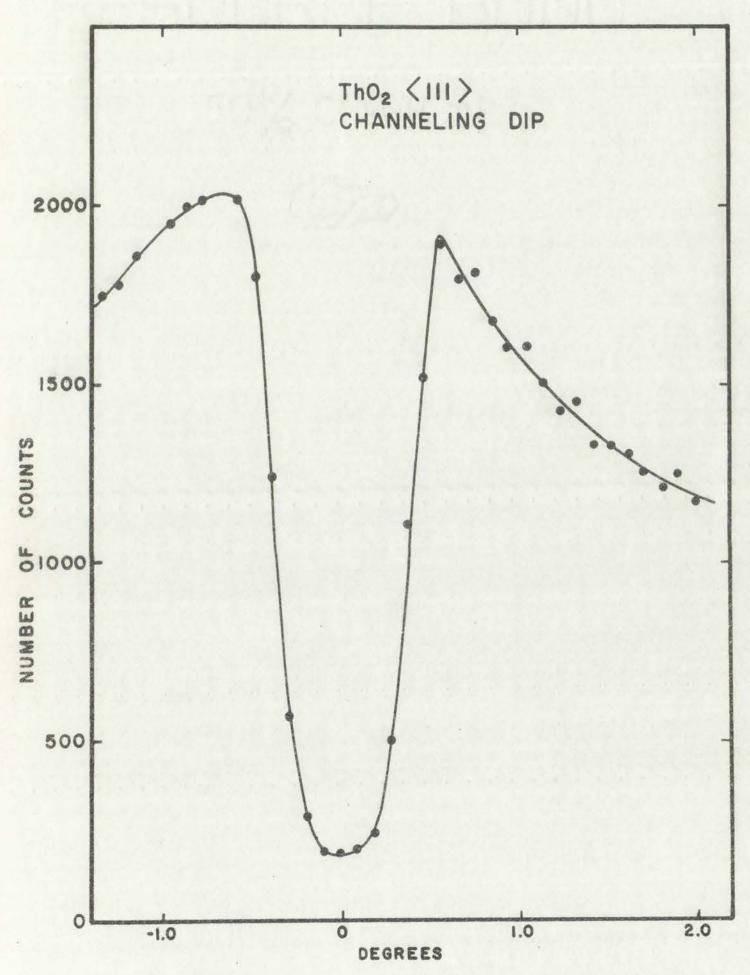
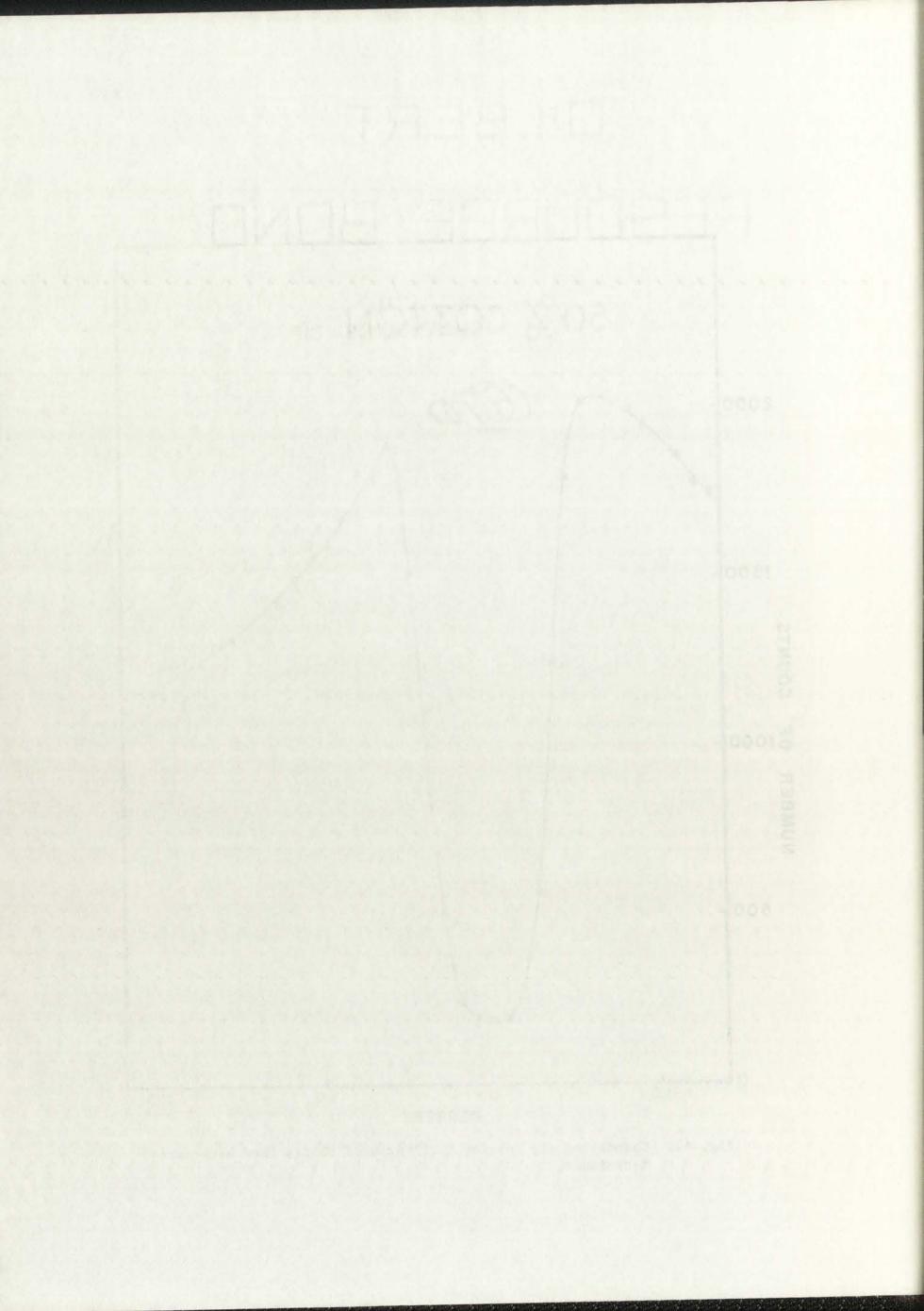


Fig. 41. Channeling dip for the <111> axis of thoria from backscatter techniques.



The dependence of the critical angle on the lattice spacing is not well understood. Picraux et al. (Ref. 16) have obtained experimental agreement with the theoretical dependence of  $\Psi_{\text{crit}}$  on the planar spacing only after correcting for the effects of surface transmission and surface oxide layers. They found that their theoretical predictions were consistently 20 to 25% larger than their experimental measurements.

The background that were present in these experiments are shown in Fig. 42. The upper plot shows the pulse-height distribution from the  $^3{\rm He}$  backscattered from the copper mask. The small background that is present in the region used to measure the thorium backscatter is from protons from carbon deposited on the mask by the beam. The background spectrum for the proton detector system is shown in the bottom plot. The absorber foil thickness was  $60.96~\mu$  aluminum.

The pulse-height distributions from the proton detector system are shown in Fig. 43 for three different crystal orientations. The top plot shows the distribution with the crystal oriented approximately 2° from the (111) channeling orientation. The spectrum is similar to that which might be obtained from a thick sample of amorphous oxygen.

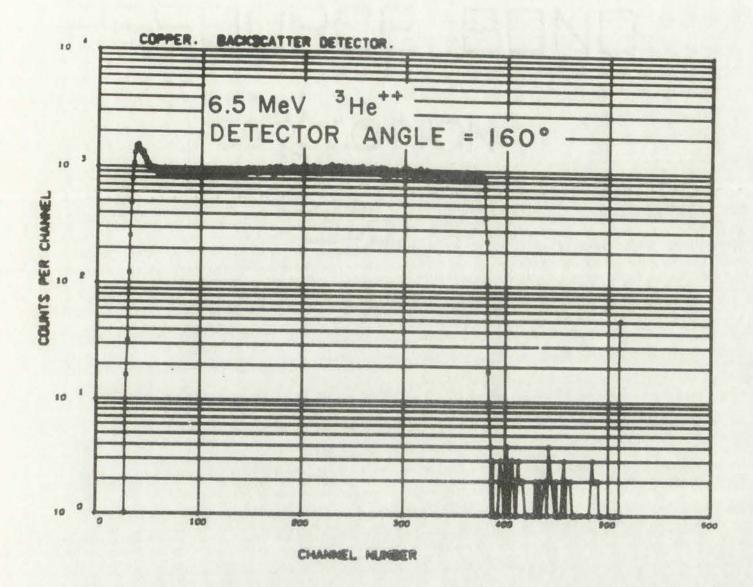
The middle plot (Fig. 43) shows the proton spectrum that was obtained with the sample oriented in the <111> direction. The lower count rate is from channeling of the <sup>3</sup>He particles between the rows of nuclei. These data show the effect that is expected for activation analyses for substitutional-type impurities in a crystalline matrix. For certain interstitial sites and crystal orientations, the count rate will also decrease. However, since these interstitial impurities are between two lattice planes, orientations which enhance their activation can be found.

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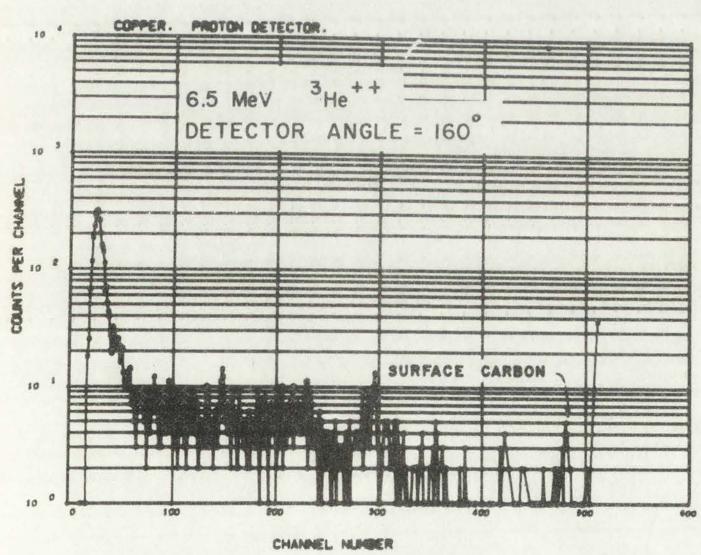
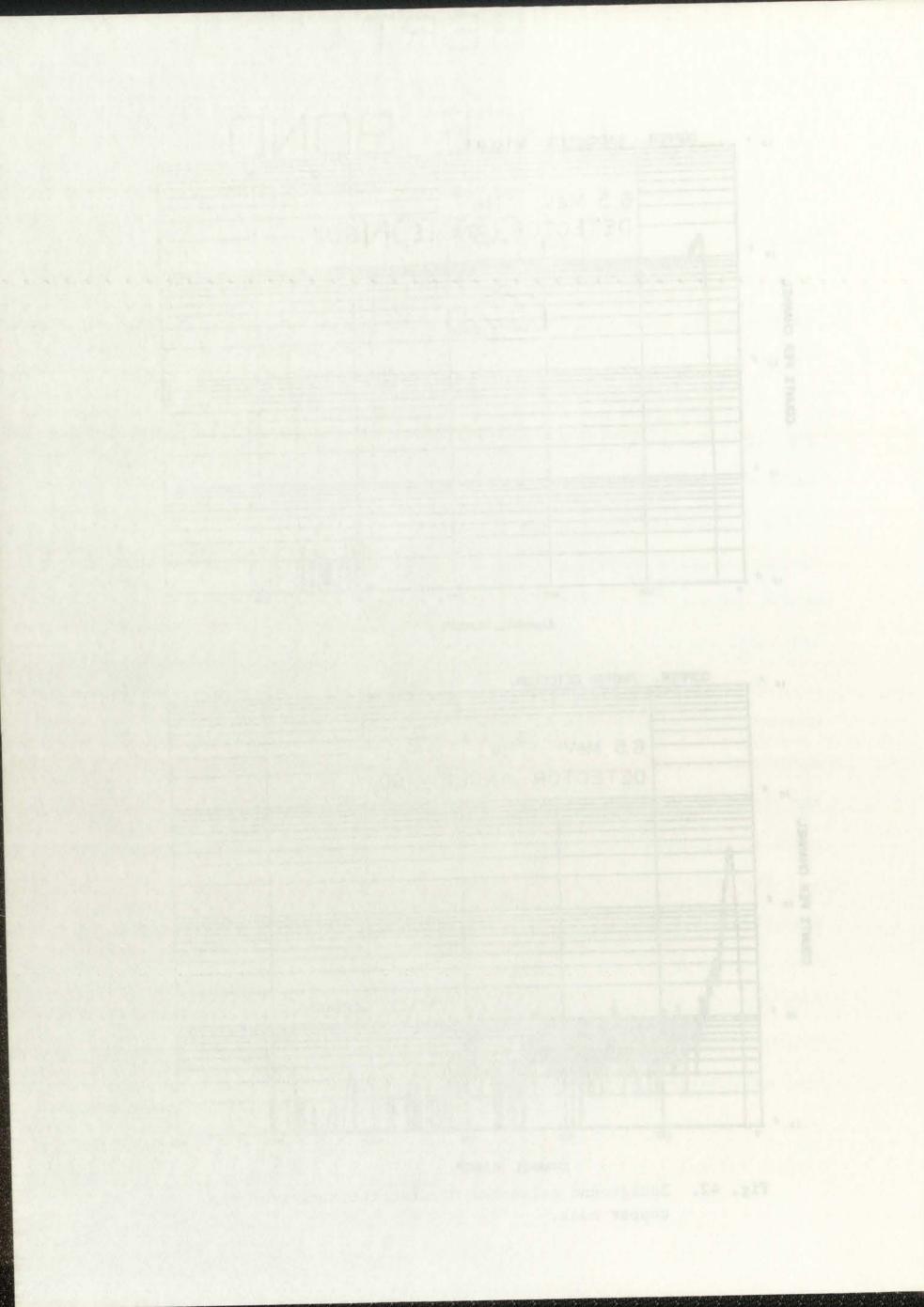


Fig. 42. Background pulse-height distributions from the copper mask.



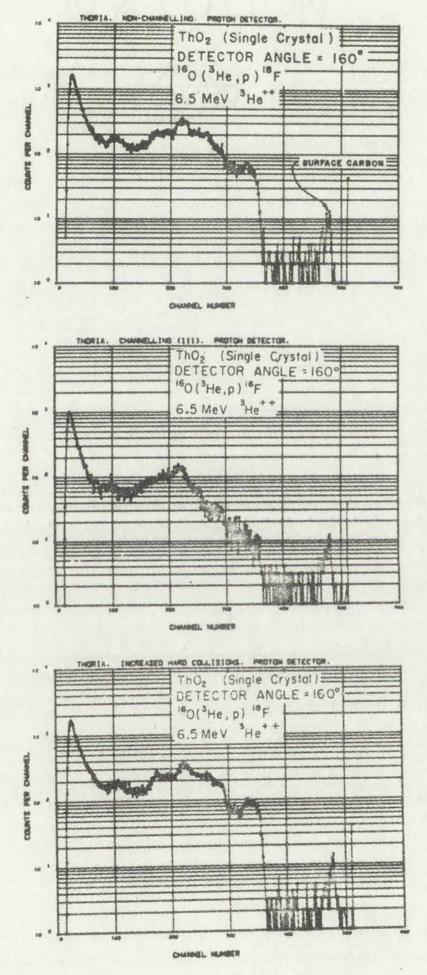
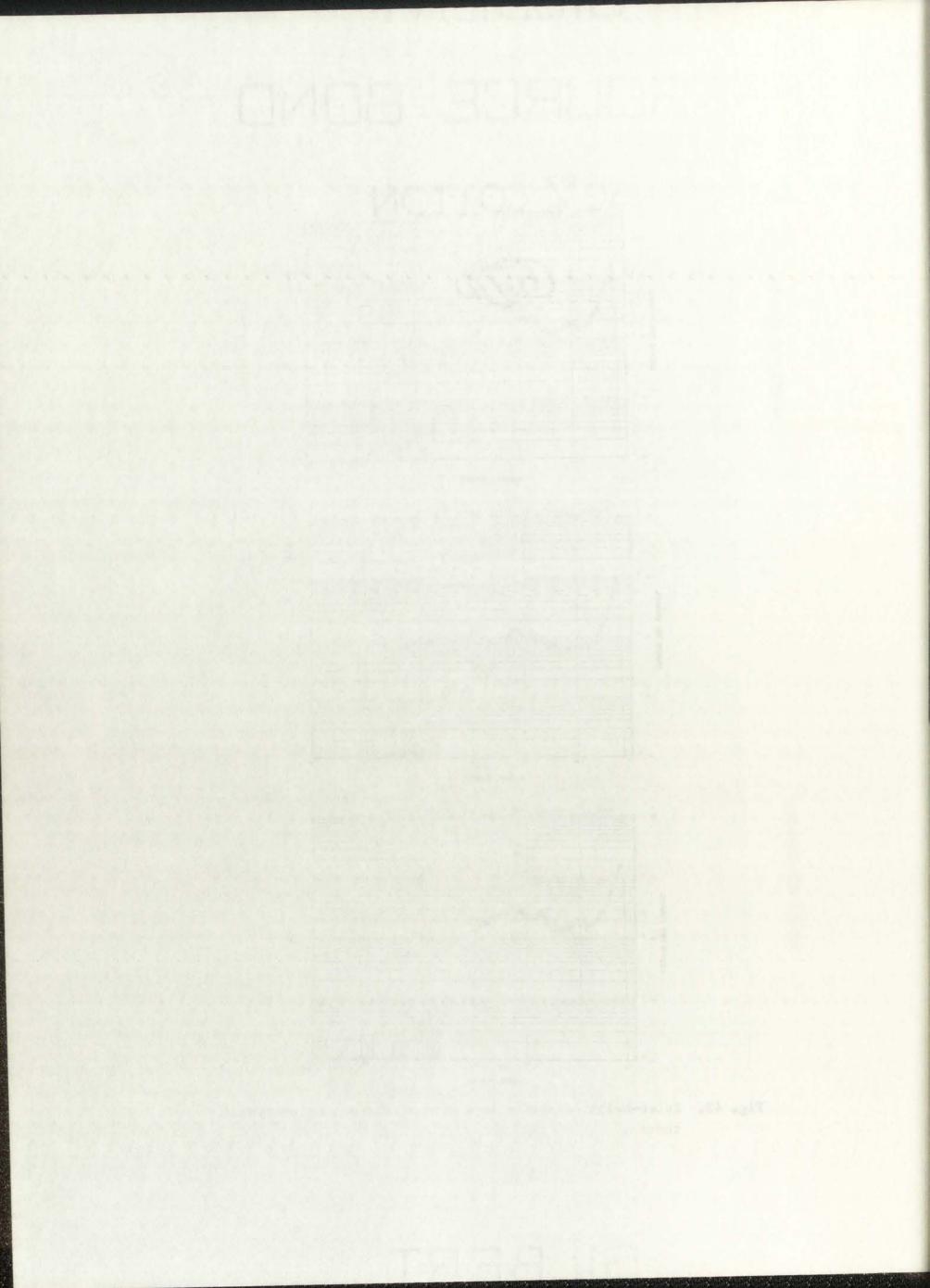


Fig. 43. Pulse-height distributions from oriented single-crystal thoria.



The pulse-height distribution that is obtained between the channeling and nonchanneling orientations is shown in the bottom plot (Fig. 43). The crystal was oriented 0.75° from the (111) axis for this irradiation.

3He ions incident at this angle are steered close to the rows of nuclei, causing an increased number of hard collisions.

#### CHAPTER VI

#### RESULTS

### Introduction

Analytical techniques were developed that utilized the thin target cross sections discussed in Chapter IV to unfold the complex proton spectra from the (<sup>3</sup>He,p) reactions. Channeling and nonchanneling irradiations were performed on thick carbon and oxygen samples for calibration purposes and proof of the technique. Upper limits for the concentrations of carbon and oxygen were determined for tantalum and germanium samples.

### Thick Target Calculations

One of the objectives of this experiment was to develop analytical techniques so that the complex proton spectra from the active <sup>3</sup>He activation analyses could be unfolded. The advantages of having a technique that would unfold the proton spectra for any bombarding energy or matrix material made it important that these be included as part of the analytical techniques.

The thick targets were considered to contain only two important impurity atoms for producing (<sup>3</sup>He,p) reactions. These were carbon and oxygen. The samples analyzed were considered to contain impurity distributions of three different types:

1) A thin surface layer of carbon or oxygen that gives a response similar to that received from a thin target. There was a thin carbon layer on the samples analyzed from the carbon deposited by the beam. Thin oxide layers were present on the germanium and tantalum sample from surface oxidation.

- 2) An exponentially decreasing concentration from directly below the surface layer into the matrix material.
- A constant volumetric concentration of the carbon and oxygen impurities.

These assumptions on the distributions of the impurities in the sample give us the capability of analyzing proton spectra from both thick and thin samples, in addition to samples with surface layers and surface gradients. Based on physical intuition, these are the types of distributions that are to be expected.

The following equation was used to unfold the pulse-height distributions that were obtained from the proton detector.

$$C = \Phi\Omega \sum_{j=1}^{m} N_{j} \sum_{i=1}^{n} \sigma_{i,j} \left(\frac{dx}{dE}\right)_{i,j}$$

where

Φ is the total number of incident <sup>3</sup>He particles.

 $\Omega$  is the solid angle of the proton detector system,

- m is the number of reactions that contribute to the experimental spectrum,
- N<sub>j</sub> is the concentration of the jth impurity atom (atoms/b-cm) in the sample interval dx,

n is the number of nuclear states associated with the jth reaction, oi, j is the differential cross section (b) for protons from the ith state and the jth reaction.

x is the distance (cm) that the <sup>3</sup>He particles have penetrated the sample, <sup>1</sup>

E is the proton energy (keV) at the detector for protons from the ith state and the jth reaction, and

C is the number of counts in each channel (counts/keV).

The energy resolution of the proton spectrum is degraded primarily from the energy straggling of the protons as they lose energy in the target and absorber foil and also from the energy straggling of the <sup>3</sup>He particles as they are slowed in the target. Other lesser effects are from the angular resolution, from the resolution of the proton detector system, and from the energy spread in the incident <sup>3</sup>He beam. An empirical function with a Gaussian shape was used as the calculated resolution function. The width of the resolution function was dependent on the proton spectrum, the initial energy of the proton, and the proton energy at the detector.

$$D(E) = \frac{e^{-\frac{1}{2}(E-E_c)^2/\Delta E^2}}{2\pi \cdot \sqrt{\Delta E}},$$

where

D(E) is the distribution of the spread data,

ΔE (standard deviation of the Gaussian) where

$$\Delta E = \left\{ P(1) \cdot E_{c}^{2} / E_{R} + P(2) \right\}^{\frac{1}{2}}$$

<sup>&</sup>lt;sup>1</sup>From the incident <sup>3</sup>He energy, reaction kinematics and the energy loss data for the target and for the absorber foil, the functions  $x = f(E_{i,j})$  were calculated. These functions were interpolated using cubic splines and the first derivatives  $(dx/dE)_{i,j}$  were determined from these interpolated functions.

P(1) and P(2) are parameters for which the best least-squares values can be obtained,

 $E_{\mathrm{p}}$  is the proton energy at the reaction, and

E is the calculated proton energy at the detector.

The 17 parameters that may be least-squares fitted to the experimental proton spectral data are listed in Table 5. In general, several of these parameters were usually fixed for a given analysis.

The computer code that was used for this least-squares analysis has not been optimized for the most efficient and fastest convergence. The running time varies greatly depending on the number of free parameters, the <sup>3</sup>He energy, and whether both carbon and oxygen concentrations are being calculated. For the most complex case, the running time would be approximately 10 min on a CDC 7600 computer. The program uses approximately (200,000)<sub>8</sub> core locations.

This code has been designated IMP for IMPurity calculation code.

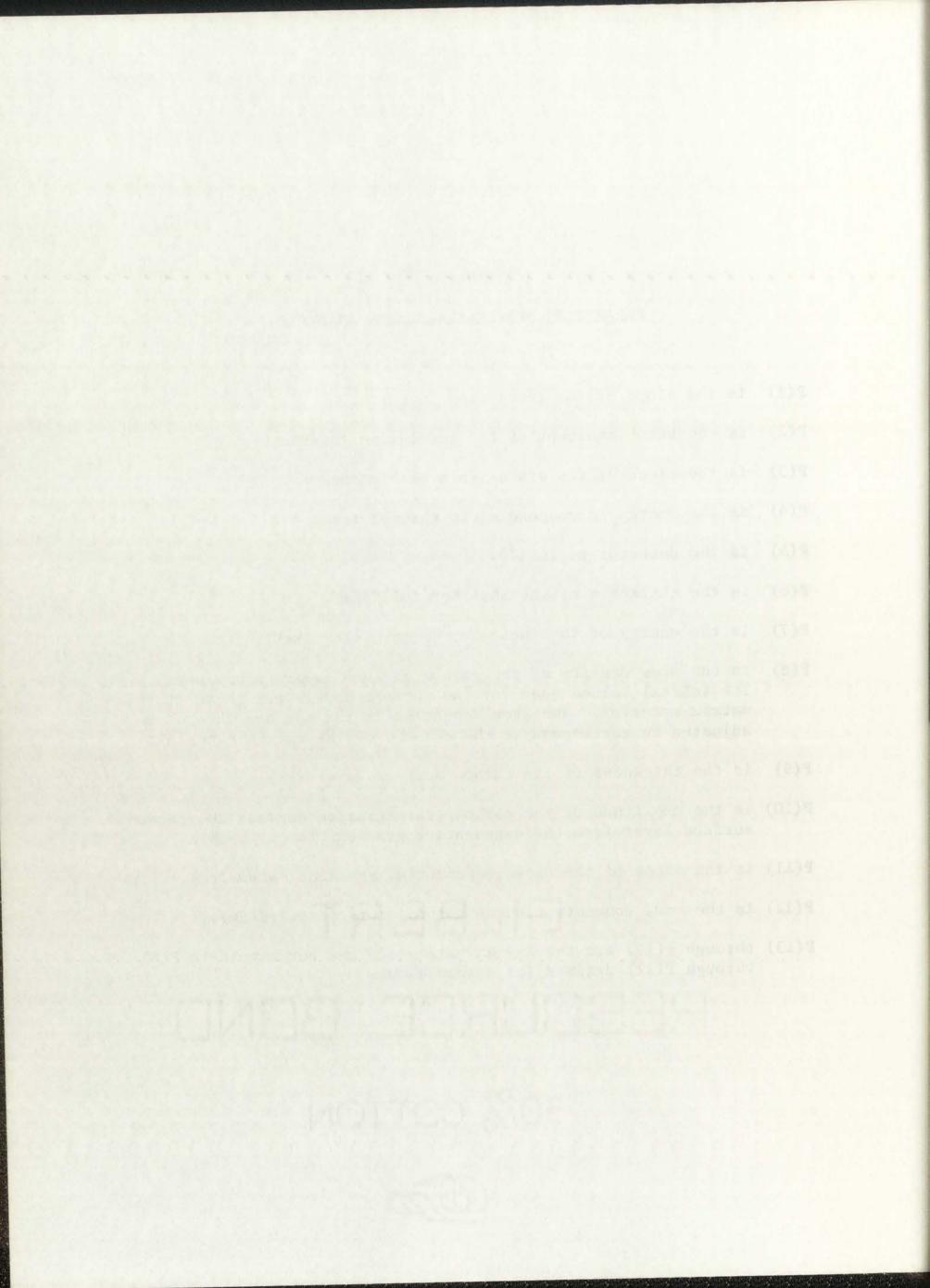
# Thin Oxygen Calibration Data

Figure 44 shows the proton spectrum from the oxygen calibration run that was unfolded using the IMP code. The results from this analysis compared quite favorably with those that were obtained using the C24HE3P unfolding code discussed in Appendix D. The thickness calculated by the IMP code was 54  $\mu g/cm^2$  compared to 48  $\mu g/cm^2$  previously calculated using comparable cross sections. This small difference could be due to several things, a slightly different resolution function, a more accurate calculation of the  $^3$ He energy in the thin layer, or a slight error in the dE/dx data that were used.

#### TABLE 5

### PARAMETERS FOR LEAST-SQUARES ANALYSIS

- P(1) is the slope of the resolution function.
- P(2) is the zero intercept of the resolution function.
- P(3) is the slope of the system gain (keV/channel).
- P(4) is the energy corresponding to channel zero.
- P(5) is the detector angle (°).
- P(6) is the thickness of the absorber foil (cm).
- P(7) is the energy of the incident  $^{3}$ He particles (keV).
- P(8) is the atom density of the carbon surface layer (atoms/b-cm). The (dE/dx) values used for the surface layers are those of the matrix material. The atom densities in the surface layers are adjusted to correspond to the density of the matrix material.
- P(9) is the thickness of the carbon surface layer (cm).
- P(10) is the amplitude of the carbon concentration beneath the carbon surface layer from the exponential gradient (atoms/b-cm).
- P(11) is the slope of the above exponential gradient (atoms/cm).
- P(12) is the body concentration of carbon atoms (atoms/b-cm).
- P(13) through P(17) are the oxygen parameters and correspond to P(8) through P(12) defined for carbon above.



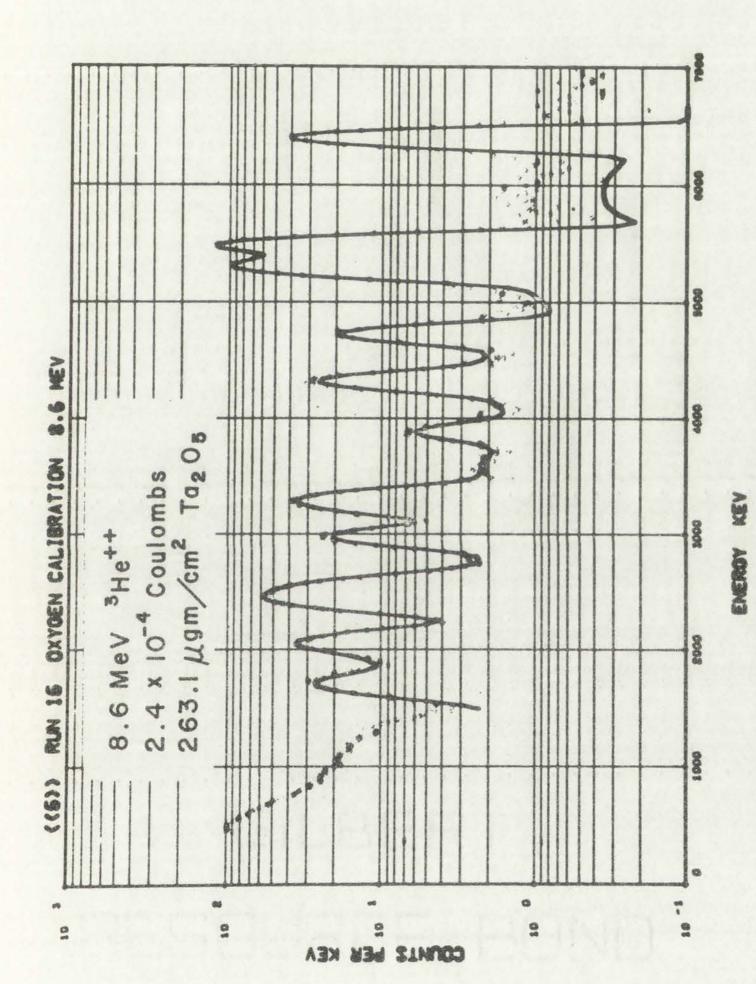


Fig. 44. Analysis of prompt proton spectrum from a thin oxygen sample using the IMP code.

# Thick Carbon and Oxygen Samples

Thick carbon and oxygen samples were irradiated with  $^3$ He particles, and the proton spectra were recorded ataa detector angle of  $160^\circ$ . Aluminum absorber foils with a total thickness from 60 to  $100~\mu$  were used. Data were obtained at  $^3$ He energies of 4.4, 5.175, 6.0, 6.5, 6.8, and 8.6 MeV. The results of these irradiations indicated that the oxygen and carbon cross sections that were calculated from the thin target irradiations at 8.6 MeV and the  $^{12}\text{C}(^3\text{He},\alpha)^{11}\text{C}$  and the  $^{16}\text{O}(^3\text{He},p)^{18}\text{F}$  cross sections from Refs. 2 and 18 were slightly inconsistent. The thick carbon data indicated that the  $^{12}\text{C}(^3\text{He},p)^{14}\text{N}$  cross sections were about 15% high and that the  $^{16}\text{O}(^3\text{He},p)^{18}\text{F}$  cross sections were about 40% too small. The cross-section data presented in Chapter IV have been corrected to correspond to these thick target irradiations. These differences are quite possibly due to the smoothing effect of the stacked foil technique on the resonance peaks that are present in the cross sections.

Figure 45 shows the analyzed proton spectrum from the irradiation of a thick carbon sample at 5.175 MeV <sup>3</sup>He energy. The analyzed data from a thick oxygen irradiation at 6.8 MeV <sup>3</sup>He energy are shown in Fig. 46. The small portion of data between 3.3 and 4.1 MeV that is not analyzed (these limits depend on the thickness of the absorber foil) is due to the lack of cross-section data for the <sup>12</sup>C(<sup>3</sup>He,p)<sup>14</sup>N ground-state reaction below a <sup>3</sup>He energy of 2.8 MeV. All spectra analyzed for carbon will contain this discontinuity.

To determine if differences in the current integration from the thick carbon and from the thick oxygen samples or absorbed water in the  ${\rm Ta}_2{}^0{}_5$  sample could have caused the deviations that were measured in these cross

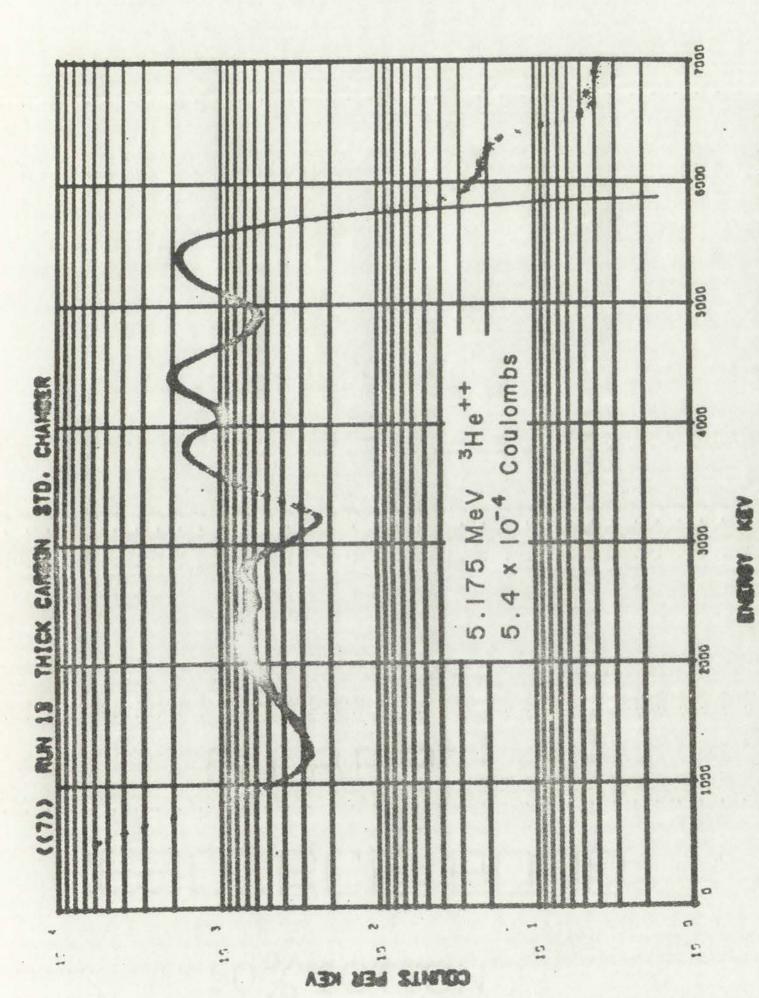
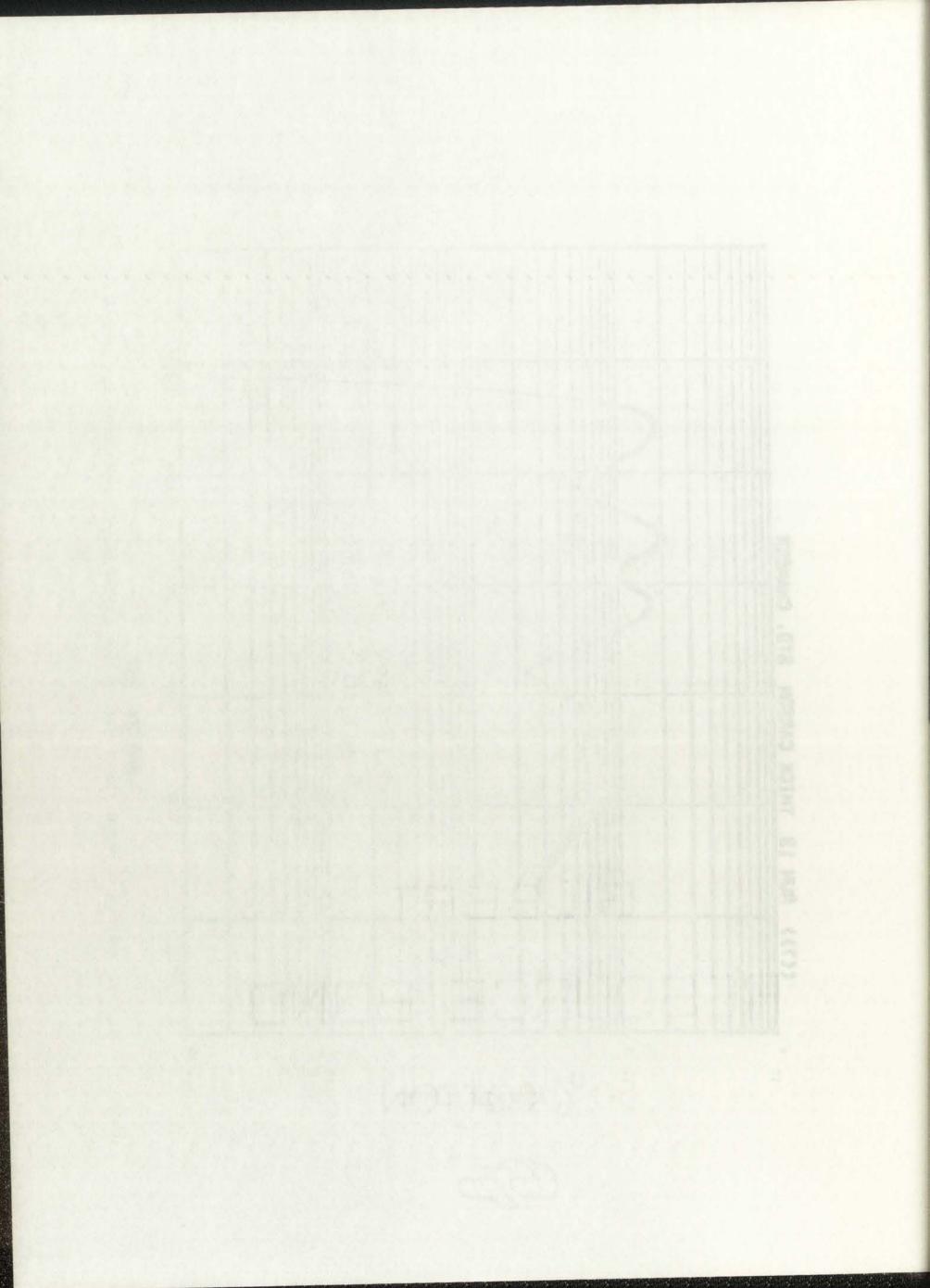


Fig. 45. Analysis of prompt proton spectrum from a thick carbon sample using the IMP code.



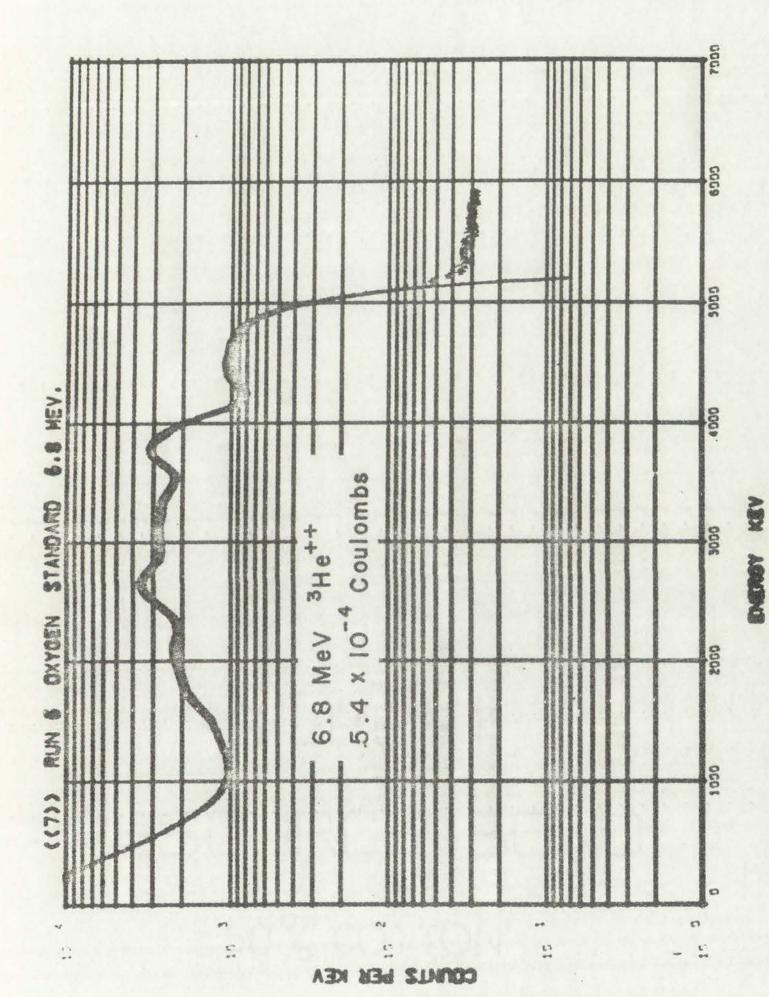
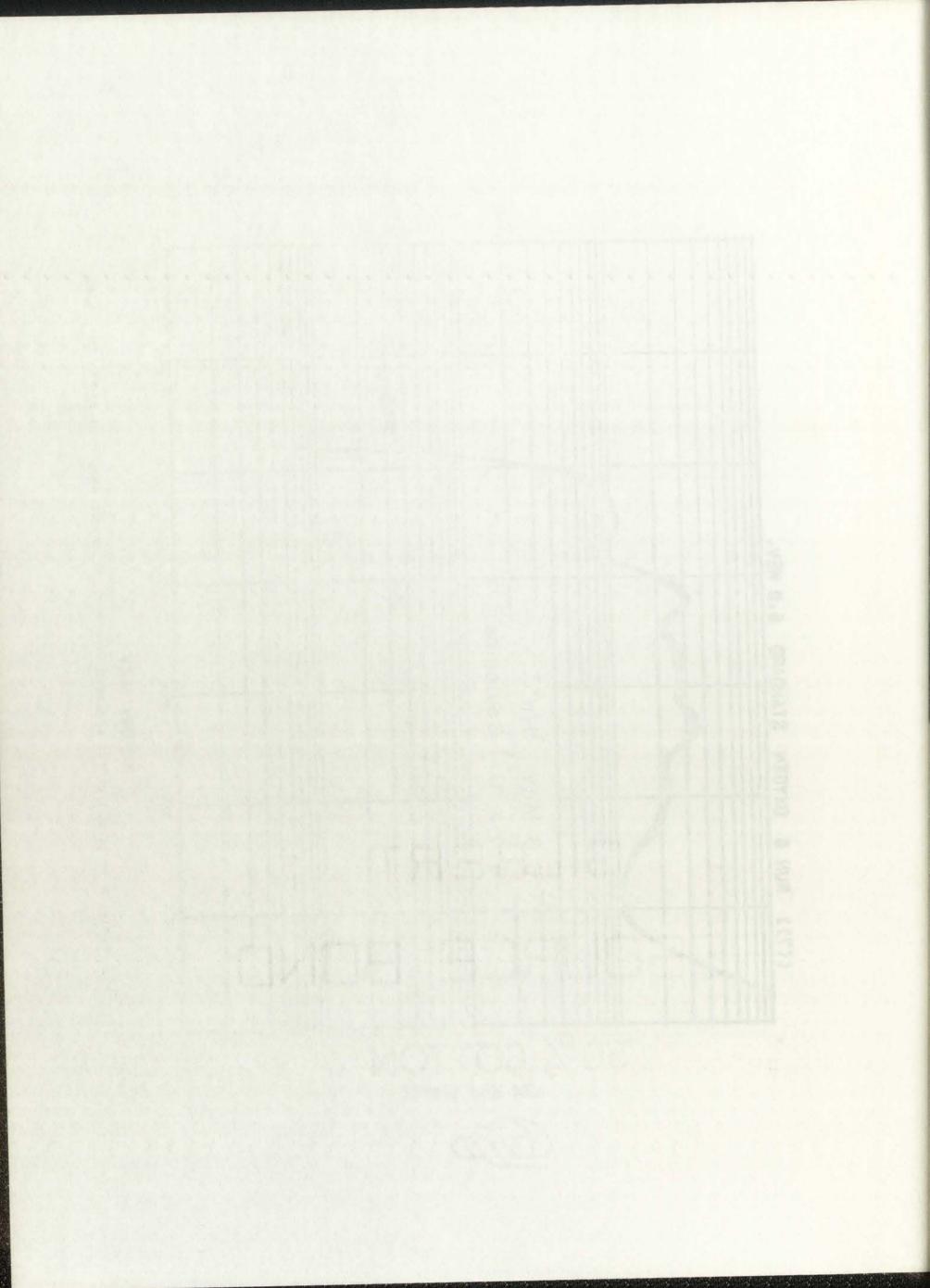


Fig. 46. Analysis of prompt proton spectrum from a thick oxygen sample using the IMP code.



sections, a calcite (CaCO<sub>3</sub>) sample<sup>1</sup> was irradiated and the C:O ratio was calculated. The calculated C:O ratio using the revised cross-section data was approximately 3.0. This compares favorably with the theoretical ratio. The analyzed calcite spectrum is shown in Fig. 47.

# Activation Analysis of Tantalum

Etched tantalum samples were irradiated at 5.175 and 8.6 MeV <sup>3</sup>He energies. These samples were analyzed for surface carbon, body carbon, surface oxygen, and body oxygen concentrations. The results of these analyses are given in Table 6. A typical analysis of a proton spectrum

TABLE 6

CARBON AND OXYGEN CONCENTRATIONS IN TANTALUM

Sample	3He Energy (MeV)	Surface Carbon (µg/cm <sup>2</sup> )	Body Carbon (ppm)	Surface Oxygen (µg/cm2)	Body Oxygen (ppm)
3	5.175	0.65	103	0.27	79
513	5.175	0.36	79	0.34	80
512	8.6	0.35	41	0.49	77
510	8.6	0.34	58	0.65	96

from a tantalum irradiation is shown in Fig. 48. The amount of surface carbon measured is from carbon deposited on the sample during the irradiation. Therefore, the values obtained for the surface carbon concentrations are greatly dependent on the quality of the vacuum in the target chamber and are not related to the sample. The amount of surface oxygen depends on the sample preparation and the length of time that the sample

<sup>&</sup>lt;sup>1</sup>A freshly cleaved sample from a crystal collected by Dr. Elva H. Clinard in the vicinity of the Harding Mine in New Mexico.

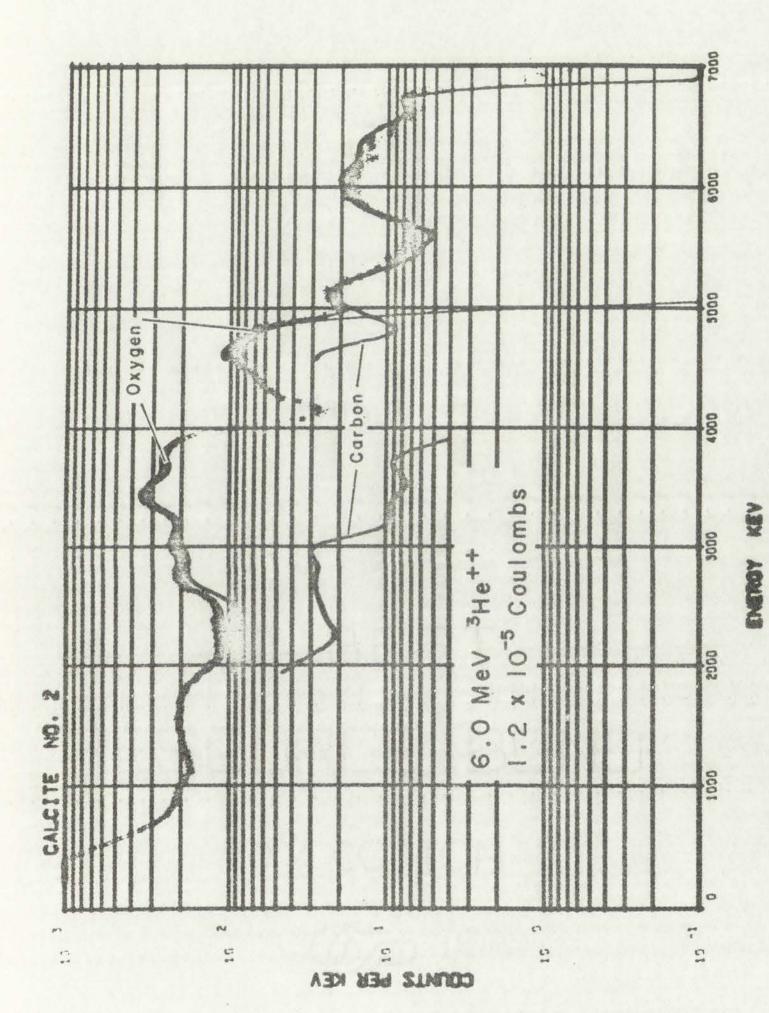
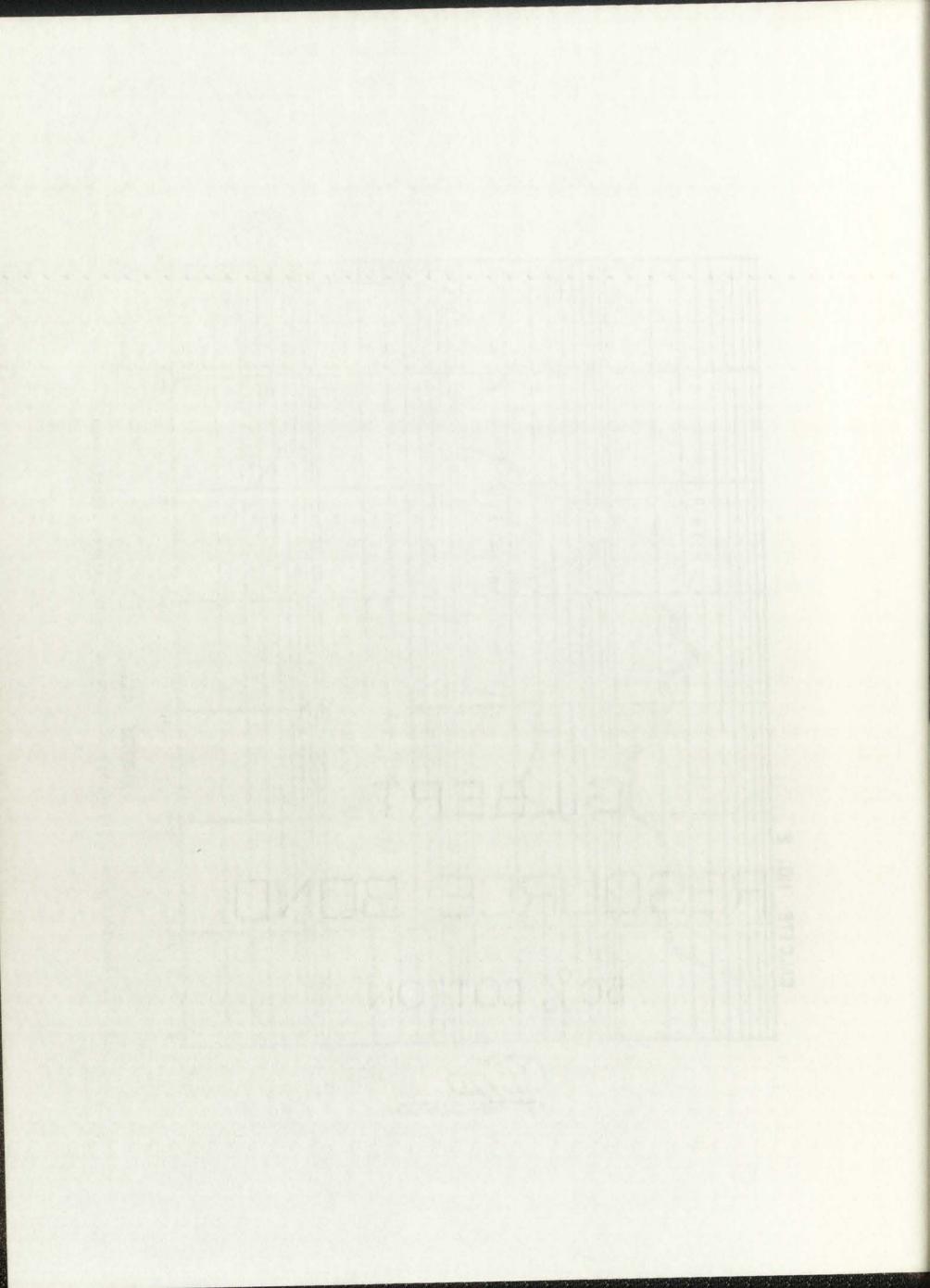
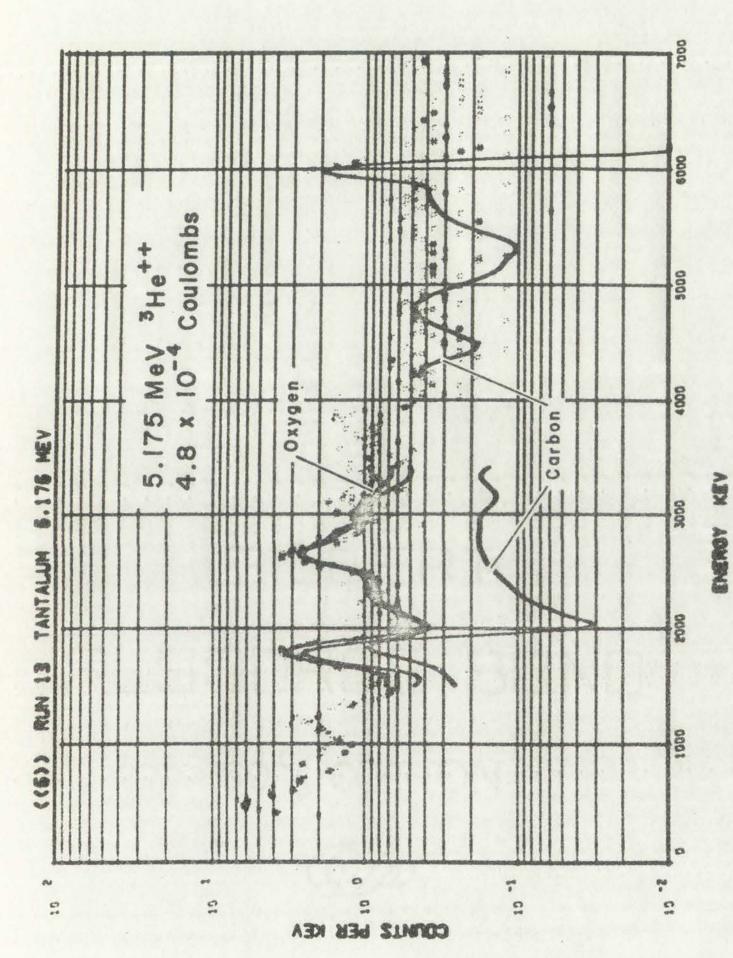


Fig. 47. Unfolded prompt proton spectrum from a 3he irradiated calcite sample.





Unfolded prompt proton spectrum from a tantalum activation sample. F18. 48.

surface was allowed to oxidize between sample preparation and irradiation. Therefore, a large variation in these surface concentrations could be expected since neither of the above variables was controlled.

The variations in the calculated values for the body oxygen concentrations are well within those expected from statistical fluctuations in the unfolding and fluctuations in the sampling process. The variations in the calculated values for the body carbon are fairly large. This might be attributed to the sampling process or the existence of an interference reaction.

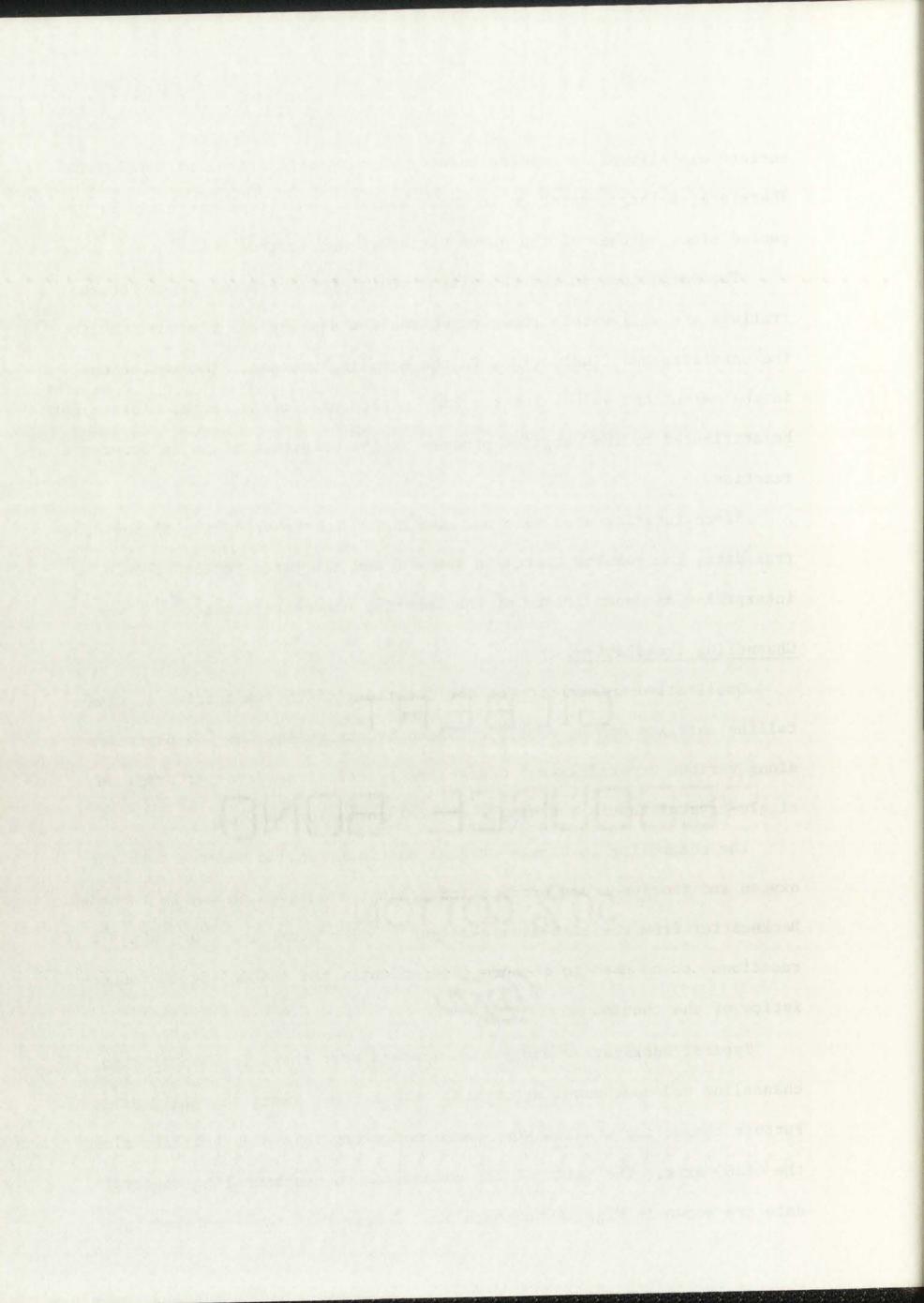
Since interferences were not considered in the unfolding of the spectral data, the results listed in Table 6 and all later results should be interpreted as upper limits of the impurity concentrations.

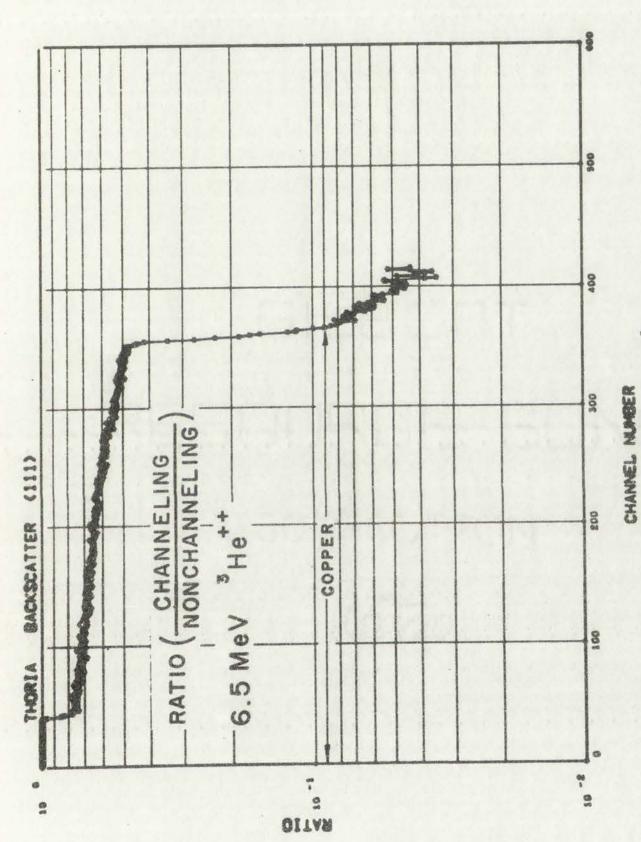
## Channeling Irradiations

Qualitative information on the locations of the impurities in crystalline matrixes can be easily obtained by channeling the <sup>3</sup>He particles along various crystal axes. Channeling irradiations were performed on single-crystal thoria and single-crystal germanium samples.

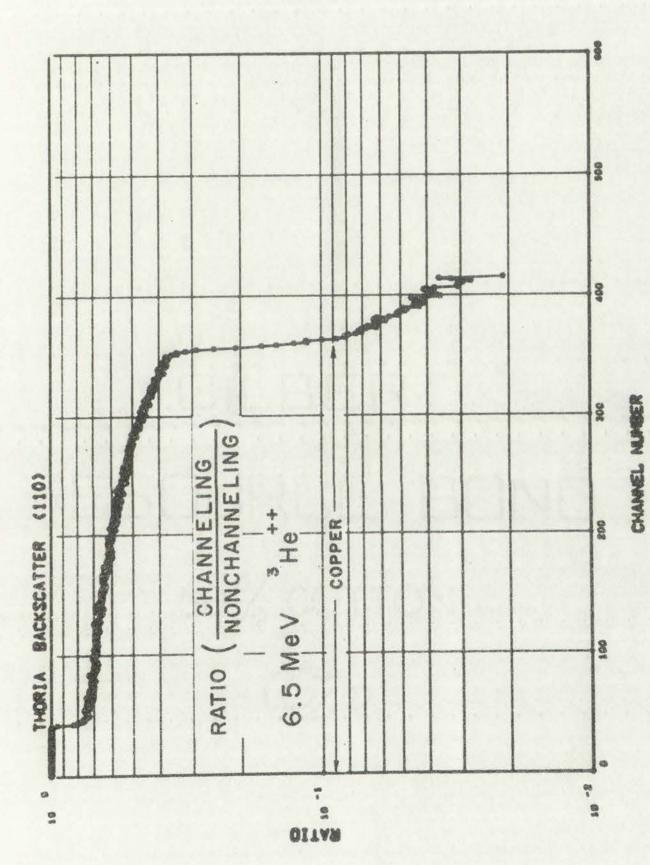
The channeling in single-crystal thoria is unique because both the oxygen and thorium atoms produce independent events which may be recorded. Backscatter from the high-atomic-weight thorium atoms and  $^{16}\text{O}(^{3}\text{He,p})^{18}\text{F}$  reactions can be used to measure independently the channeling characteristics of the thoria.

Typical backscatter and proton spectra were shown in Chapter V for channeling and nonchanneling crystal orientations along the <111> axis. Further channeling studies were performed along this axis and also along the <110> axis. The ratio of the channeling to nonchanneling spectral data are shown in Figs. 49 through 52. Thoria is a face-centered cubic

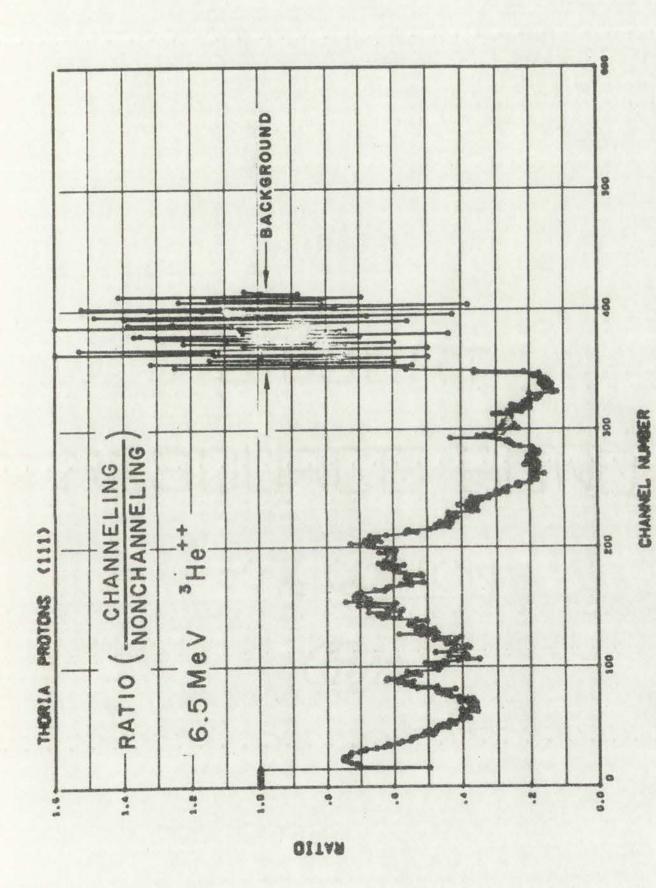




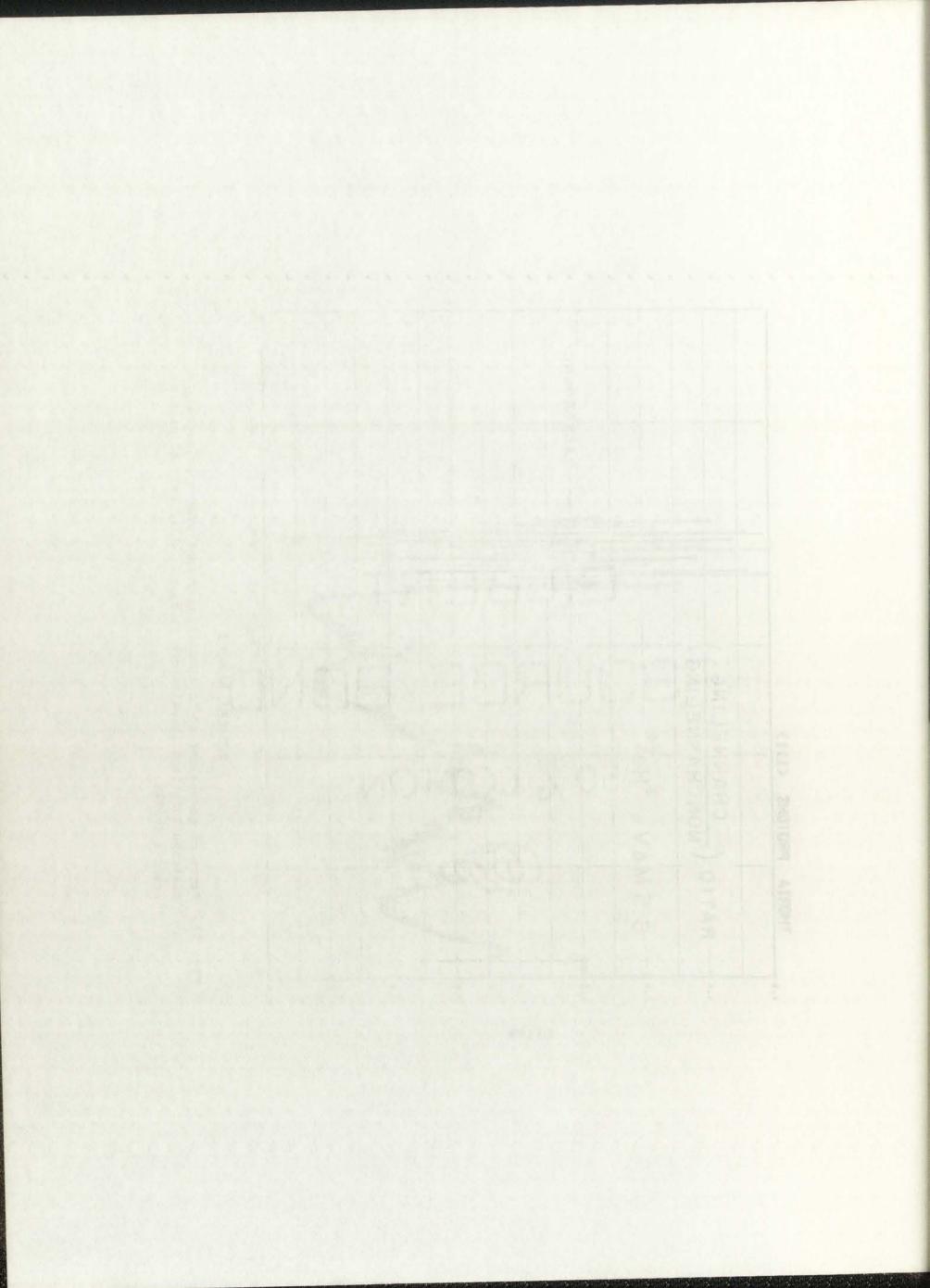
Ratio of channeling to nonchanneling <sup>3</sup>He backscatter pulse-height distributions from irradiations along the <111> axis of single-crystal thoria. F18. 49.



Ratio of channeling to nonchanneling 3He backscatter pulse-height distributions from irradiations along the (110) axis of singlecrystal thoria. F1g. 50.



Ratio of channeling to nonchanneling prompt proton pulse-height distributions from irradiations along the (111) axis of singlecrystal thoria. F1g. 51.



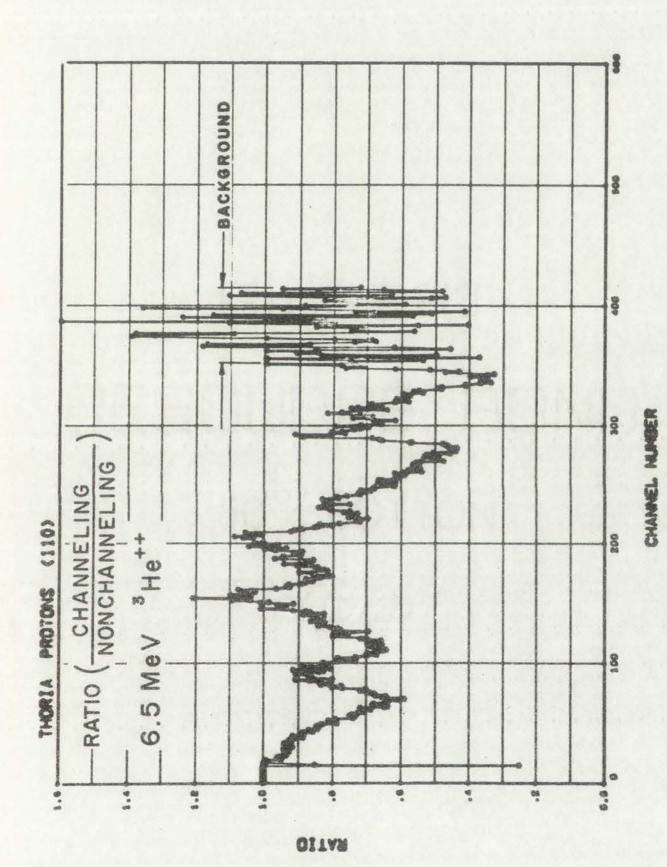
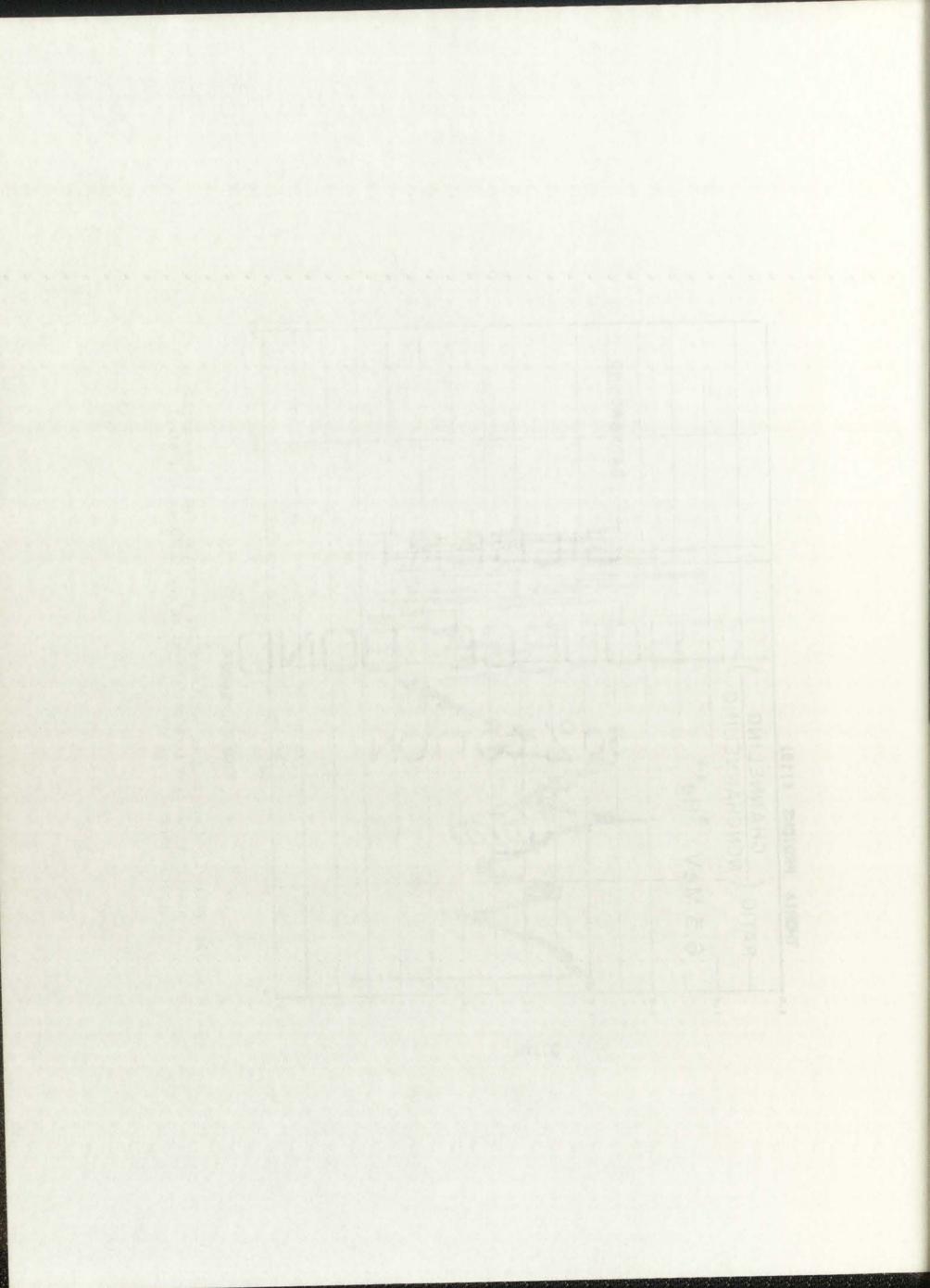


Fig. 52. Ratio of channeling to nonchanneling prompt proton pulse-height distributions from irradiations along the (110) axis of singlecrystal thoria.

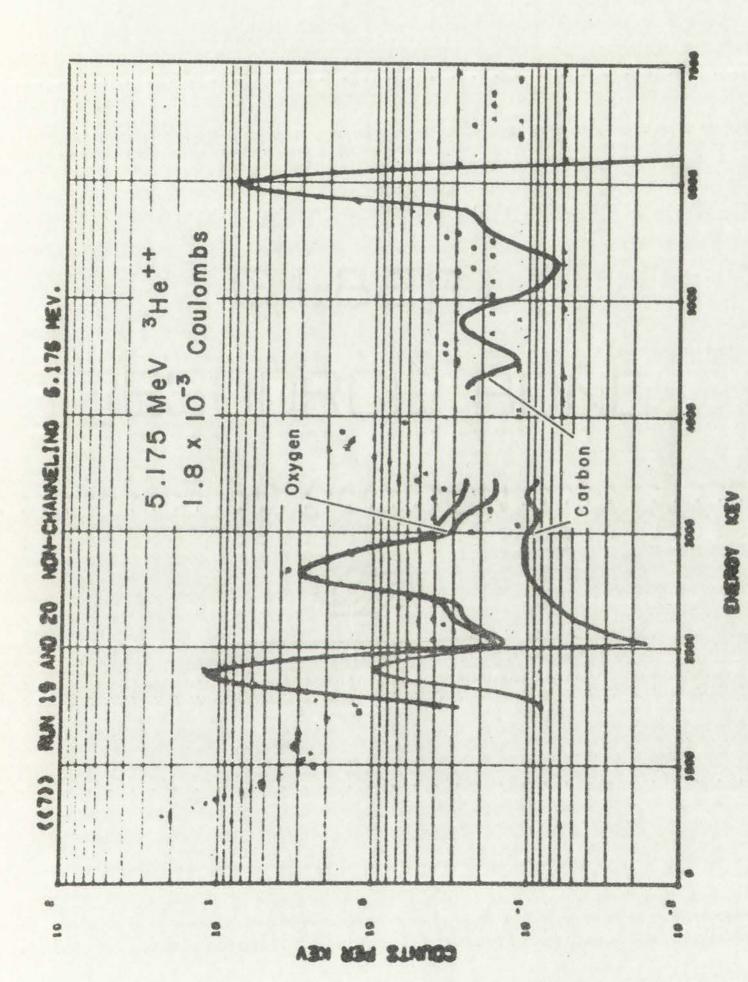


preferentially scatter from and activate interstitial impurities in the large (1/2,1/2,1/2) interstitial sites. However, channeling irradiations along the (110) axis should cause preferential activation of displaced oxygen atoms or impurity atoms located in these sites. Likewise, if the thorium atoms are displaced into these sites, increased backscatter should be measured relative to the increase in the number of counts in the proton spectrum from the oxygen atoms.

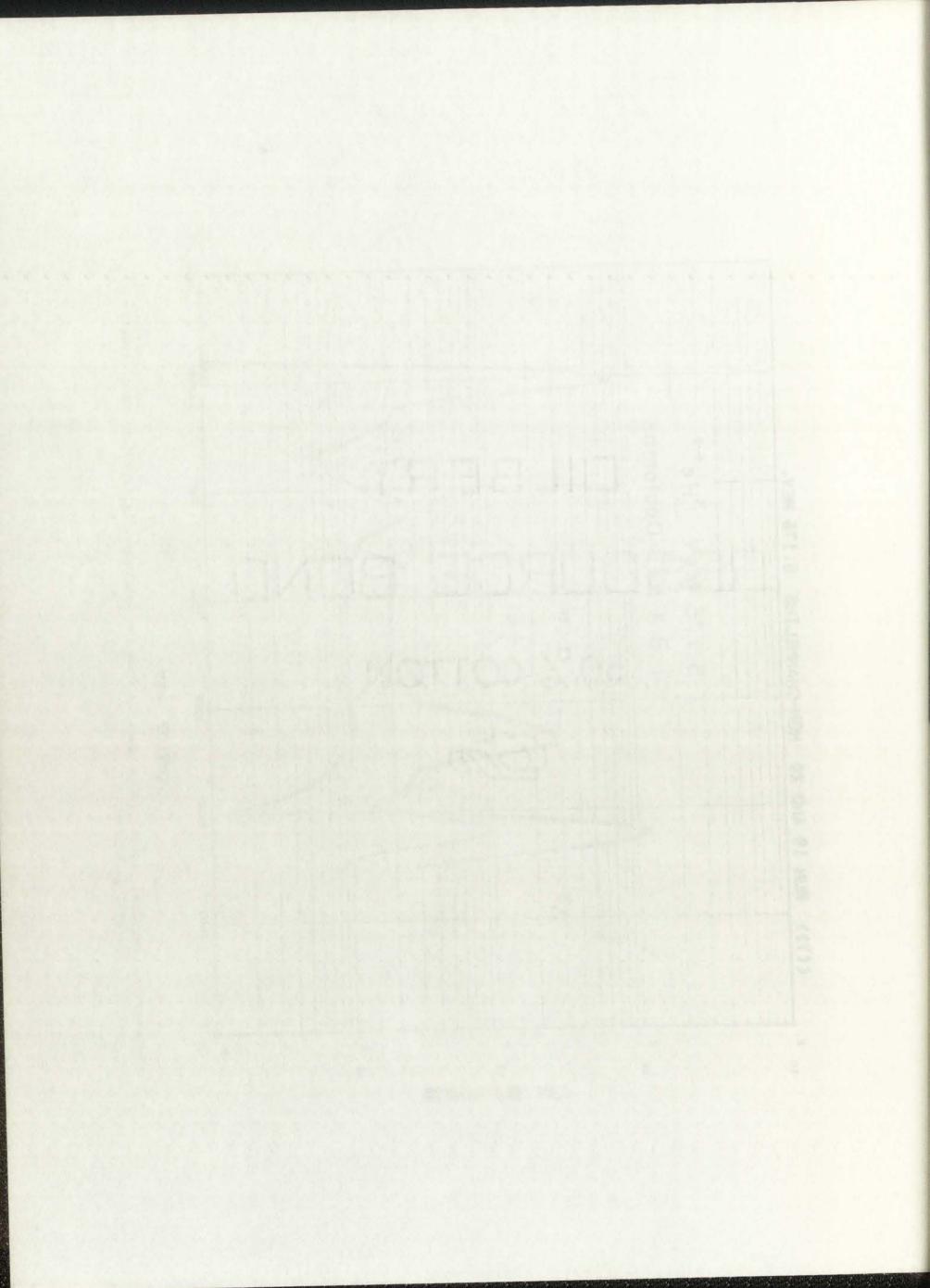
The ratio of the counts in the channeling backscatter spectrum to the counts in the nonchanneling backscatter spectrum that were obtained for the <111> channeling orientation is shown in Fig. 49. The corresponding ratio of data obtained for the <110> axis is shown in Fig. 50. These data are quite similar but with slightly better channeling along the <111> axis.

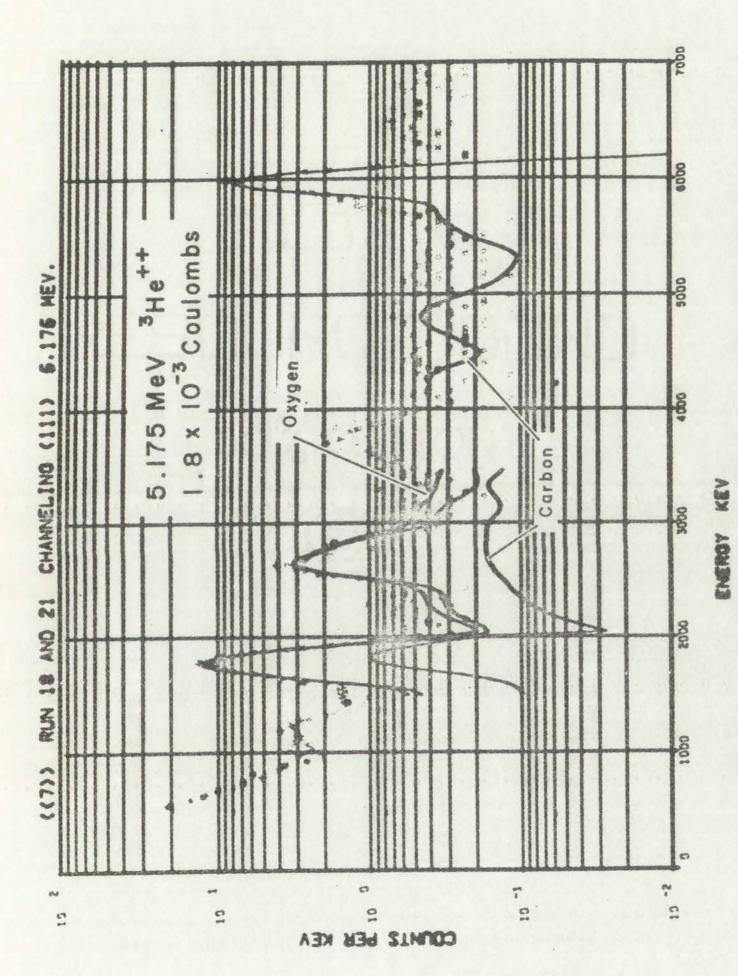
The corresponding ratio of the proton spectral data is shown in Figs. 51 and 52. Figure 51 is from data that were obtained near the  $\langle 111 \rangle$  axis, and Fig. 52 is from data that were obtained near the  $\langle 110 \rangle$  axis. There is a significant difference in these data. These proton data indicate much better channeling along the  $\langle 111 \rangle$  than along the  $\langle 110 \rangle$  axis. This is interpreted to indicate that the number of oxygen activations is increased because of displaced oxygen atoms in the  $(\frac{1}{2},\frac{1}{2},\frac{1}{2})$  sites which are unshielded and parallel with the  $\langle 110 \rangle$  axis.

Channeling and nonchanneling irradiations were performed on single-crystal germanium to attempt to measure and locate the oxygen and carbon impurity atoms. Figures 53 and 54 show the analyzed proton spectrum from the channeling and nonchanneling irradiations, respectively. The



Unfolded prompt proton spectrum from the nonchanneling irradiations of single-crystal germanium, Fig. 53.





Unfolded prompt proton spectrum from the channeling irradiation of single-crystal germanium along the (111) axis. Fig. 54.

results from these analyses are listed in Table 7. These irradiations were performed at 5.175 MeV  $^{3}\text{He}$  energy.

TABLE 7
GERMANIUM ACTIVATIONS

Sample Irradiation Number	Surface Carbon (µg/cm <sup>2</sup> )	Body Carbon (ppm)	Surface Oxygen (µg/cm <sup>2</sup> )	Body Oxygen (ppm)	Total Charge (C)
7-1920 nonchanneling	0.37	14	0.11	7.7	1.8 x 10 <sup>-3</sup>
7-1821 channeling <111>	0.35	22	0.11	9.2	1.8 x 10 <sup>-3</sup>
3-223 nonchanneling	0.33	20	0.08	13.4	3.0 x 10 <sup>-4</sup>

The surface carbon is from carbon that is deposited on the sample during the irradiation. The surface oxygen is from a thin oxide layer on the germanium. The slightly higher carbon and oxygen impurity concentrations measured in the channeling orientation (Sample 7-1821 and Sample 7-1920) indicate that both the carbon and the oxygen are mostly interstitial impurities. Sample irradiations 7-1821 and 7-1920 correspond to similar irradiations on the same sample, except for the channeling and nonchanneling parameters. Sample irradiation 3-223 was performed on a different sample during a different accelerator shift.

### Errors

The uncertainties associated with the data that are presented can only be estimated. The uncertainty in the cross-section data is estimated to be ±15%. The primary sources of this uncertainty are the solid angle of the detector system, the stopping power of the matrix material and the resolution function used in the unfolding code.

It is estimated that the uncertainties in the surface and body concentrations due to the statistical fluctuation in the unfolding process is much less than that due to the sampling process itself.

Insufficient data were obtained to calculate these uncertainties.

#### CHAPTER VII

#### CONCLUSIONS

High-energy reaction protons, due to the high Q value of the ( $^3$ He,p) reactions with oxygen and carbon, present a unique method of studying the surface and body concentrations of these isotopes in high-Z samples. This active method allows the determination of surface layer thicknesses in the 0.01  $\mu g/cm^2$  region and body concentrations in the 1.0 ppm region. There are low backgrounds associated with this type of measurement.

The thin sample cross sections that were determined and used in the unfolding code allow proton spectral data to be analyzed for various <sup>3</sup>He energies, matrix materials, and impurity distributions. The optimum <sup>3</sup>He energies for activation analysis for carbon and for oxygen in the presence of each other can be calculated using the techniques that are presented.

Channeling phenomena can be used to obtain qualitative information on the location of the oxygen and carbon impurities in crystalline matrixes. If the impurities are substitutional, the effective cross sections will be lowered for all channeling irradiations. If the impurities are interstitial, preferential activation of the impurities will be obtained for irradiations in some of the major channeling directions. Irradiations of single-crystal germanium indicated that the carbon and oxygen impurities were primarily interstitial.

Because of their large Q values, it appears that boron and/or nitrogen could produce a significant interference if they were present in the sample. Isotopes of both of these elements have (3He,p) reactions with

quite large positive Q values. The (<sup>3</sup>He,p) reactions involved are of no importance to normal passive analyses, since all of the reaction products are stable. The percent natural abundance and Q values for these reactions are listed in Table 8.

TABLE 8

POSSIBLE INTERFERENCE REACTIONS

Reaction	Abundance (%)	Q Value (MeV)
$^{10}_{\rm B}(^{3}_{\rm He,p})^{12}_{\rm C}$	18.83	19.6945
$^{11}_{\text{B}}(^{3}_{\text{He,p}})^{13}_{\text{C}}$	81.17	13.1854
$^{14}N(^{3}He,p)^{16}O$	99.64	15.2426
<sup>15</sup> N( <sup>3</sup> He,p) <sup>17</sup> O	0.36	8.5504

It should be possible to measure nitrogen impurities in addition to carbon and oxygen by using these techniques.

The phenomenon of carbon buildup on the targets during the irradiations was a problem. The buildup rate seemed to vary directly with the pressure in the vacuum system. Installation of additional liquid nitrogen cold traps and vacuum pumps near the target chambers lowered the carbon buildup rate to a tolerable background.

The carbon buildup on the sample surface was greatly reduced during the channeled germanium irradiations. It is suspected that the energy and kinetmatics of the carbon atoms that normally adhere on the surface are such that they channel deeper into the crystal before stopping and do not add to the carbon surface layer.

Sample temperature and radiation damage should be considered when doing channeling experiments. At higher sample temperatures, the increased thermal motion of the lattice will decrease the amount of channeling. Radiation damage to the lattice structure during the bombardment will also decrease the amount of channeling. To minimize the increase in sample temperature and also the radiation damage to the sample, low particle energies and currents were used in the irradiations.

The techniques and data that have been presented offer new and interesting ways to study carbon and oxygen impurity concentrations in materials.

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#### APPENDIX A

#### DECAY CURVE ANALYSIS CODE

This code is written in FORTRAN IV for the CDC 6600 computer to unfold the complex decay curves that were obtained using the large  $4\pi$  detector system.

Activation analyses with <sup>3</sup>He quite often result in reaction products that are neutron poor and decay by positron emission. Two reasonably long-lived reaction products from the bombardment of carbon and oxygen are <sup>11</sup>C and <sup>18</sup>F. Both of these decay by positron emission, and the complex decay curve obtained from counting the annihilation gamma rays must be unfolded into its components to determine how much carbon and how much oxygen were present in the sample. Special analyses and detector equipment can be used where there is a gamma ray coincident with the positron decay of an activation product (Ref. 40); however, this is not the case with <sup>11</sup>C and <sup>18</sup>F.

Shortly after the completion of an activation irradiation, the sample was placed in the 4 $\pi$  detector. Both coincident and singles spectra were recorded at 100-sec intervals using a 4096-channel ADC. The entire 4096 channels of data could be transferred to magnetic tape in 2.14 sec. At the tape densities used, slightly more than 1000 spectra could be recorded on a single tape. Data from these tapes were used as input to the DECURA code.

The function

$$Y(J) = P(1)*\sum_{I=1}^{NOI} P(I*2)*EXP(P(I*2+1)*X(J))$$

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is least squares fitted to the data. The J subscript refers to the Jth data point, and the I subscript refers to the Ith exponential. Best least-squares values can be obtained for each of the parameters, P(I), in the equation. The parameters may be fixed (held constant at the input value) or free (allowed to vary until their best-least-squares value is obtained). Y(J) is the rate of decay (counts/sec), and X(J) is the elapsed time since the irradiation stopped (sec). No provision is made in the code to correct for decay during the counting interval. Therefore, the count interval should be much less than the mean life of the shortest half-lived isotope that is being counted. The code will fit a maximum of ten exponentials and 4096 data points.

The code is written to use data from a 4096-channel spectrum for each input data point. Various sections of each spectrum are summed and stored as the dependent variable after the data are corrected for dead time.

Least-squares techniques of Moore and Zeigler (Ref. 41) are used in the code.

## Main Program DECURA

The main program calls the subroutines and sets up the fixed parameters for the first five iterations. If some of the exponential slopes are designated as being free, they will be fixed for the first five iterations, and only those amplitudes that are designated as being free are allowed to vary. Usually P(1) is fixed; however, if P(1) is free, the calculation starts at iteration five.

The more important variables used in the main program are listed in Table 9.

TABLE 9

## MAIN PROGRAM DECURA VARIABLES

IM number of fixed parameters

IPLTFL input flag

IT number of iterations

IX indexes of fixed parameters

NODP number of data points being fit

P(I) best-least-squares value of the Ith parameters

PART(I) partial derivative of the function with respect to the Ith parameter

PG(I) input values of the Ith parameter

## Subroutine BSS

This is the Linear System Solver (LSS) subroutine, 1 except for minor changes.

## Subroutine DINSET

Most of the input data are processed by this subroutine (see also subroutine PLOTGN). The input data is entered into the computer by cards and by magnetic tape. Tape 10 refers to the card input file, and Tape 7 refers to the magnetic tape input.

The magnetic tape input contains the 4096-channel spectra that are to be analyzed. Up to 50 sections of each spectrum can be summed and stored as the dependent variable.

<sup>&</sup>lt;sup>1</sup>The LSS subroutine, LA-FD04, may be obtained by writing to C Division of the Los Alamos Scientific Laboratory.

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This version of DINSET was written to analyze spectra that were accumulated in clock time, and a 60-Hz pulser with a constant output voltage was used to indicate the dead time for each spectrum.

The more important variables used in this subroutine are listed in Table 10.

### Live Time Calculation

Constant voltage pulses from a 60-Hz pulser were recorded and used to determine the live time during the count intervals. The total counts in the pulser peak were determined by summing 29 channels above to 30 channels below the peak channel. (The peak channel number is input for the first spectrum.) After the first spectrum, the value determined from the previous spectrum is used for the peak channel number. From this sum, the counts in 30 channels below and 30 channels above this region are subtracted for background. The channel containing the most counts in this calculation is used as the peak pulser channel for the following spectrum to be analyzed. This allows the code to accommodate slight changes in the system gain or pulser input voltage.

#### Input Formats and Data

The format on the magnetic tape input is:

Record Number	Information		
1	89999 first record of data set		
2	00001 data set number		
3	80 BCD characters, title information		
4	90001 control character and spectrum number		
5 to 192	spectral data		

The above sequence from Record 4 is repeated for each spectrum on the tape.

# TABLE 10

# SUBROUTINE DINSET VARIABLES

	SUBROUTINE DINSET VARIABLES
DTSEC	clock time for each data accumulation
IK	total number of parameters
IM	number of fixed parameters
IPR	print control flag
ITAG1	spectrum number
IX(I)	indexes of fixed parameters
KGMAX(I)	maximum channel of the Ith region of each spectrum that is to be summed
KGMIN(I)	minimum channel of the Ith region of each spectrum that is to be summed
KGROUP	number of regions in each spectrum that are to be summed
LLEH	plot control flag
MAXSP	number of the last spectrum that is to be analyzed
MINSP	number of the first spectrum that is to be analyzed
NODP	number of data points that have been generated and are to be fitted
NOI	number of exponentials to be used in the fit
NOIT	maximum number of iterations that are allowed before forced convergence
NPUL	channel containing the most counts in the pulser peak
OTIME	elapsed time (sec) from when the irradiation stopped until the start time of the first spectrum to be analyzed
PG(I)	initial input values of the parameters
TITT(I)	title information (80 BCD characters)
TLIVE	live-time (sec) calculated from the pulser peak
W(I)	statistical weight of the Ith data point
X(I)	elapsed time (sec) from when the irradiation stopped until the accumulation of data started for the Ith data point
Y(I)	counts/sec calculated for the Ith data point

storage for the 4096-channel spectrum

YY(I)

The card inputs (Tape 10) are:

Card Sequence	Information
1	READ (10,90) (TITT(I), I=1,8)
	FORMAT (8A10)
	This is the title card.
2	READ (10,95) NOI, IM, (IX(I), I=1, IM)
	FORMAT (1813)
	NOI is the number of exponentials.
	IM is the number of fixed parameters.
	IX(I) are the indexes of the fixed parameters.
3	READ (10,100) PG(1)
	FORMAT (E12.7)
	PG(1) is the normalizing parameter. It is used when a set of exponentials is fitted to data. Usually the value of this parameter is 1.0.
4 to 3 + NOI	READ (10,100) (PG(I), I=2, IK)
	FORMAT (2E12.7)
	PG(I), I even, are the amplitudes of the Ith exponential at zero time in counts/sec.
	$PG(I)$ , I odd, are the slopes of the Ith exponential. These are decay constants in $sec^{-1}$ .
	One card containing the amplitude and slope is required for each exponential.
4 + NOI	READ (10,105) KGROUP, NOIT, IPR, LLEH, NPUL
	FORMAT (1216)
	KGROUP is the number of regions that are to be summed in each spectrum for the dependent variable. Fifty regions may be defined.
	NOIT is the maximum number of iterations that is allowed before convergence is forced. A normal problem should have converged in 25 iterations.

The card Seguida (Table 10) even

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sort is the maximum number of fractions that is all covered before to covered. A covered problem should have converged to if therestons.

## Card Sequence

### Information

IPR is the print control flag.

- = 0, do not print the parameter values after each iteration.
- # 0, print the parameter values after each iteration.

LLEH is the plot control flag.

- = 1, read in card containing the plot parameters.
- # 1, plot code generates its own plot parameters.

NPUL is the channel containing the maximum number of counts in the pulser peak for the first spectrum.

5 + NOI to 4 + NOI - KGROUP

READ (10,105) KGMIN(I), KGMAX(I)

FORMAT (1216)

These are the minimum and maximum channels for the Ith region to be summed in each spectrum.

5 + NOI + KGROUP READ (10,120) OTIME, DTSEC, MINSP, MAXSP

FORMAT (2F12.0,216)

OTIME is the elapsed time (sec) from when the irradiation stopped until the first spectrum to be analyzed.

DTSEC is the clock time for the accumulation of each spectrum. 2.14 sec is added to this time to obtain the elapsed time between spectra.

MINSP is the number of the first spectrum that is to be analyzed.

MAXSP is the number of the last spectrum that is to be analyzed.

The above card may be repeated if you desire to analyze more than one section of data from Tape 7.

BLANK CARD A blank card is used to indicate the end of the above input.

If the plot control flag (LLEH) equals 1, an addi-PLOT CARD tional card is necessary.

READ (10,145) XL, XR, YT, YB, KDY

### Card Sequence

## Information

PLOT CARD (continued)

FORMAT (4E12.7, 16)

XL is the left boundary of the plot.

XR is the right boundary of the plot.

YT is the log<sub>10</sub> (top boundary).

YB is the log<sub>10</sub> (bottom boundary).

KDY is the number of vertical lines dividing the X axis. One-half of these lines will be scaled.

### Subroutine MAZGN

This subroutine does the least-squares fit to the data using techniques of Moore and Zeigler (Ref. 41). Bounds and other restrictions are placed on the parameters so that convergence is obtained even for poor data or, in some cases, for poor initial guesses for the initial values of the parameters.

If an exponential amplitude, P(2\*I), tries to change sign during an iteration, the calculated value for this parameter is set to P(2\*I)/2.0. If this results in a value that is less than Y(N)/5000.0, the parameter is then fixed at a value equal to Y(N)/5000.0, where the N subscript refers to the last data point.

The exponential slopes, P(2\*I+1), are not allowed to change sign. If an exponential slope tries to change sign during an iteration, this parameter is fixed at its initial input value. The calculated values for the exponential slopes must remain within a factor of 2 of their initial input values. If these bounds are exceeded, the parameter is fixed at its initial input value. The iteration number is not incremented for an iteration where a parameter was fixed.

The more important variables used in this subroutine are listed in Table 11.

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# TABLE 11

# SUBROUTINE MAZGN VARIABLES

J) matrix elements
J) matrix elements
correction to Ith parameter for one iteration
lower bound of the exponential amplitudes
number of parameters
number of fixed parameters
I flag that determines type of calculation to be made by the PHICAL subroutine
output flag
iteration number
indexes of the fixed parameters
number of free parameters
convergence flag
number of data points
number of iterations before forced convergence
best value of the Ith parameter
I) partial derivatives
just-calculated value of the Ith parameter
initial estimate of the Ith parameter
deviation of the Ith parameter
convergence factor
statistical weight of the Ith data point
weighted variance
independent variable
dependent variable
calculated value of the function at the Ith data point

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W(I)W

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Y(I)Y

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# Subroutine OUTGN

Essentially all of the output by this code is through this subroutine. The output from a sample problem is given at the end of this appendix. The initial value, calculated value, and standard deviation are printed for each parameter. The data point number, weight, independent variable, dependent variable, calculated function, deviation, and standard deviation of the predicted mean are printed for each data point.

Since the code will fix parameters if restrictions on sign changes and bounds are not met, the output should be carefully checked to determine which parameters were fixed when the calculation converged. If a parameter is fixed, both the initial guess and calculated value are identical, and the standard deviation of the calculated value is zero.

The more important variables used in this subroutine are listed in Table 12.

## Subroutine PHICAL

This subroutine evaluates the function for use in the plot routine, calculates the sum of the squares of the deviations or calculates the weighted sum of the squares of the deviation that is used to calculate the weighted variance. IPLTFL indicates which of the above options is to be calculated. If IPLTFL = 1, the function is evaluated for each X(I) and stored as Y(I), destroying the original Y(I). If IPLTFL = 2, the sum of the squares of the deviations is calculated and stored as PHI. If IPLTFL = 3, the weighted sum of the squares of the deviations is calculated and stored as WVAR. This variable is later used to calculate the weighted variance. For both IPLTFL = 2 and = 3, it is assumed that the original Y(I)'s are stored.

# TABLE 12

# SUBROUTINE OUTGN VARIABLES

B(I)	best values of the parameters													
DY(I)	deviation of the function at the Ith data point													
IB(I)	indexes of the fixed parameters													
IK	number of parameters													
IP	number of fixed parameters													
IT	number of iterations													
NODP	number of data points													
NOI	number of exponentials													
PDD	standard deviation of the predicted mean													
PG(I)	initial value of the Ith parameter													
SA(I)	standard deviation of Ith parameter													
TITT(I)	title information													
W(I)	statistical weight of Ith data point													
WVAR	weighted variance of the fit													
X(I)	independent variable													
Y(I)	dependent variable													
YC(I)	calculated value of the function at the Ith data point													

The more important variables used in this subroutine are listed in Table 13.

#### TABLE 13

#### SUBROUTINE PHICAL VARIABLES

IPLTFL	control flag for type of calculation
NODP	number of data points
NOI	number of exponentials
P(I)	best value of the Ith parameter
PHI	sum of the squares of the deviations
W(I)	statistical weight of the Ith data point
WVAR	weighted sum of the squares of the deviations
X(I)	independent variable
Y(I)	dependent variable

## Subroutine PLOTGN

Subroutine plotgn is used to plot the data using the SC4020 plotter. Variable LLEH determines if the plot boundaries are to be determined by the subroutine or read as part of the card input. This plot option was discussed in the section on the DINSET subroutine.

The plots generated are semi-log. The dependent variable is counts/
sec, and the independent variable is decay time after the irradiation in
sec. The data points, the calculated function, and the individual
exponentials are plotted.

The standard boundaries that are determined by the subroutine,

LLEH # 1, are set so that only complete cycles are plotted, and all but

the bottom cycle will contain data points. The left boundary will be

100 sec less than the first data point truncated to the nearest 100 sec.

Similarly, the right boundary will be 100 sec greater than the last data point truncated to the nearest 100 sec.

This subroutine uses the X's and Y's as temporary storage and destroys the original data after plotting it.

The following subroutines, written for using the SC 4020 plotter have been used in the PLOTGN subroutine.

Number	Subroutine Called
LA JEO6	ADV, FRAME, EMPTY
LA JE07	DGA, DLNLG, SLLOG, SBLIN, PLOT
LA JE09	WLCV, WLCH

The more important variables used in this subroutine are listed in Table 14.

TABLE 14

## SUBROUTINE PLOTGN VARIABLES

A(I)	labels for the plot axes
B(I)	best values of the parameters
IPLTFL	flag for PHICAL subroutine
LLEH	plot flag
NODP	number of data points
NOI	number of exponentials
TITT	title information
X(I)	independent variable
XL	left plot boundary
XR	right plot boundary
Y(I)	dependent variable
YB	log <sub>10</sub> (bottom boundary)
YT	log <sub>10</sub> (top boundary)

<sup>&</sup>lt;sup>1</sup>Copies of these subroutines may be obtained by writing to C Division of the Los Alamos Scientific Laboratory.

## Subroutine YP

This subroutine evaluates the function and calculates the partial derivatives of the function with respect to each parameter. The function is

$$Y(J) = P(1)*\sum_{I=1}^{NOI} P(I*2)*EXP(P(I*2+1)*X(J))$$

where J refers to the Jth data point and I refers to the Ith exponential.

This subroutine is entered for each data point during each iteration performed by the MAZGN subroutine.

The more important variables used in this subroutine are listed in Table 15.

#### TABLE 15

#### SUBROUTINE YP VARIABLES

NOI number of exponentials

P(I) best values of the parameters

PART(I) partial derivatives

YT value of the function

ZZA value of X where the function is evaluated

## Sample Problem

Input for a sample problem and the output from it are presented on the following pages. This code is available for distribution from the author and will be copied and sent to those wishing to use it.

## SAMPLE INPUT FOR DECURA CODE

```
THIN CARBON 3HE ACTIVATION.

4 4 1 3 7 9

1.0 E+0

1.7080 E+4-.54759 E-3

6.5360 E+3-.12609 E-2

6.2965 E+2-.1050223E-3

5.0349 E+20.0 E+0

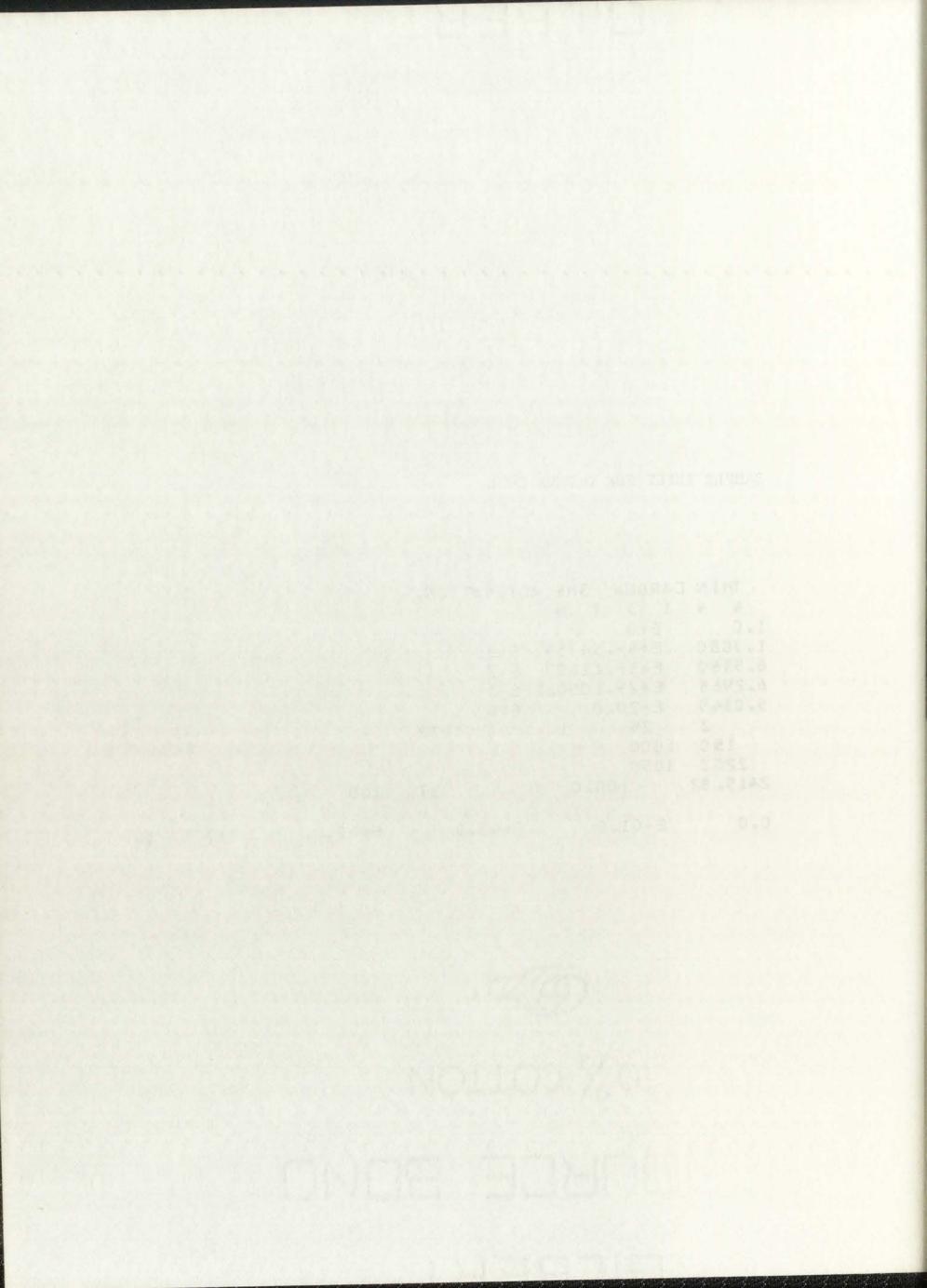
2 25 1 1 1938

150 1000

2200 3050

2415.82 100.0 37 108

C.0 E+01.0 E+45.0 E+02.0 E+0
```

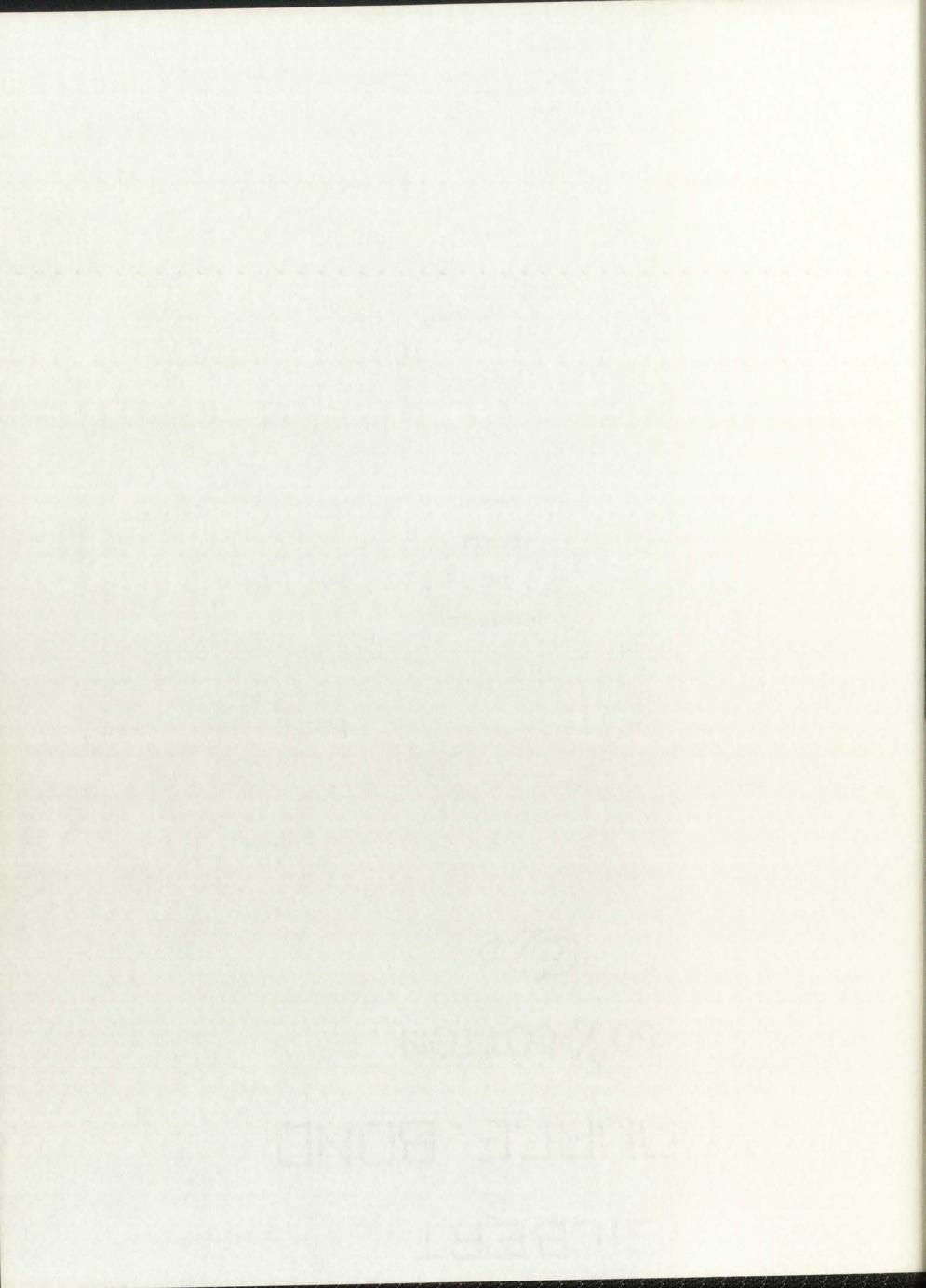


SAMPLE

OUTPUT

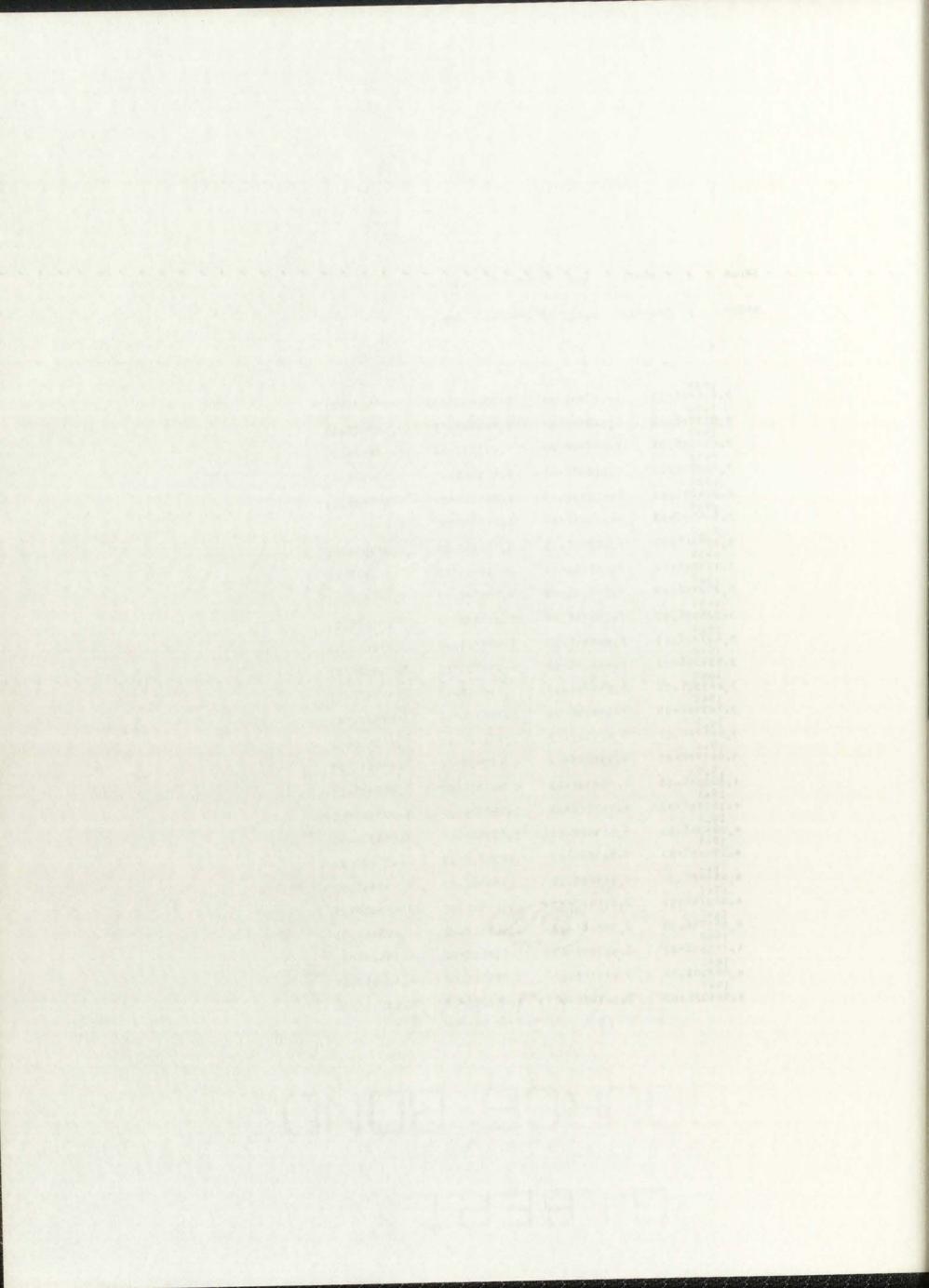
FOR

DECURA CODE

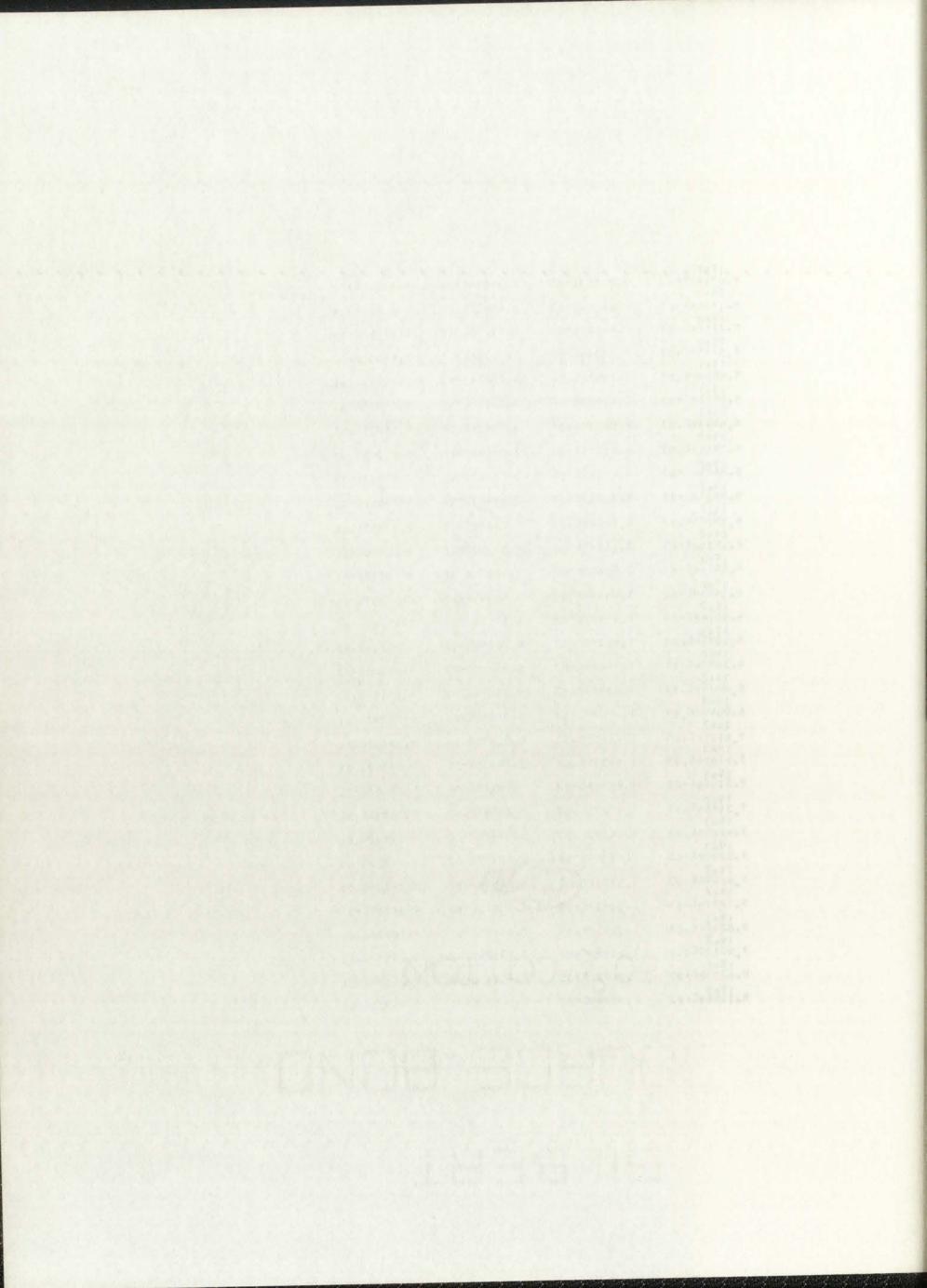


GROUP 1 CHANNEL 150 TO CHANNEL 1000
GROUP 2 CHANNEL 2200 TO CHANNEL 3050

X	Y	W	LIVE TIME
1938			
7.41582E+03	1.21760E+04	5.001658-03	6.09000E+01
2.51796E+03	1,14380E.04	5,45694E-03	6,24167E.01
7.62n1nE.03	1.06902E.04	6.01173E-03	6.42667E.01
2.72224E.03	1.01033E+04	6,47148E=U3	6,53833E.01
2.82438E.03	9.65371E.03	6.83157E-03	6.59500E+01
2.92652E+03	8.94121E+03	7.64438E-03	6.835n0E+01
3.02966E+03	8.49295E+03	8,15774E-03	6,92833E.01
3.13080E+03	8.00661E * 03	8.81980E-03	7.06167E+01
3.23294E.03	7,55426E+03	9.50677E-03	7,18167E.01
3.3350RE.03	7.18114E.03	1.00982E-02	7.25167E.01
3.43722E.03	6,80684E.03	1.08273E-02	7.370008.01
3.53936E+03	6.44414E+03	1.15893E-02	7.46833E+01
3,64150E.03	6.21878E.03	1,19664E-02	7.44167E.01
3.74364E+03	5.83070E+03	1.30831E-02	7.62833E+01
3.84578E.03	5,61632E.03	1,35112E=02	7,58833E.01
1.94792E . 03	5.33452E+03	1.44280E-02	7.69667E * 01
4.050068.03	5.02930E.03	1,56151E=02	7.85333E.01
4.15220E.03	4.78771E*03	1.65737E-02	7.93500E*01
4.25434E.03	4,545468.03	1.75963E-02	7.99833E.01
4.35648E+g3	4.36329E+03	1.83921E-02	8.02500E+01
4,45862E.03	4.14440E+03	1,96369E-02	8,13833E.01
4.56076E+g3	3.911926-03	2.11149E-02	8.26000E+01
4.66290E.03	3,798188.03	2,16551E-02	8.22500E.01
4.76504E+03'	3.612098+03	2.30614E-02	8.33000E+01
4.86718E.03	3,476198.03	2,39534E.02	8,32667E.01
4.96932E+03	3.303958+03	2.55149E-02	8-43000E+01



E . 07	146E+03	3.23043E+03	2.5786nE-U2	8 • 330n0E • 01
5.17	35nt • 03	J. n6146E + 03	2.76012E-02	8 • 45000E • 01
	474E . 03	2.89801E+03	2.97158E-02	8.61167E.01
	42 78RE+03	2.78304E+03	3.11351F-02	8,66500E+01
	002E.03	2.68422E.03	3.22689E-02	8.66167E,01
	476E+03	2.60488E.03	3.33157E-02	8.67833E.01
5,68	41 430E+03	2.50508E+03	3,45231E-02	8,64833E+01
	42 644E.03	2.427548.03	3.56465E-02	8.65333E.01
5.88	\$58E+03	2.29227E+03	3.87317E-02	8.87833E+01
5.99	692E+03	2.24599E+03	3.89583E-02	8+75000E+01
	286E.03	2.14780t.03	4.10342E-02	8,81333E.01
6.19	42 500E+03	2.089896+03	4.220326-02	8.82000E+01
	42 714E+03	2.00495E+03	4.43071E-02	8.88333E+01
5.39	42 928E+03	1.93959E+03	4.60063E-02	8.92333E+01
6.50	142E+03	1.89437E+03	4.67173E-02	8.85000E+01
6.60	356E.03	1.81319E • 03	4,97465E-02	9.02000E.01
5.70	1570E+03	1.77043E+03	5.07409E-02	8.98333E.01
6,80	784E+03	1,70462E+03	5,31594E-02	9.061678.01
6,90	1998E.03	1.67889E.03	5.34482E-02	8.97333E.01
7.01	143 1212E+03	1.61451E+03	5,61057E-02	9.05833E+01
7.11	426E.03	1.561998.03	5.79603E-02	9.05333E.01
	640E+03	1.525148*03	5.96119E-02	9.091678.01
	A54E.03	1.47191E.03	6,2390RE-02	9,18333E.01
7.42	068E.03	1.44193E.03	6.37226E-02	9.188335.01
7.5	282E+03	1.41364E+03	6.46793E-02	9 • 1 4 3 3 3 E + 0 1
7 6	2496E+03	1.37368E+03	6.67185E=02	9.16500E+01
7.77	710E+03	1.33404E+03	6.90511E=02	9.21167E+01
	43 974E.03	1.31159E.03	7.005518-02	9.18833E.01
7.9	138E.03	1,28425E+03	7.13126E-02	9,15833E.01
8.0:	347 3352E+03	1.247288+03	7.40949E-02	9.24167E.01
a.1	3586E+03	1.22080E+03	7.58791E-02	9.26333E+01



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H.44208E.03
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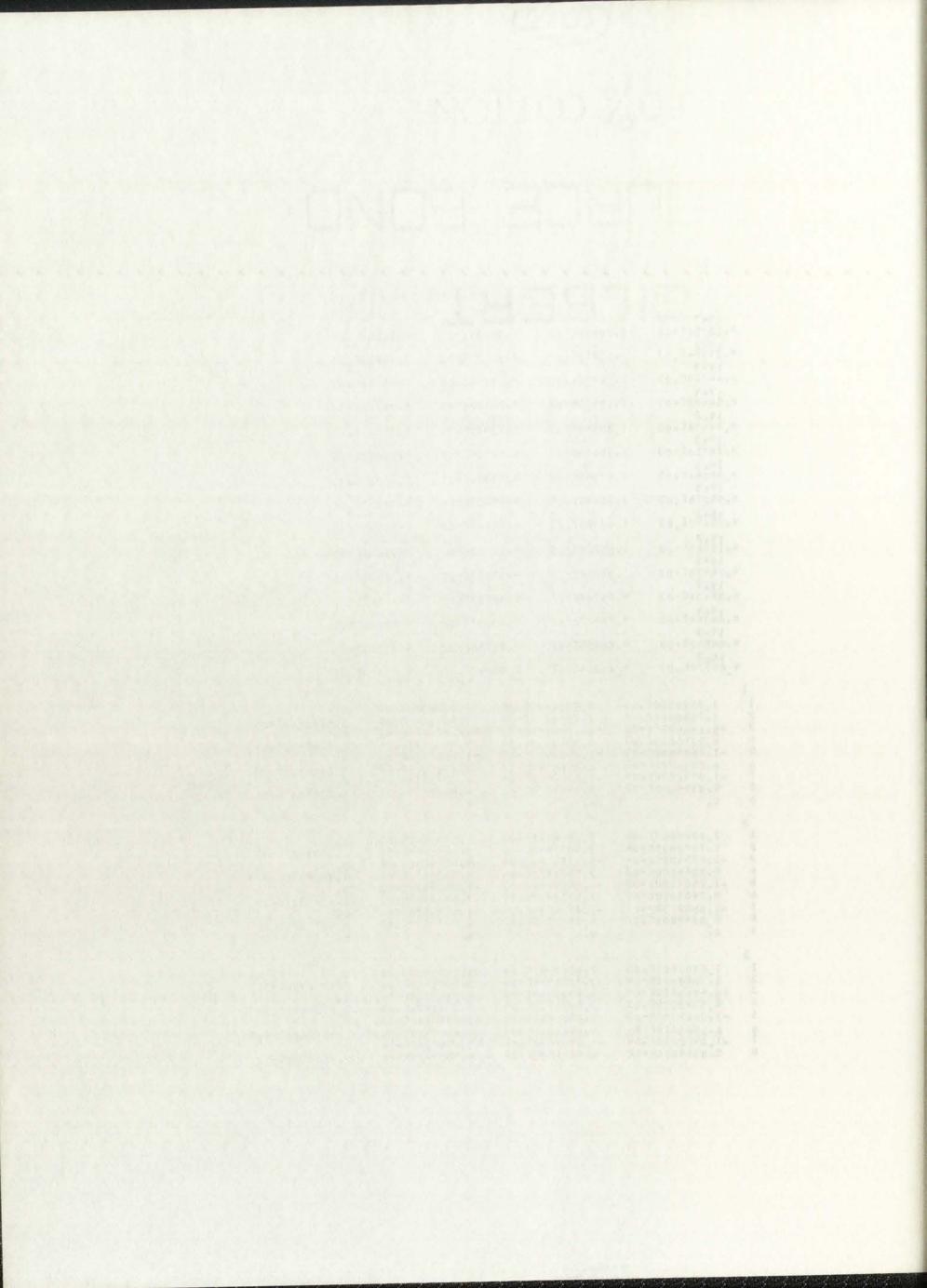
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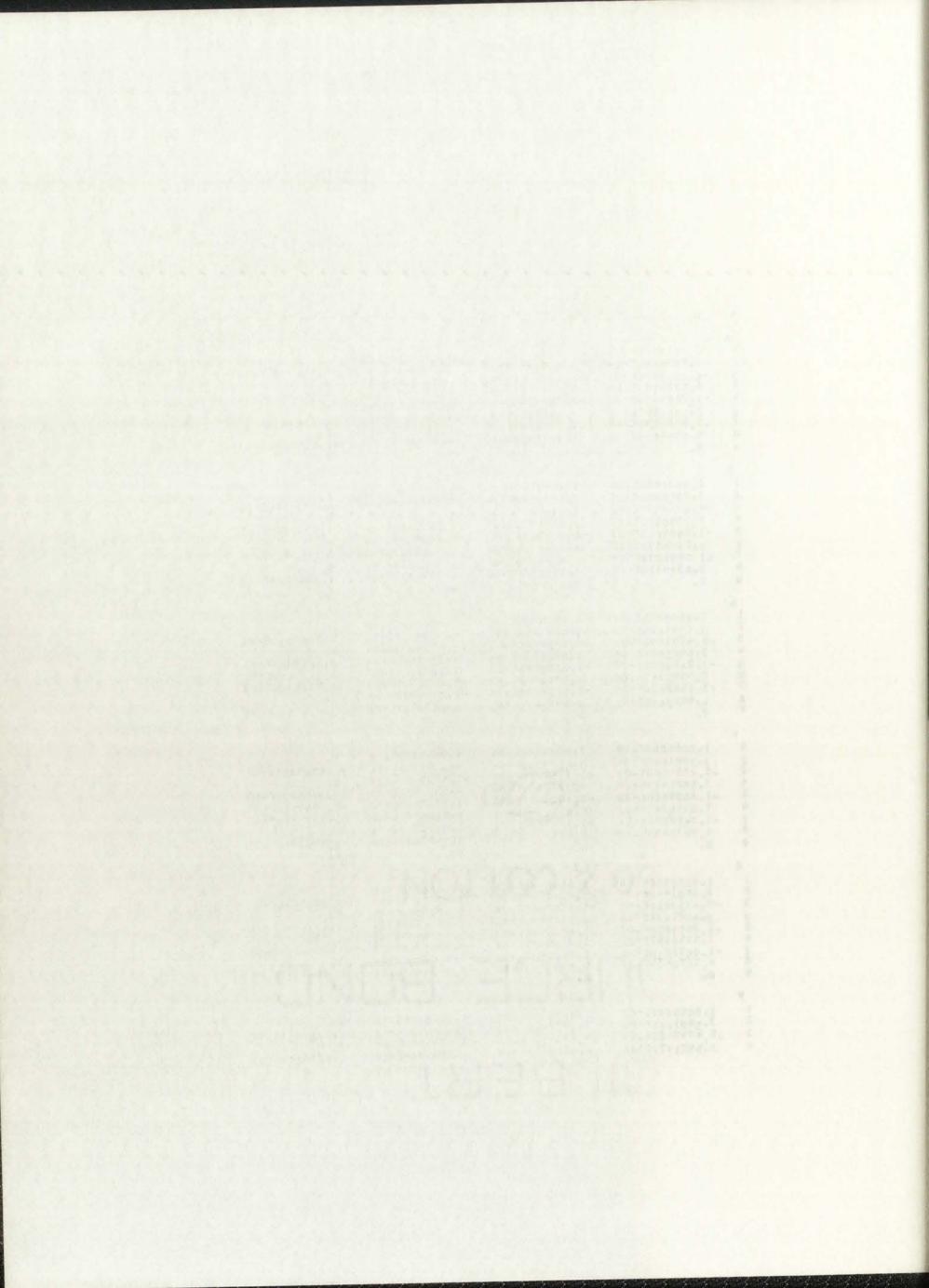
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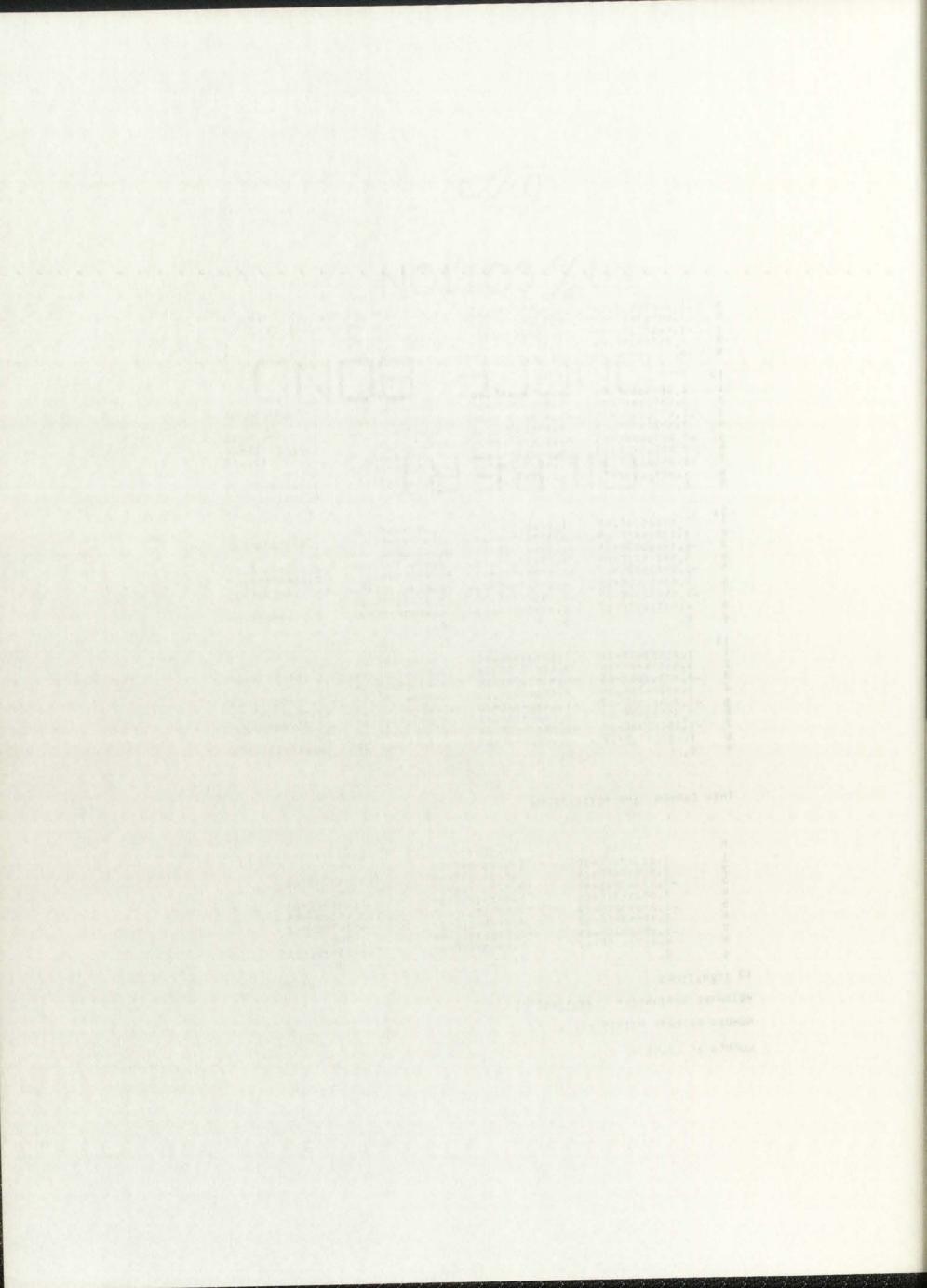
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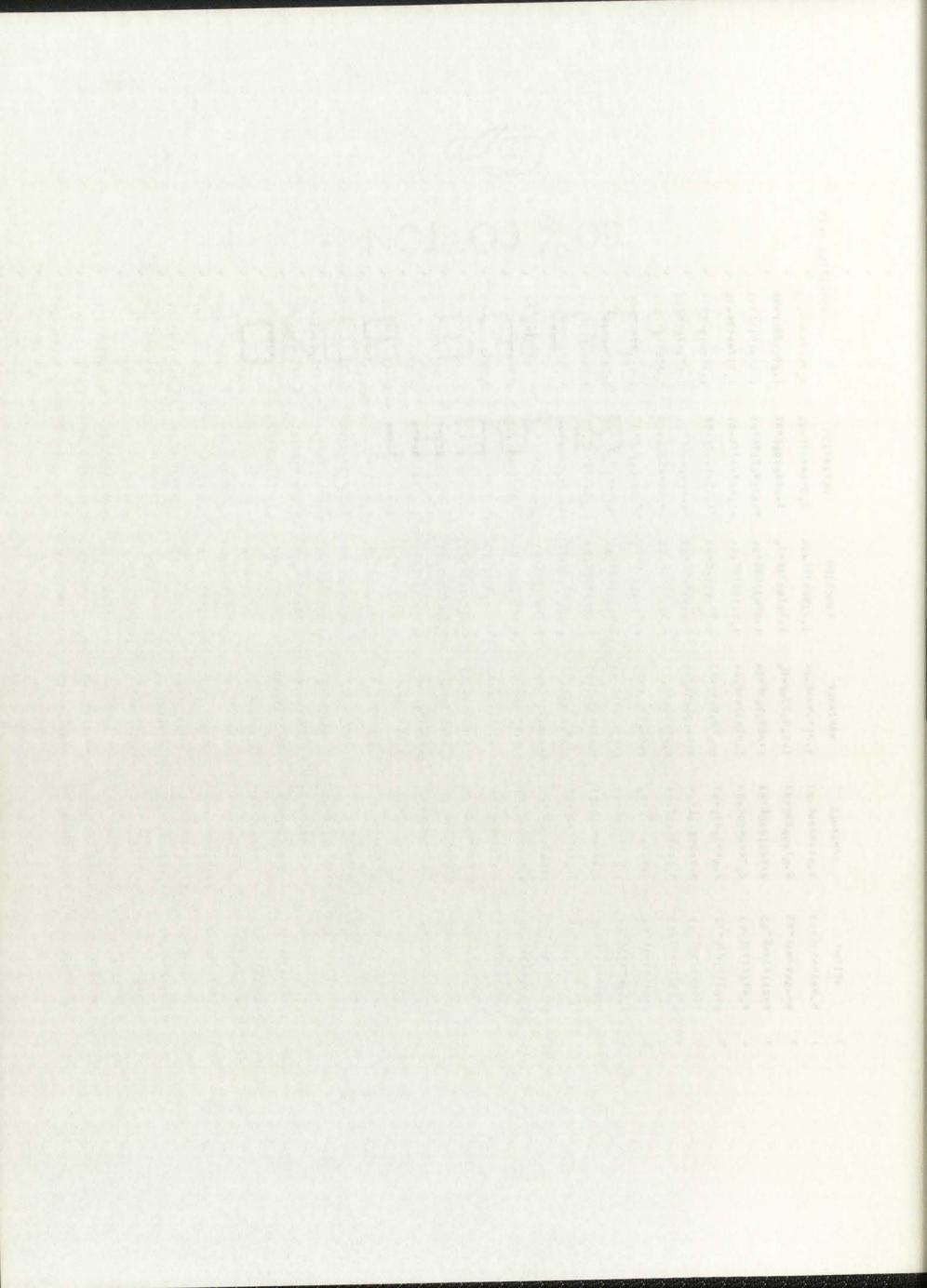
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-5.4759000E-04
3.5821471E+04
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13 ITERATIONS

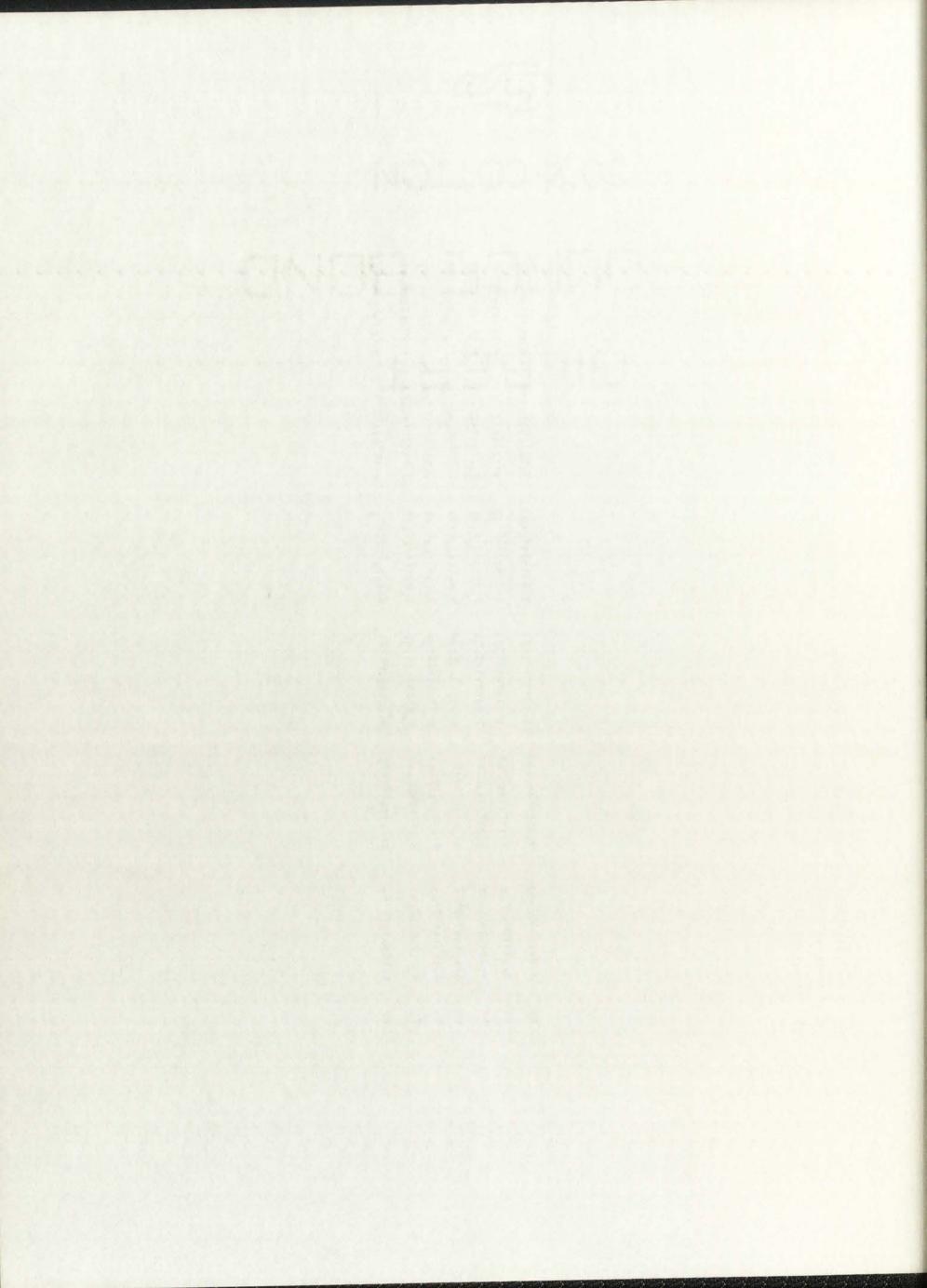
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NUMBER OF LINES = 4



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DEVIATION	2,35148H7E+01	1.8196796E.01	-5.3090718E.n1	-1,4270327E.01	1.1571772E.02	"5.9141419.6"	-8.0044532E+00	-2.9858676E.01	-4.9651727E*01	-1,9497833E.01	-1.7388502E.01	"2.8398793E.01	7,5151489E+01	-5.0414611E.00	6.9044203E*01	5,7721525E+01	6.3151119E.00	3.0536879E.00	.1,5255661E.01	1,3130116E+01	-7.6794664E*00	-5,3707718E+01	8.1251951E+00	"1.2534545E*01	7,4987363E.00	-1.7707965E+01	4.7477291E*01	9,3903891E.00	"3.0496936E*01	-2.8798462E.01	-1.7409741E.01	7.376ggggE.00
+ UNCTION	1,<152479£+04	1.14198388+04	1.0743298E+04	1,0117579E.04	9.5379896E+03	9.0003558E.03	8,5009561E.03	8.0364671E.03	7.6039149E.03	7,2006332E.03	6.82422705.03	6-4725407E-03	6,1436301E,03	5.8357384E.03	5.5472747E.03	5,2767956E,03	5.0229888E.03	4.7846590E+03	4,5607151E,03	4,3501596E+03	4.1520784E.03	3,9656327E,03	3.79005112.03	3.6246234E.03	3,4686942E,03	3,3216581E+03	3.18295496.03	3,0520652E,03	2.9285074E.03	2.8118337€.03	2,7016276E,03	2.5975011E+03
VAHIAHLE	1.217599 16.04	1.14380358.04	1.0690207F.04	1.0103309E.04	9.6537074E.03	A.9412143E.03	8,4929516E,03	8.0066084E.03	7.5542632E+03	7,1811354E,03	6.8668385E+03	6.44414198.03	6,2187816E,03	5.8306970E.03	5.6163189E.03	5,33451718,03	\$ .0293039E .03	4.7877127E.03	4,5454595E,03	4.3632897E.03	4.1443989E+03	3,9119249E.03	3.7981763E+03	3.5126888E.03	3,4761930E,03	3.3039502E+03	3.2304322E*03	3,06145568,03	2.898010gE+03	2.7830352E+03	2,68421785,03	2.604878nE+03
VAMIABLE	2,413H20UE+03	2.5 4 19600E.03	2.64J1000E.03	2,7622400E.03	2.8 243800E+03	2.9405200E*03	3,0<46600E+03	3.1398000E+03	3.2369400E+03	3,3350800E.03	3.4 \$ 12200E+63	3.5373600E+03	3,6415000E,03	3.7436400E+03	3.8457800E*03	3,9% (9200E.03	4.05,0600E+03	4.1542000E*03	4,2543400E,03	4.3564800E.03	4.4586200E+03	4,5007600E.03	4.6029000E+03	4.7650400E.03	4,80/1600E.03	4.90×3200E+03	5.0/14600E*03	5,1 (36000E,03	5.2/57400E.03	5.3/78800E.03 .	5,400200E+03	5.5 <sub>8</sub> 21600E+03
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#### APPENDIX B

# SURFACE AND VOLUMETRIC CONCENTRATIONS FROM CHARGED-PARTICLE ACTIVATION CODE

# Main Program SVCCPA

This code is written in FORTRAN IV for the CDC 6600 computer and calculates the surface concentration in g/cm<sup>2</sup> and the volumetric concentration in atoms/cm<sup>3</sup> for the passive <sup>3</sup>He activation analysis. Corrections are made for variations in the beam current during the irradiation.

The incident <sup>3</sup>He particles are followed in 0.01-MeV energy decrements into the sample as they are slowed by ionization energy losses.

The calculation is terminated once the <sup>3</sup>He energy reaches 1 MeV. This 1 MeV cutoff energy is arbitrary but satisfactory for the reactions being considered because the cross sections are negligible below this energy.

Calculation of the volumetric impurity concentration is as follows:

$$\frac{dE}{dX} = s(E)$$

$$\Delta X_{j} = X_{j+1} - X_{j} = \int_{E_{j}}^{E_{j+1}} \frac{dE}{s(E)}.$$

The integral,  $\int_{E_j}^{E_j+1} \frac{dE}{s(E)}$ , is determined from the numerical integration of the cubic spline interpolation function S(E), where S(E) = 1/s(E).

The average cross section for each energy step is determined from

$$\bar{\sigma}_{j} = \frac{\int_{E_{j+1}}^{E_{j}} \sigma(E) dE}{E_{j+1} - E_{j}},$$

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$$\int_{E_1}^{E_2} \sigma(E) dE$$

is determined by numerical integration of the analytical function used to represent  $\sigma(E)$ .

The concentration of impurity atoms,  $N_v$ , is

$$N_{\mathbf{v}} = \frac{R}{\Phi \cdot \sum \overline{\sigma}_{\mathbf{j}} \cdot \Delta X_{\mathbf{j}}},$$

where

 $N_v$  is the volumetric concentration of impurity atoms (atoms/cm<sup>3</sup>),

R is the total number of activation product atoms present,

 $\Phi$  is the number of incident  $^3$ He particles,

 $\bar{\sigma}_{i}$  is the average cross section for the jth energy step, and

 $\Delta X_{j}$  is the sample increment corresponding to the jth energy step.

A calculation is also made assuming that all of the impurity atoms are located in a thin layer on the surface of the material being irradiated. This calculation assumes that the energy loss of the  $^3$ He particles is small as they pass through this layer. The concentration of surface impurity atoms,  $N_{\rm g}$  (atoms/cm $^2$ ), is

$$N_{s} = \frac{R}{\Phi \cdot \sigma(E_{T})} ,$$

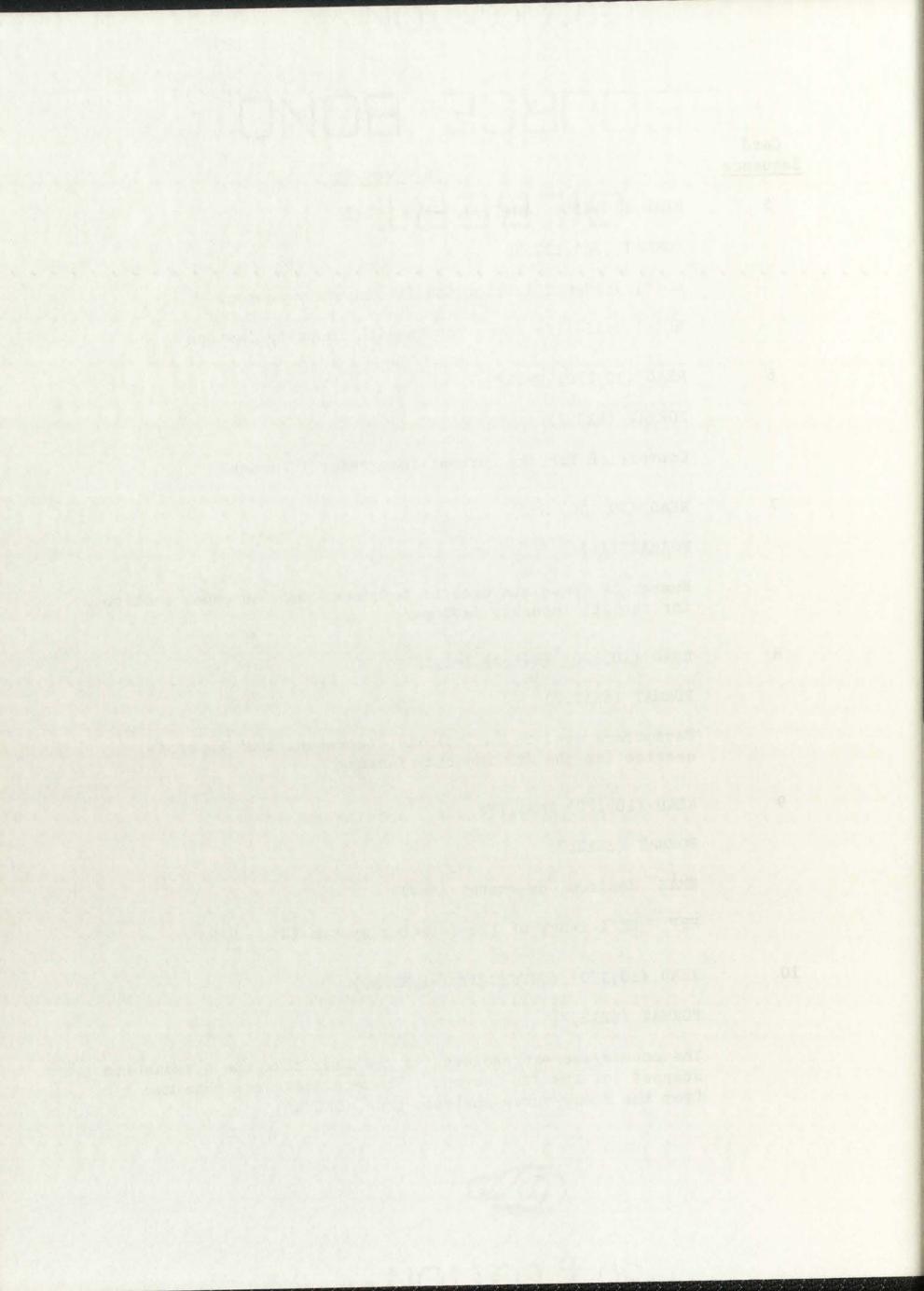
where  $\sigma(E_{\underline{I}})$  is the cross section corresponding to the incident  ${}^3\text{He}$  energy.

The current history of the target was recorded during the irradiations. This allowed corrections to be made for variations in the beam current during the run.

The following is a list of the input required. Most of the input is in the main program.

Card Sequence	Information
1	READ (10,125) (TIT(I),J=1,20)
	FORMAT (20A4)
	Title information 80 BCD characters
2	READ (10,65) (TIT(I), I=1,8)
	FORMAT (8A10)
	READ $(10,75)$ E(J),X(J),M(J)
	FORMAT (3E12.5)
	The CALL TFOX (XX,YY,0) statement in the main program is to enter the TFOX subroutine to read in the title and
	$1.0 / \frac{dE}{dX}$
	versus E data for the material being irradiated. A blank card terminates this sequence.
3	READ (10,135) ZOHRS, ZOMIN, ZOSEC
	FORMAT (3F6.0)
	Time of day that run stopped
	ZOHRS hour
	ZOMIN minutes
	ZOSEC seconds
4	READ (10,150) NOISO
	FORMAT (16)
	Number of impurity isotopes to be calculated: (<10)

Card Sequence	Information
5	READ (10,155) (AD(I,J),J=1,3),HL(I)
	FORMAT (3A4, E12.7)
	AD(I,J) Identification for Ith impurity isotope
	HL(I) Half-life (sec) for the Ith impurity isotope
6	READ (10,170) SMULT
	FORMAT (E12.7)
	Conversion for the current integrator (C/count)
7	READ (10,150) N(I)
	FORMAT (16)
	Number of Gaussians used to represent the <sup>3</sup> He cross section for the Ith impurity isotope
8	READ (10,170) (B(I,J), I=1,IK)
	FORMAT (6E12.7)
	Parameters used to analytically represent the <sup>3</sup> He cross section for the Jth impurity isotope
9	READ (10,170) EMAX, EFF
	FORMAT (2E12.7)
	EMAX Maximum <sup>3</sup> He energy (MeV)
	EFF Efficiency of the detector system (%)
10	READ (10,170) (CNTSEC(J), J=1, NOISO)
	FORMAT (6E12.7)
	The counts/sec extrapolated to the time that the irradiation stopped for the Jth isotope. These numbers are obtained from the decay curve analysis code (DECURA)



Card Sequence	Information
11	READ (10,170) (DECAYC(J), J=1, NOISO)
	FORMAT (6E12.7)
	Branching ratio for the positron decay (or energy being analyzed) for the Jth isotope
12	READ (10,185) IDATA, THR, TMIN, TSEC, TSTDLT
	FORMAT (16,4F6.0)
	This is the start of the current integrator history
	IDATA Number of data points in the data set that follows
	THR, TMIN, and TSEC Time of day for the first data point
	TSTDLT Time between integrator dumps (sec)
13	READ (10,180) (INC(I), I=1, IDATA)
	FORMAT (4X,1614)
	Current integrator data (counts)

Card sequences 12 and 13 are repeated if more than one set of current integrator data is used. A blank card designates the end of the current integrator data.

The more important variables in the main program are listed in Table 16.

## Function GFN (A,C,D,E)

This function calculates the number of activation product atoms that were present when the irradiation stopped from those that were born during some current integrator interval.

- A Average <sup>3</sup>He current during the interval (particles/sec)
- B Decay constant (sec 1)

### TABLE 16

### MAIN PROGRAM SVCCPA VARIABLES

	MAIN PROGRAM SVCCPA VARIABLES
AD(I,J)	identification for the Ith impurity isotope
ATOMS(I)	volumetric concentration of the Ith impurity in (atoms/cm <sup>3</sup> )
B(J,I)	Jth parameter for the analytical representation of the Ith $^3\mathrm{He}$ cross section
CNTSEC(I)	counts/sec extrapolated to the time the irradiation stopped for the Ith impurity
DECAYC(I)	branching ratio for the positron decay of the activation product from the Ith impurity
DELTT	time (sec) between current integrator dumps
EFF	detector efficiency (%)
EMAX	energy (MeV) of the incident <sup>3</sup> He ions
HL(I)	half-life (sec) of the activation product from the Ith impurity
ICASE	flag that is used to indicate whether or not the E and X data have been read into the memory
IDATA	number of current integrator dumps in the data set that follows
INC(I)	current integrator history data
LAM(I)	decay constant ( $\sec^{-1}$ ) for the reaction product from the Ith impurity
NG(I)	number of Gaussians used for the analytical representation of $^3\mathrm{He}$ cross section for the Ith impurity
NOISO	number of impurities to be calculated
Q	average $^3\mathrm{He}$ flux (particles/sec) striking the target during a current integrator dump
SIGBAR	average <sup>3</sup> He cross section over the energy interval being calculated
SIGDX(I)	average cross section of the irradiated sample volume for the Ith impurity
SMULT	conversion factor for the current integrator (C/count)

SUCAN cross section for the surface layer

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# TABLE 16 - continued

SURF	concentration of the surface layer (atoms/cm2)
TIT(I)	identification information
THR, TMIN, TSEC	time of day for the first integrator dump in the set of data that follows
TSTDLT	time between current integrator dumps (sec) for the set of data that follows
TZ	elapsed time (sec) from a current integrator data point to the end of the irradiation
W(I)	weights for the Gaussian-type numerical integration
X(I)	interval for the Gaussian-type numerical integration
ZION	electronic charge of the incident ion
ZOHRS, ZOMIN, ZOSEC	time of day when the irradiation stopped. For each midnight that was passed during the run, 24.0 should be added to ZOHRS

- D Time (sec) between current integrator dumps
- E Elapsed time (sec) from the dump until the irradiation stopped.

### Subroutine FSIGE

This subroutine is used to evaluate the parameters for the analytical representations of the <sup>3</sup>He cross sections. The analytical representation consists of Gaussians with exponential tails on the high-energy side of the Gaussian. These parameters are determined using least-squares techniques and the code GHLET (see Appendix C).

The arguments in the subroutine call statement are:

- X 3He energy MeV,
- YT Cross section (mb), and
- IZ Index of the cross section to be calculated.

#### Subroutine TFOX

This subroutine solves the cubic spline interpolation function y = S(E), where  $S(E) = 1.0 \frac{dE}{dX}$ . The data are usually stored from E = 1.0 to E = 12.0 MeV.

The arguments in the subroutine call statement and more important variables are:

- ZZ 3He energy (MeV),
- YY Reciprocal of the stopping power (cm/MeV),
- L Data input flag,
- E(J) Energy of the Jth data point (MeV),
- X(J) Reciprocal of the stopping power for the Jth data point (cm/MeV),
- M(J) Second derivative at the Jth data point,
- TIT(I) Title information for above data, and
  - NPTS Number of data points.

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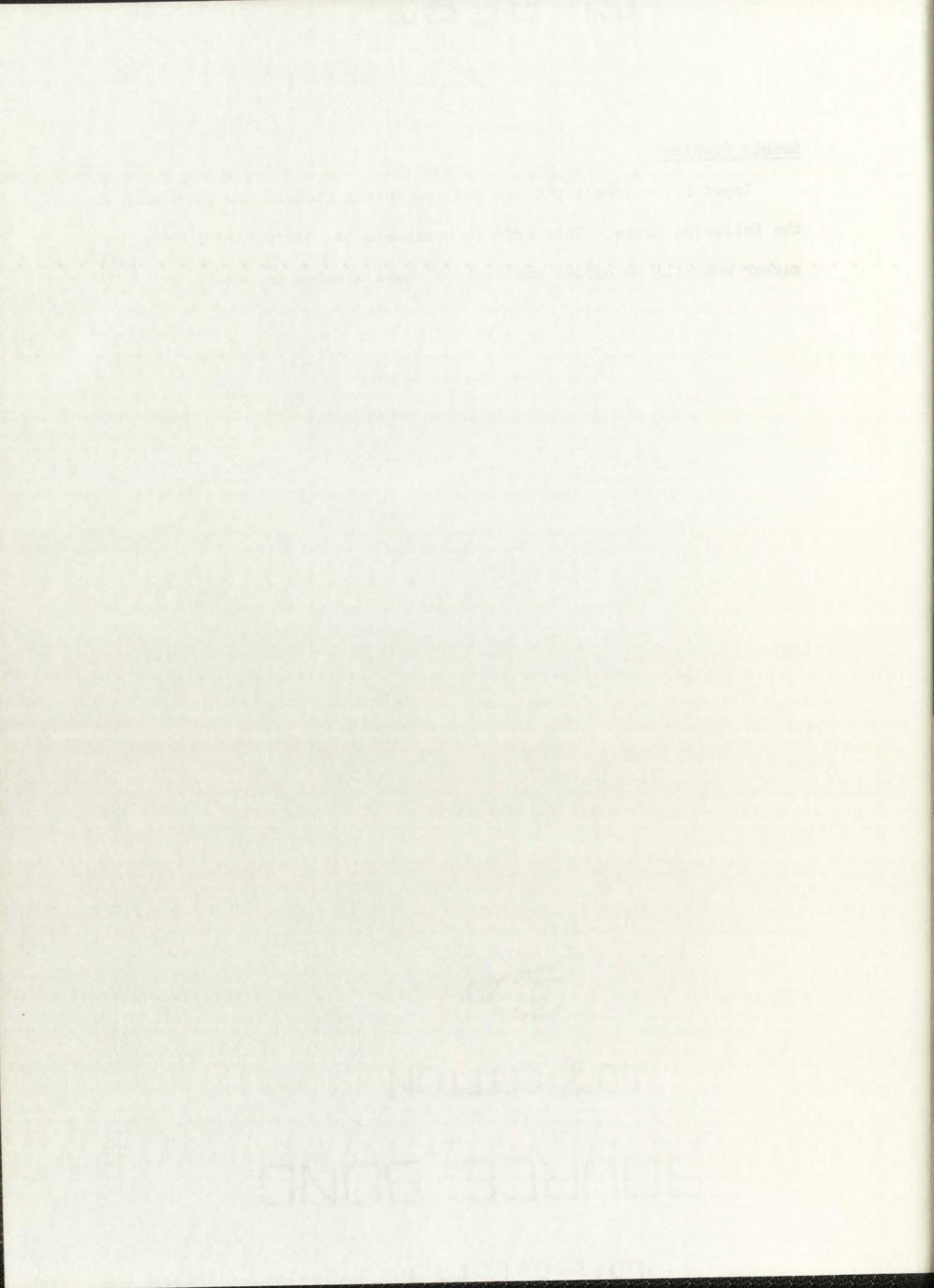
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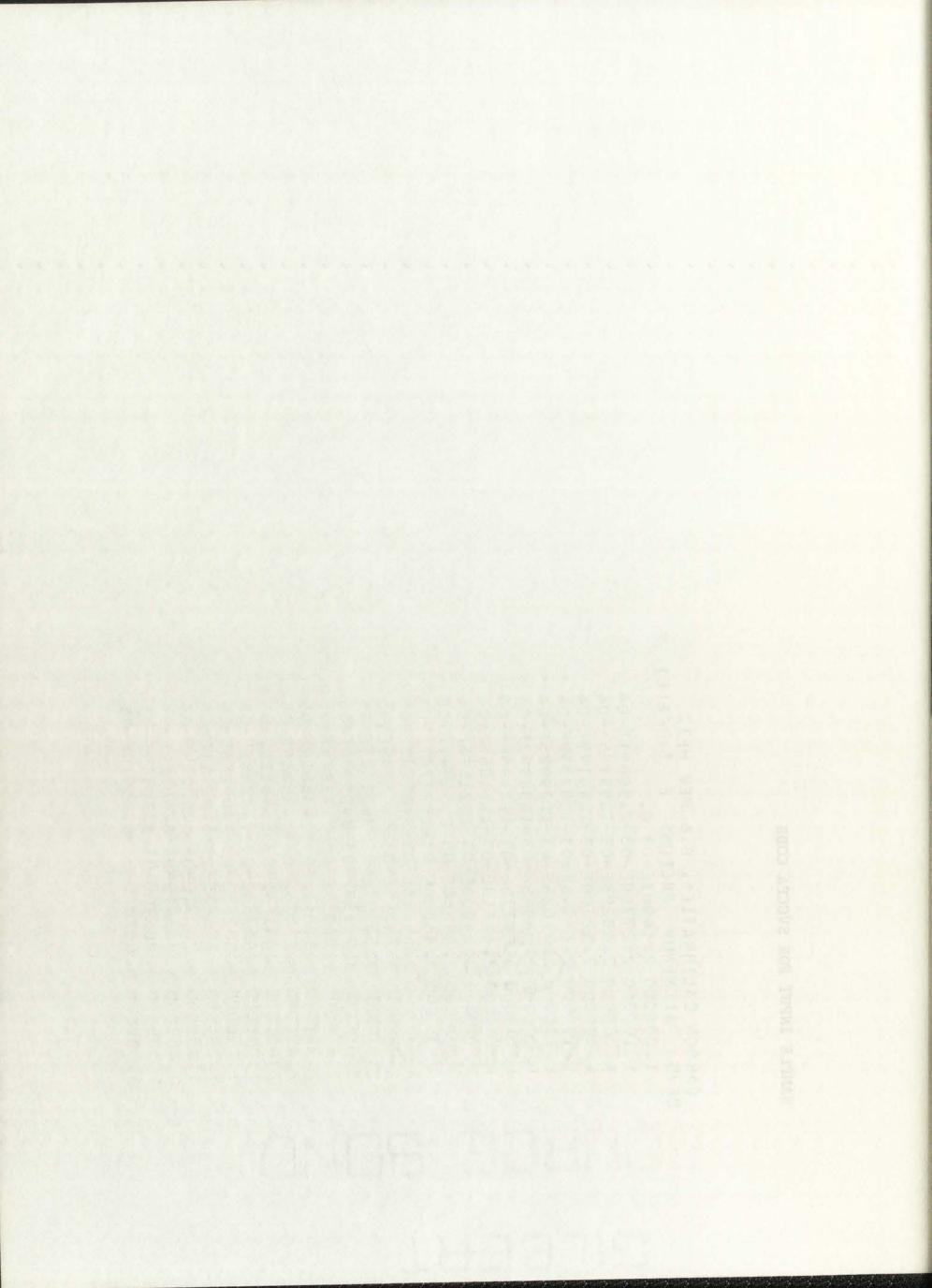
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# Sample Problem

Input for a sample problem and the output from it are presented on the following pages. This code is available for distribution from the author and will be copied and sent to those wishing to use it.



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                                                      2.27700E-03-2.50691E-04
                                                                       2.40298E-03-1.95105E-04
                                                                                          2.52700E-03-1.40199E-04
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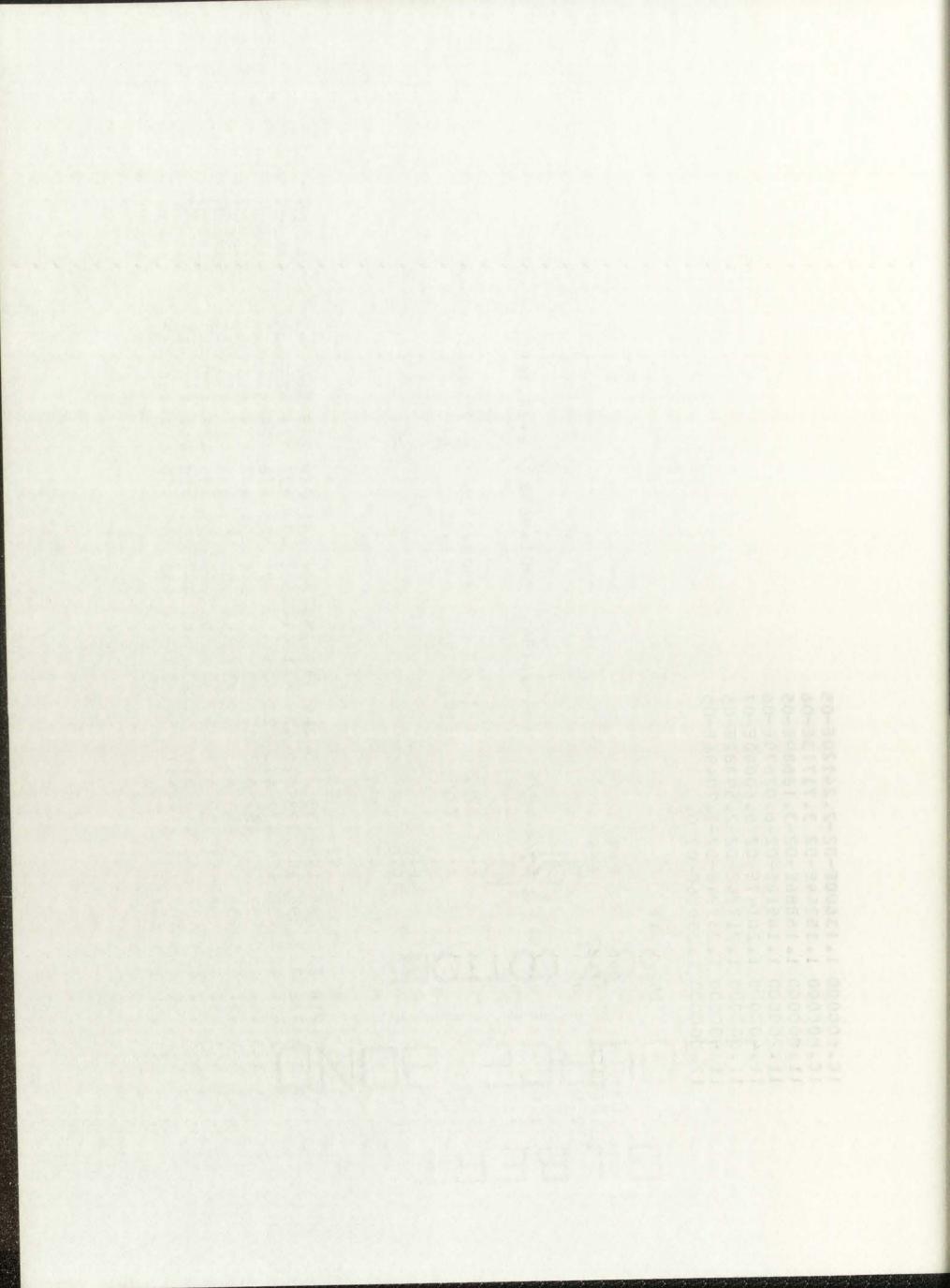
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5.26981E-03-3.78246E-05
                                    5.37009E-03-6.57015E-05
5.16907E-03-5.25549E-05
                                                      5.46981E-03-4.14416E-05
                                                                        5.66785E-03-5.23306E-05
                                                                                           5.86397E-03-3.58682E-05
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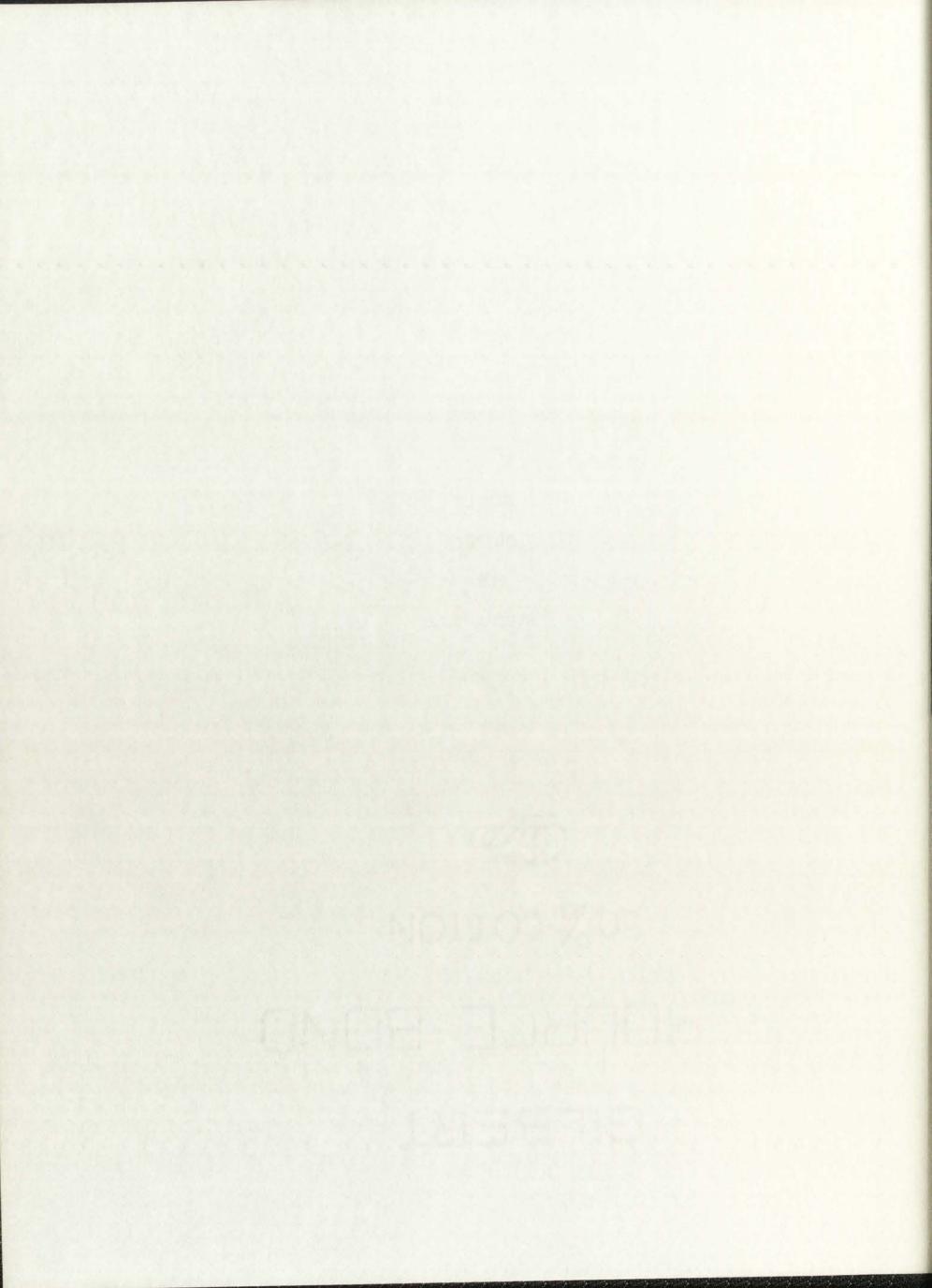


SAMPLE

OUTPUT

FOR

SVCCPA CODE



CAMBON CALIBRATIONS B.O MEV MES.

UE/DX ALUMINUM PROTONS E 1.0/F(E) M
RUN STOPPED AT 6 MRS 15 MIN 37 SEC

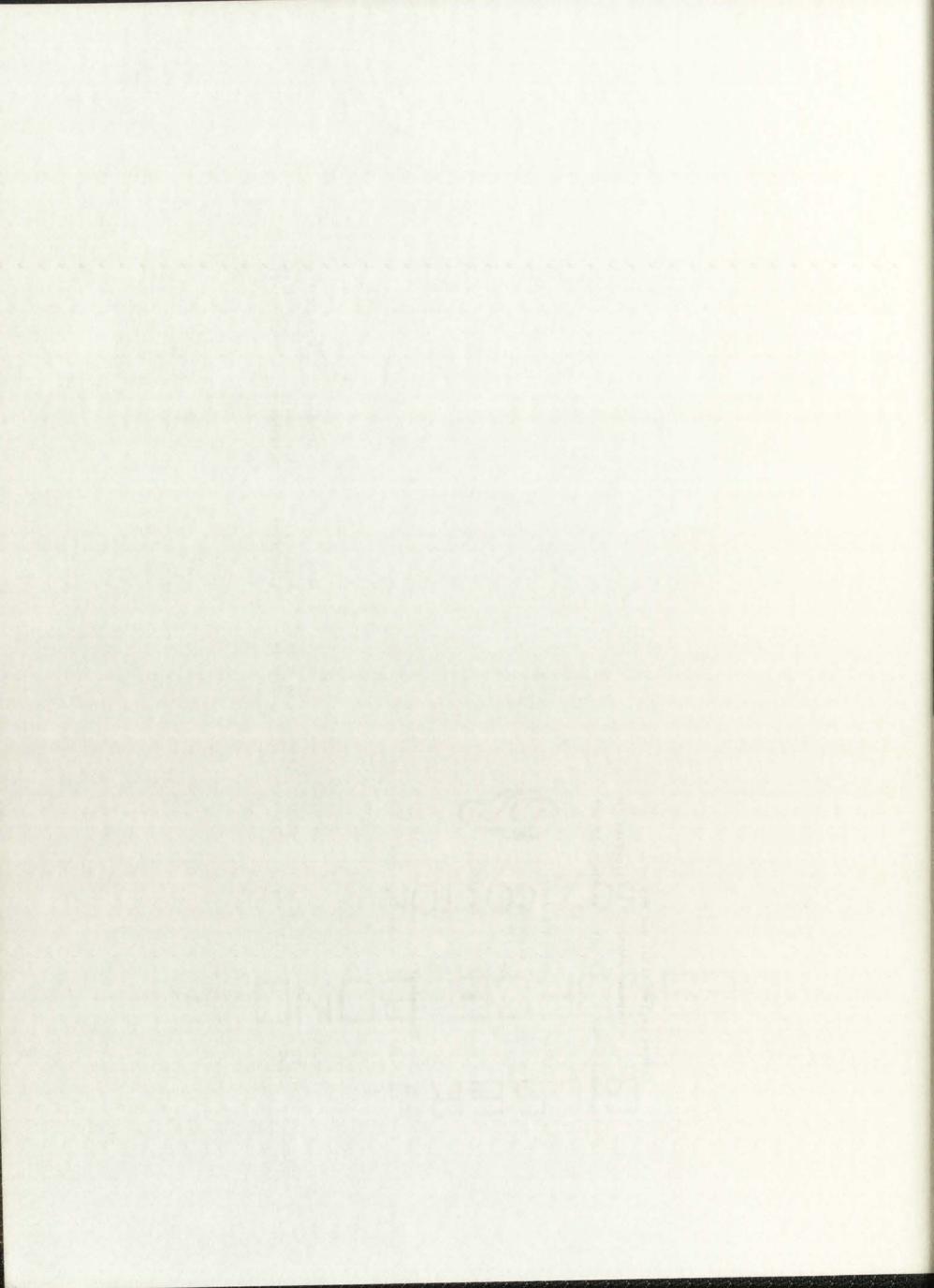
ISOTOPE MALF-LIFE (SEC)

CARGEN 6.6000E.03

CLICK MULTIPLIER = 2,0000F-09

MAXIMUM ION ENEMGY & H.60 COUNTING EFFICIENCY & 99,3HPERCENT

ATOMS/CH#2	7.6254E+16
ATOMS/CC	4.2348F.17 3.4237F.18
DECAY CORR.	1.0000E+00 1.0000E+00
SUM	3.4913E+14 2.6235E+16
SIGDA	6.0917F.01 7.6933E.01
CNT/SEC	9.4000E+02
ISOTOPE	DXYGEN



#### APPENDIX C

#### GAUSSIAN WITH HIGH AND LOW EXPONENTIAL TAILS FIT CODE

### Main Program GHLET

This program, written in FORTRAN IV for the 6600 computer, is similar to the DECURA code discussed in Appendix A and also to the computer code discussed in Ref. 25. The code does a least-squares fit of a Gaussian with high-energy and low-energy exponential tails. In addition to the analytical representation of the total <sup>3</sup>He cross sections used in this experiment, the code has been quite useful in the analysis of neutron cross-section data in the resonance region (Ref. 42).

The main program is quite simple and is used only to call subroutines. Subroutine DINSET reads the data into memory and sets up the initial values for the parameters. Subroutine MAZCS is the least-squares portion of the code. Subroutine OUTCS is the output portion of the code, and the PLTZ subroutine plots the data using the SC 4020.

Subroutines in the code that are identical to those mentioned elsewhere in this report will not be discussed.

#### Subroutine DATA

The data that is to be fitted is read into the computer by this code. The input cards read by this subroutine are:

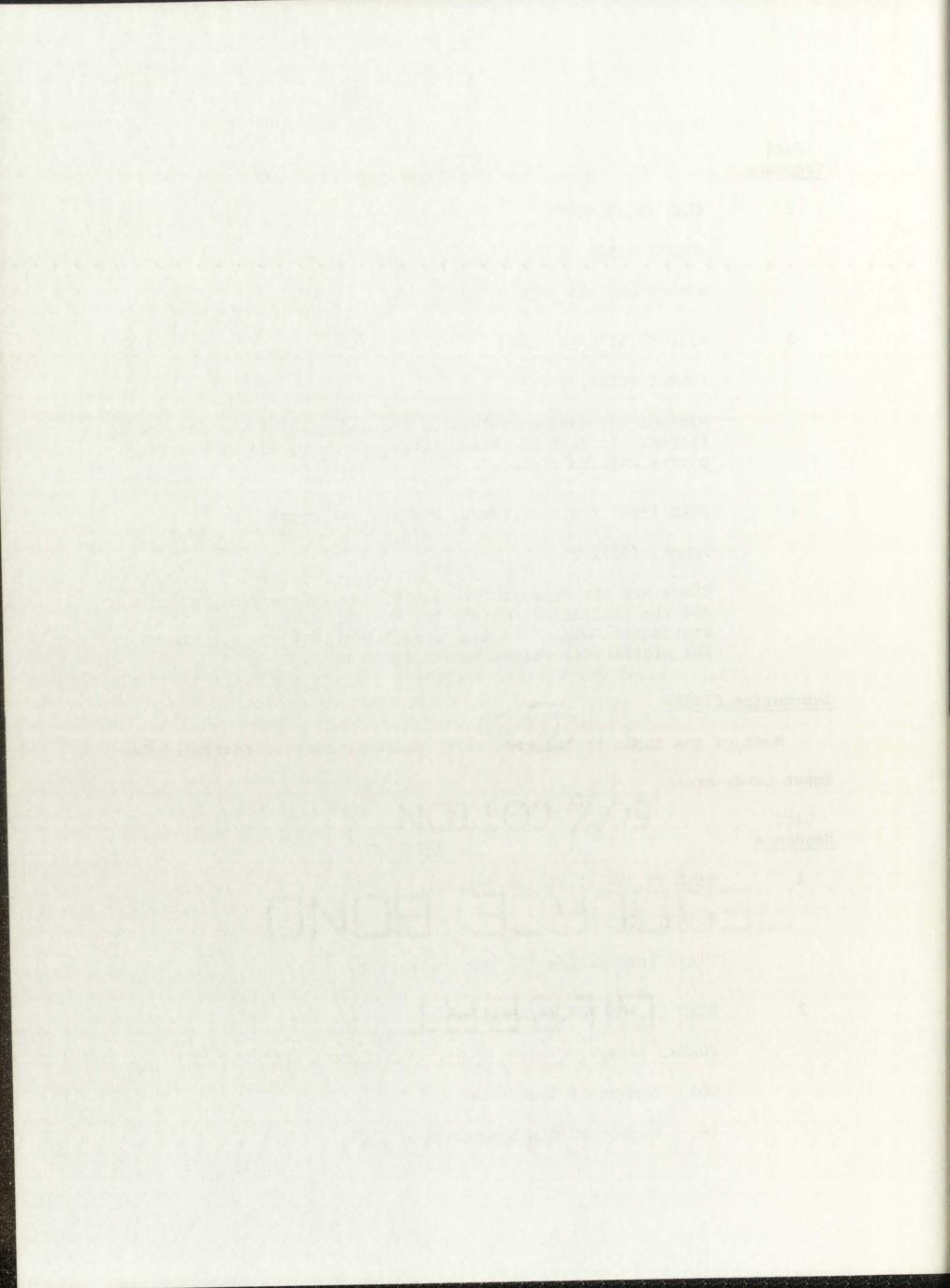
Card Sequence	Information
1	READ (5,1) (TITLE(J), J=1,8)
	FORMAT (8A10)
	Title information (80 BCD characters)

Card Sequence	Information
2	READ (5,3) NODP
	FORMAT (16)
	Number of data points
3	READ (5,4) XMIN, XMAX
	FORMAT (2E12.7)
	Minimum and maximum values of the independent variable to be fitted. If both of these values are zero, all of the data points will be fitted.
4	READ (5,4) ((XIN(I),YIN(I),WIN(I)),I=1,NODP)
	FORMAT (3E12.7)
	These are the dependent variable, the independent variable, and the statistical weight for the Ith data point. If the statistical weight is less than 1.0 x $10^{-10}$ (e.g., blank), the statistical weight is set equal to 1.0.

# Subroutine DINSET

Most of the input to the code takes place in this subroutine. The input cards are:

Card Sequence	Information
1	READ (5,35) (TITLE(J),J=1,20)
	FORMAT (20A4)
	Title information (80 BCD characters)
2	READ (5,40) NOI, IM, IPR, LLEH
	FORMAT (413)
	NOI Number of Gaussians
	IM Number of fixed parameters



Card Sequence	Information
2 (cont.)	<pre>IPR List control flag = 0 list of each iteration # 0 list only final results</pre>
	LLEH Plot control flag = 1 read input card for plot parameters  # 1 code generates plot parameters
3	READ (5,40) (IX(I), I=1, IM)
	FORMAT (1813)
	Indexes of fixed parameters
4	READ (5,45) (PG(I), I=1,7)
	FORMAT (6E12.7)
	The first seven parameters
	PG(1) standard deviation of the Gaussian
	PG(2) amplitude of the flat tail on the high-energy side of the Gaussian
	PG(3) amplitude of the sloped tail on the high-energy side of the Gaussian
	PG(4) slope for above exponential tail
	PG(5) amplitude of the flat tail on the low-energy side of the Gaussian
	PG(6) amplitude of the sloped tail on the low-energy side of the Gaussian
	PG(7) slope for the above exponential tail
5	READ (5,45) (PG(I), I=8, IA)
	FORMAT (6E12.7)
	Areas of the Gaussians
6	READ (5,45) (PG(I), I=IA, IB)
	FORMAT (6E12.7)
	Mean energies of the Gaussians

Card Sequence	Information
7	READ (5,45) PG(IK)
	FORMAT (E12.7)
	Rate of convergence of the exponential tails under the Gaussians
8	READ (5,30) (A(I),I=1,16)
	A(1) through A(8) label for the vertical plot axis
	A(9) through A(16) label for the horizontal plot axis
9	CALL DATA (X,Y,W,NODP)
	See previous section on DATA subroutine

### Subroutine MAZCS

This subroutine is similar to the MAZGN subroutine discussed in Appendix A. The variables are generally the same, with the exception being the bounds and restrictions on the parameters to insure convergence.

One of two corrective actions is taken if a parameter tries to change sign during an iteration. Parameters 1, 4, 7, and the mean energies are fixed at their initial values, and all parameters are reinitialized if one of them tries to change sign. The just-calculated value for the parameter PC(I) is set to P(I)/2.0 if parameters 2, 3, 5, 6, or the Gaussian areas try to change sign. For the latter case, the sign checks are then continued.

The bounds on the parameters and the corrective action taken if a bound is violated are listed in Table 17.

TABLE 17
BOUNDS ON PARAMETERS MAZCS

Parameter	Bound	Corrective Action
1	None	
2	>1.0 x 10 <sup>-4</sup>	Fixed at initial value All parameters reinitialized
3	>1.0 x 10 <sup>-4</sup>	Same as 2
4	None	
5	Same as 2	Same as 2
6	Same as 2	Same as 2
7	None	
Areas	>X(N)/10000.0	Fixed at lower bound Checks continued
Energies	<x(n) &="">X(1)</x(n)>	Same as 2

## Subroutine OUTCS

Most of the output is generated by this subroutine. The initial value, best least-squares value, and the standard deviation associated with the fitted value are listed. In addition, the integrals under each of the sloped exponential tails are numerically determined. The sum of the Gaussian area and the two exponential tail areas associated with it are summed and listed. In many applications, this total area is more nearly the area of interest. The sum of the zero slope exponential tails on the low-energy side of all the Gaussians is calculated and also the corresponding sum on the high-energy side of Gaussians. The values are listed as the low-energy background and the high-energy background.

### Subroutine PLTZ

This subroutine is quite similar to the PLOTGN subroutine listed and discussed in Appendix A.

#### Subroutine SITRE

The numerical integration that is used to determine the integral under the exponential tails is performed by this code. It assumes that 100 evenly spaced values for the dependent variable are stored as Y(I) and that X1 and X2 are the independent variables corresponding to Y(1) and Y(100). The cubic spline interpolation function is calculated, and the integral of this function between X1 and X2 is determined. The value of the integral is stored as SX in COMMON/LIMBO/. The cubic spline is discussed in Appendix E.

#### Subroutine YP

The variables in this subroutine are similar to the variables in the YP subroutine discussed in Appendix A. The function that is being fitted to the data, however, is quite different. The analytical function and its parameters are

$$Y(J) = \sum_{I=1}^{NOI} G(I,J) + HT(I,J) + LT(I,J)$$
,

where NOI is the number of Gaussians in the energy region being analyzed. The J subscript refers to the Jth data point, and the I subscript refers to the Ith resonance. The Gaussian contribution to the function is

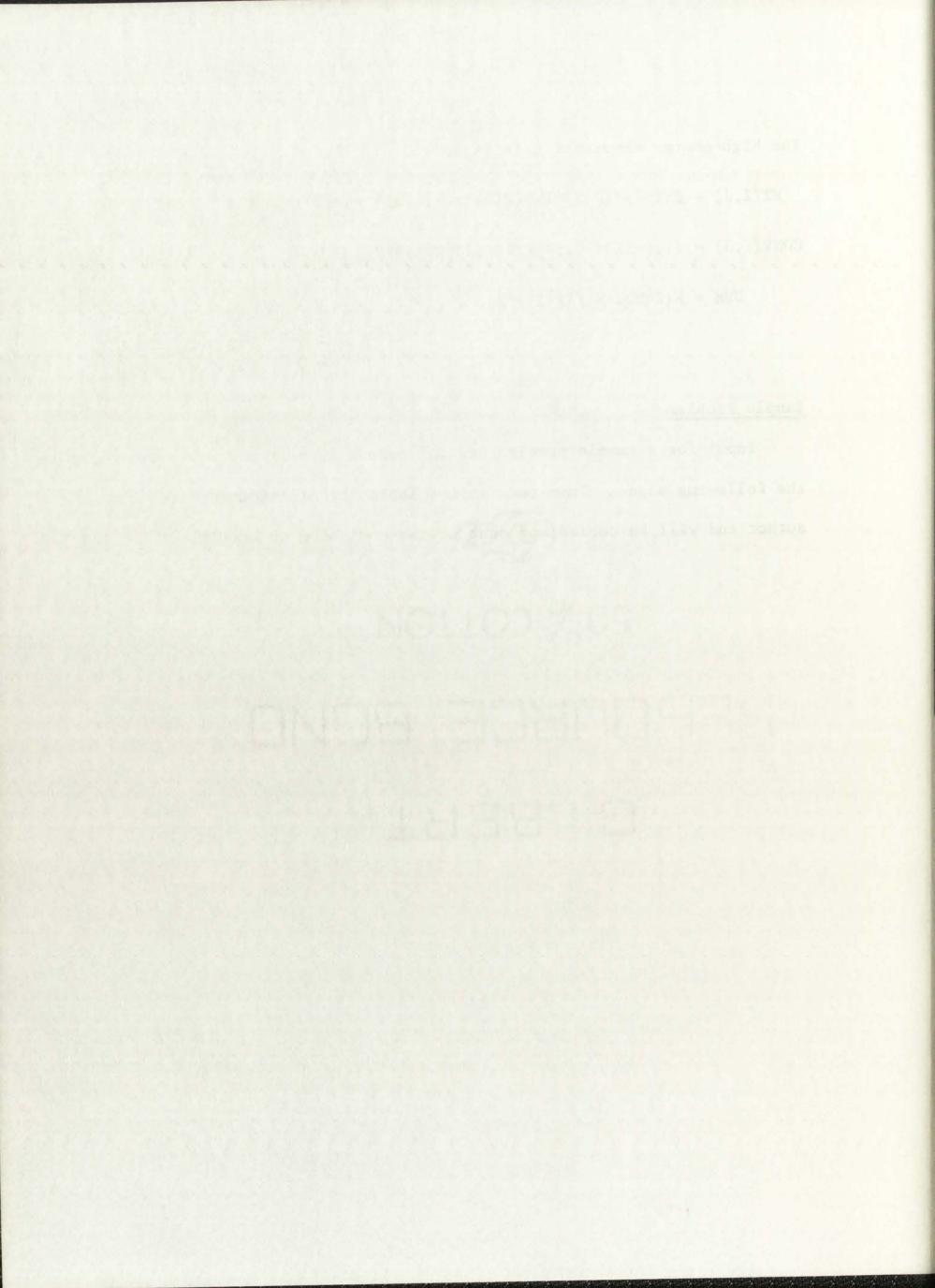
$$G(I,J) = P(I+7)*EXP(0.5*(PEP(I,J)/P(1))**2)/(0.39894*P(1))$$
  
 $PEP(I,J) = X(J)-P(I+NOI+7)$ 

The high-energy exponential tails are

$$\begin{aligned} \text{HT}(\mathbf{I},\mathbf{J}) &= \text{P}(\mathbf{I}+7)*(\text{P}(3)*\text{EXP}(\text{P}(4)*\text{PEP}(\mathbf{I},\mathbf{J})) + \text{P}(2))*\text{CONV}(\mathbf{I},\mathbf{J})*\delta(\mathbf{I},\mathbf{J}) \\ \text{CONV}(\mathbf{I},\mathbf{J}) &= (1.0-\text{EXP}(-0.5*(\text{PEP}(\mathbf{I},\mathbf{J})*\text{DUM})**2)) \\ \\ \text{DUM} &= \text{P}(2*\text{NOI}+8)/(\text{P}(1)**2) \quad , \\ \\ \delta(\mathbf{I},\mathbf{J}) &= 1 \quad \text{PEP}(\mathbf{I},\mathbf{J}) < 0.0 \\ &= 0 \quad \text{PEP}(\mathbf{I},\mathbf{J}) > 0.0 \end{aligned}$$

# Sample Problem

Input for a sample problem and the output from it are presented on the following pages. This code is available for distribution from the author and will be copied and sent to those wishing to use it.

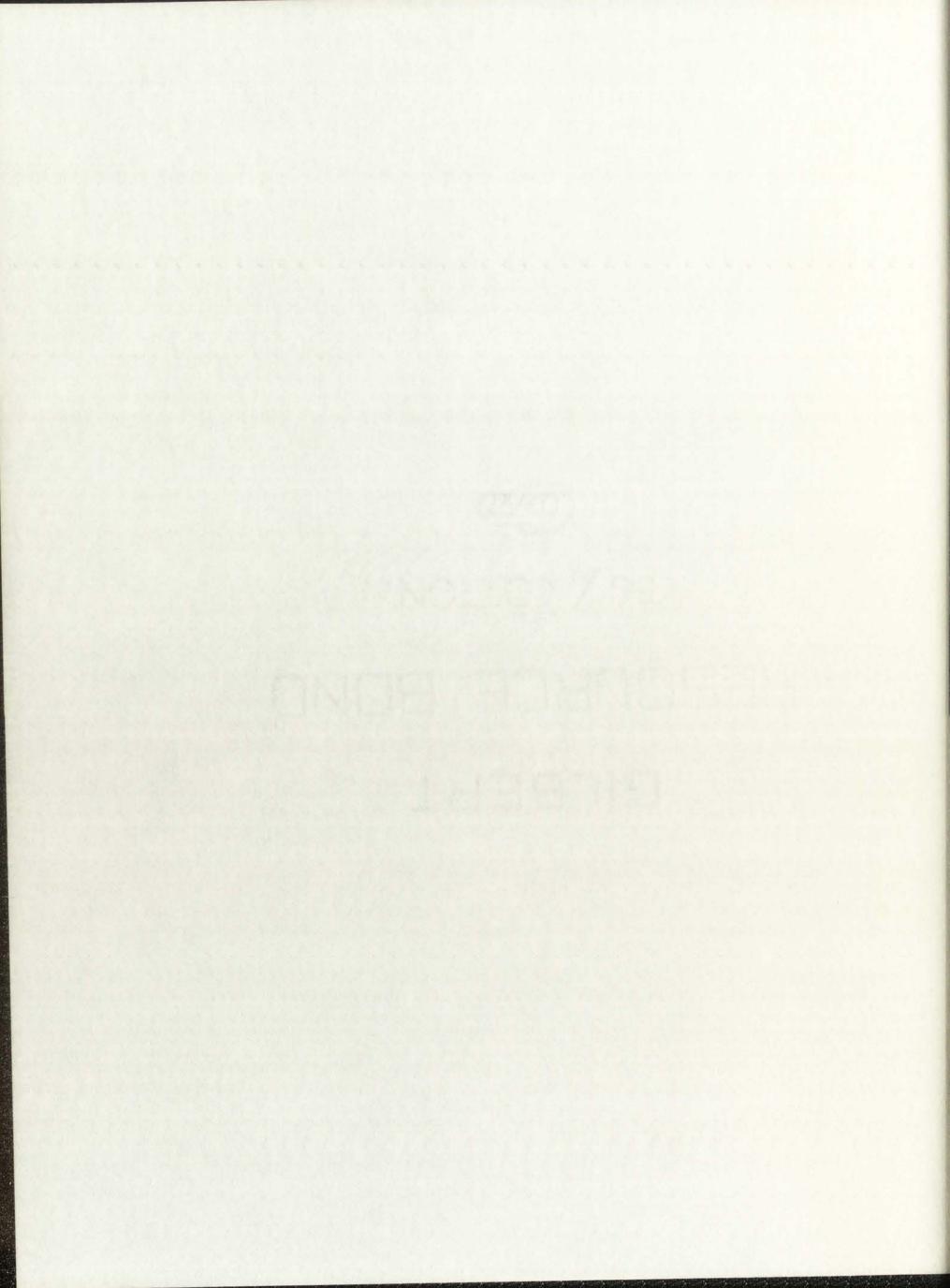


SAMPLE

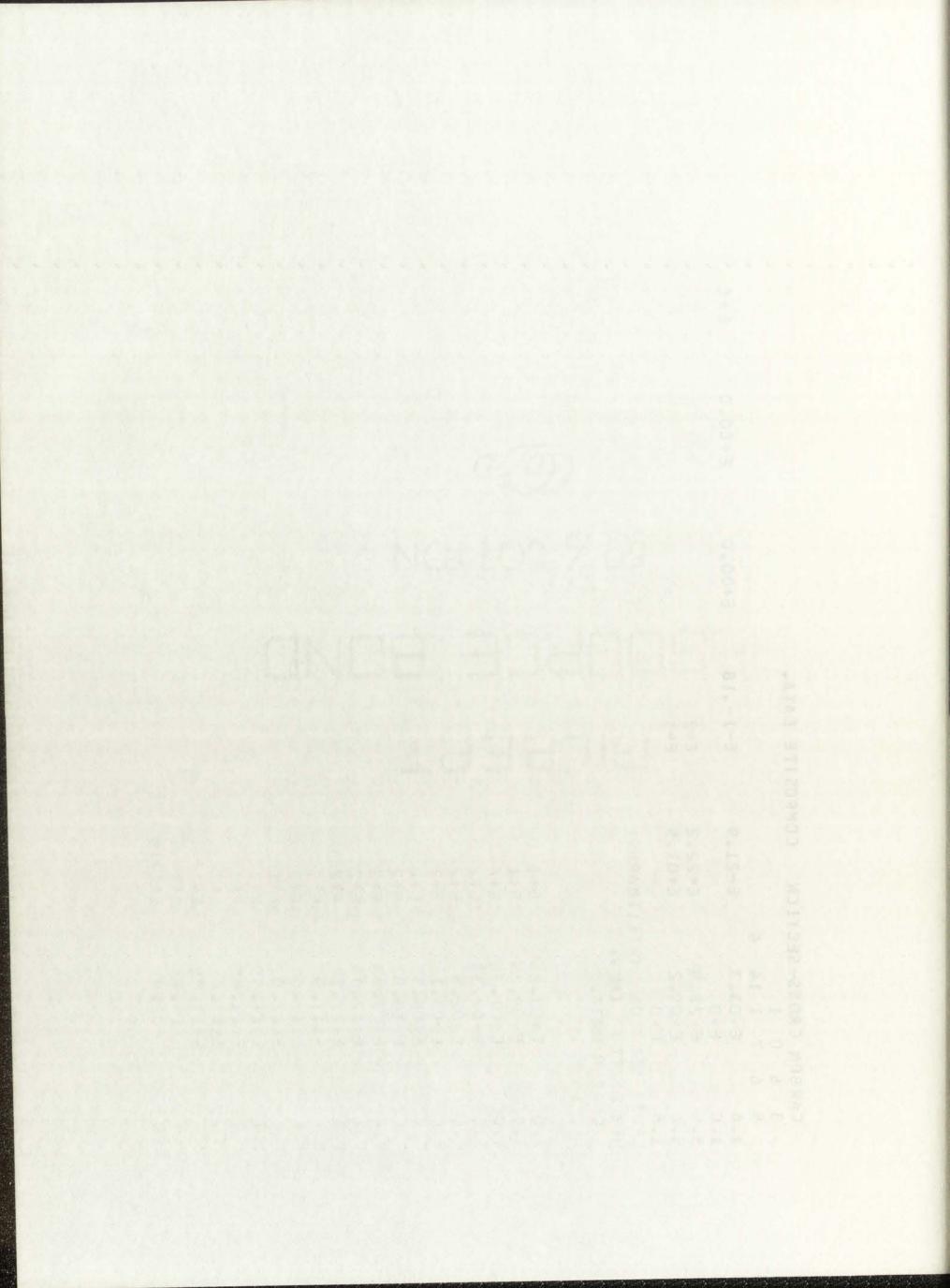
INPUT

FOR

GHLET CODE



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O 1 14 4	E+03	4	E+09.2	E+0	TION (MI	RGY (MEV)	DAT		+03.2	E+09.25	+01°7	E+02.33	E+02.3	E+03.1	E+03.5	E+13.0	E+12.65	E+12,35	E+12.1	4110	E+12.0	E+12.0	E+11.65	+11104	E+11.2	E+11,08	E+19.4	E+02.0
CARBUN 3 6 5 6	1.6	8.9	5.1	1.5	ROS	HE3 ENERG	4	19	2.0	3.0	4.0	5.0	0.9	8.0	0.6	1.0	I.I	1.2	1.3	1.4	1.5	1.6	1.7	1.8	2°C	2.2	2.4	0.0

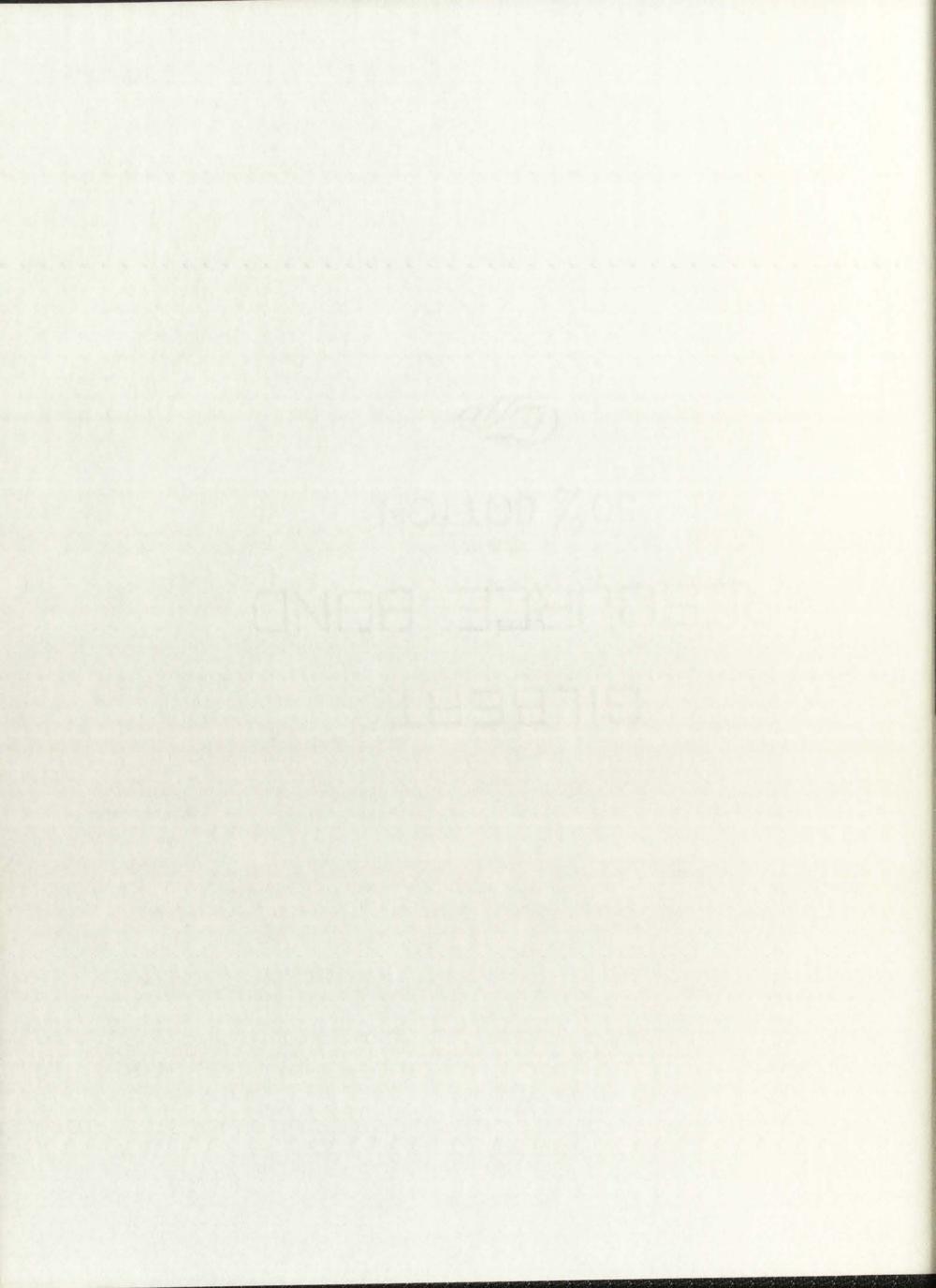


SAMPLE

OUTPUT

FOR

GHLET CODE



0° 62701767E+01

LOW ENERGY BACKGROUND \*\*

000

02

CARBON DATA. CARBON CROSS-SECTION COMPOSITE DATA.

1.511324E+ 1.556786E+ 3.921845E+	6.382964E.02 6.574969E.02 1.656362E.02	8.730279E+02 8.992893E+02 2.265483E+02	1.210108E=25 1.246509E=25 3.140197E=27	5.058200E+00 9.152149E+00 1.554867E+01
TOTAL	HIGH TAIL	GAUSSIAN	LOW TAIL	ENERGY
		00000000	00E+00	1.5000
	1.2109902E-01 3.7938159E-01	521487E+00	000E+00	3 1.50000
	.1462012E+0	654831E+0	00E+02 8.2	2,2000
	.1286875E .0	302791E+0 928933E+0	00E+02	00000
		000000E+0	00E+00	1.0000
		000000E-01	00E-01 "1.8	-1.80
	1024785E	968939E.0	00E_01	1,9000
	019875F=0	000000E+00 527g51E-02	00E+00	
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CALCULATED	.5045317E+0	W-	.3913308E+0	.3673557E+0	.1318003E+0	.6983392E+0	.2700056E+0	9966175E.0	.9991358E+0	.8816309E+0	.7004126E+0	. 4038322E+0	2203875E.0	.0520763E+0	.3661840E+0
VARIABLE	2500000E+0	.3300000	*3000000E +0	·5000000E+0	.000000000.	. 6500000E+0	. 1000000E+0	.9000000E+0	*0000000E+0	*000000000 *	·6500000E+0	.4500000E+0	.2000000E.0	.0800000E+0	. 4000000E+0
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### APPENDIX D

#### C24HE3P COMPUTER CODE

Sections of this code are similar or identical to the DECURA code discussed in Appendix A and the code discussed in Ref. 1. Those sections that are similar will not be discussed. This code is written in FORTRAN IV for the CDC 6600 computer.

# Main Program C24HE3P

The masses and Q values for several reactions are defined. AM1 is the mass of the incident particle (<sup>3</sup>He). AM3 is the mass of the light reaction product (proton). AM2(I) is the target mass for the Ith reaction. AM4(I) is the mass of the heavy product for the Ith reaction. GSQ(I) is the Q value for the Ith reaction. The reactions defined are listed in Table 18.

TABLE 18

REACTIONS DEFINED IN C24HE3P CODE

Index	Reaction
1	$^{12}C(^{3}He,p)^{14}N$
2	$^{13}\text{C}(^{3}\text{He,p})^{15}\text{N}$
3	$^{14}\text{N}(^{3}\text{He,p})^{16}\text{O}$
4	$^{15}\text{N}(^{3}\text{He,p})^{17}\text{O}$
5	$^{16}0(^{3}\text{He,p})^{18}\text{F}$
6	$^{17}0(^{3}\text{He,p})^{19}\text{F}$
7	$^{18}0(^{3}_{\text{He,p}})^{20}_{\text{F}}$

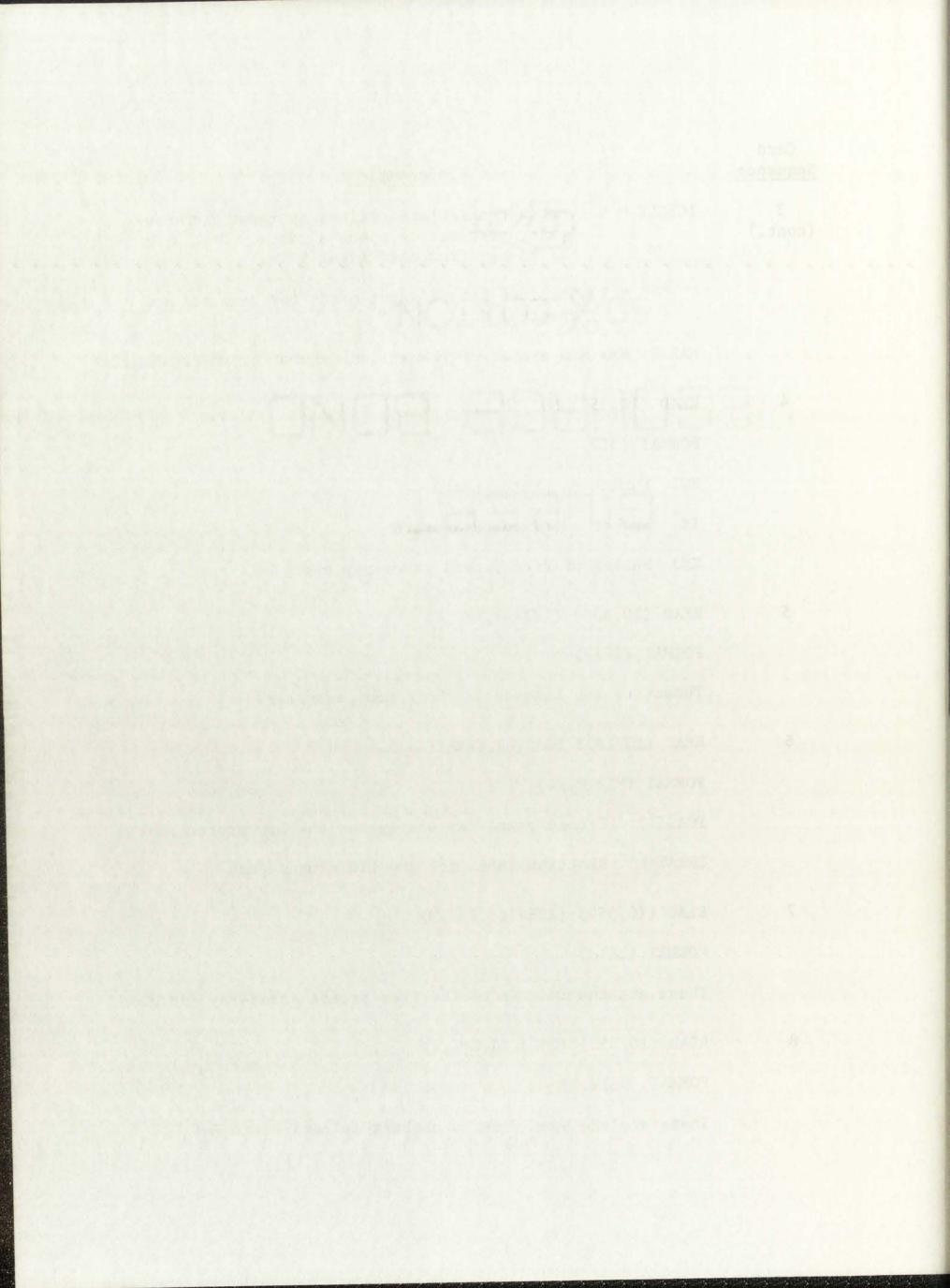
# Subroutine DATAIN

One of the major modifications between this subroutine and the similar subroutine that was discussed in Ref. 25 is the number of regions that can be analyzed in a spectrum. Only one region is defined in each spectrum. The following upper bounds exist on variable storages: proton peaks - 20, data points analyzed - 512, and reactions - 10.

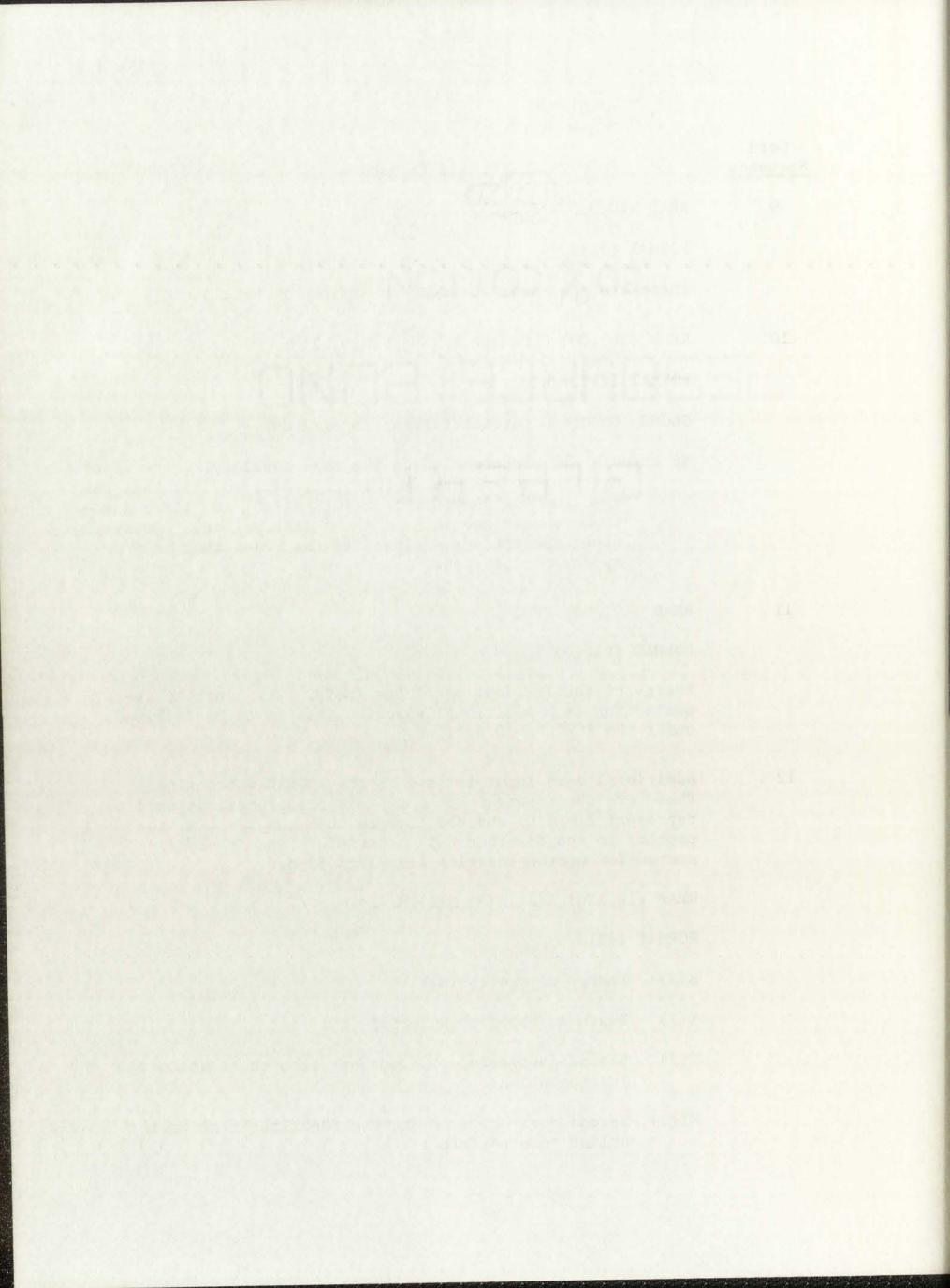
The bounds on the data region that is being fitted in the spectrum are controlled by the code. The lower bound will be CBLOW channels less than the peak channel of the lowest energy proton peak. The upper bound is the lesser of the peak channel number of the highest energy proton peak plus 13 and 512. Those channels containing zero counts are ignored.

Card Sequence	Information
1	READ (10,340) (TITLE(J),J=1,8)
	FORMAT (8A10)
	Identification information (80 BCD characters)
2	READ (10,280) NFOIL, FOILTH, CBLOW, SAM, IPUNF
	FORMAT (16, 3F12.0, 16)
	NFOIL Number of absorber foils between target and detector
	FOILTH Thickness of absorber foils (cm)
	CBLOW Number of channels to fit below the lowest energy proton peak
	SAM Lowest proton energy (after absorber foils) to be used in the fit
	IPUNF Punch output flag
3	READ (10,350) ICYCLE, MAXIT
	FORMAT (213)

Card Sequence	Information
3 (cont.)	ICYCLE = 0 Use just-calculated values as input for analyzing next set of spectral data. Read only <sup>3</sup> He energy from card input file.
	= 1 Complete set of input cards for next set of spectral data.
	MAXIT Maximum number of iterations before forced convergence
4	READ (10,350) NOI, IM, KEJ
	FORMAT (313)
	NOI Number of proton peaks
	IM Number of fixed parameters
	KEJ Number of free prompt gamma-ray energies
5	READ (10,350) (IXJ(L),L=1,K)
	FORMAT (2413)
	These are the indexes of the fixed parameters
6	READ (10,285) PGAS(L), IREAT(L)
	FORMAT (F12.0,16)
	PGAS(L) Prompt gamma-ray energy for the Lth proton peak
	IREAT(L) Reaction index for the Lth proton peak
7	READ (10,350) (KEEJ(L),L=1,M)
	FORMAT (2413)
	These are the indexes of the free prompt gamma-ray energies
8	READ (10,355) (PG(J,L),L=1,9)
	FORMAT (6E12.7)
	These are the same nine parameters as defined in Ref. 1



Card Sequence	Information
9	READ (10,355) (PAS(L),L=1,NOII)
	FORMAT (6E12.7)
	These are the Gaussian areas as defined in Ref. 1
10	READ (10,300) CLCNN,N6,N7,N8,N9,N10,N11
	FORMAT (E12.7,613)
	CLCNN Counts/C for the current integrator
	N6 through N11 Information on the tape identifying the first spectrum to analyze (m, d, y, h, min, and sec that the spectrum was dumped). For ICYCLE = 0, the first spectrum is searched for the above information. Subsequent spectra are analyzed in the order that they appear on the tape.
11	READ (10,290) EHE3
	FORMAT (F12.0)
	Energy of the incident particles (MeV). This card is repeated for each additional spectrum that is to be analyzed under the ICYCLE = 0 option.
12	Additional card input is read in the PIONIZ subroutine. These are the inputs for the cubic spline functions used to represent $X = f(E)$ and the inverse function $E = f(X)$ for protons in the absorber foil material. Data is usually stored for proton energies from 1 to 12 MeV.
	READ (10,120) E(J),X(J),M(J),MI(J)
	FORMAT (4E12.5)
	E(J) Energy of proton (MeV)
	X(J) Depth in absorber material (cm)
	M(J) Second derivative of function (from cubic spline interpolation)
	MI(J) Second derivative of inverse function (from cubic spline interpolation)



# Subroutine LSRMZ

Quite similar to the code discussed in Ref. 25. Some of the bounds and restrictions on the parameter value have been changed to ones that correspond to the resolution of the proton peaks.

# Subroutine OUTRAN

Similar to other output subroutines. (See Ref. 25 and Appendix A.)

# Subroutine PHICAL

See Ref. 25 and Appendix A.

## Subroutine PIONIZ

This subroutine is used to calculate the proton energy losses in the absorber foils. The depth versus energy has been calculated for 12-MeV protons incident on a thick absorber foil. The resulting function and the inverse of this function are interpolated using cubic splines. These functions are then used in the code to calculate the energy losses in the absorber foil.

The function is first solved to determine the material depth to give the incident proton energy. The foil thickness is then added to this value of X, and the inverse function is evaluated at this sum. The result is the proton thickness after passing through the foil.

The more important variables used in this subroutine are listed in Table 19.

### Subroutine PLTZ

This subroutine is similar to other plotting subroutines. (See Ref. 25 and Appendix A.) The left and right plot boundaries are fixed at 0.0 and 8.0.

#### TABLE 19

# LIST OF VARIABLES IN PIONIZ SUBROUTINE

E(J)	Energy (MeV) of Jth interpolation point
FOILTH	Thickness of an absorber foil (cm)
L	Card input data flag, = 0 read new data, # 0 use old data
M(J)	Second derivative of Jth interpolation point for the function $X = f(E)$
MI(J)	Second derivative of the Jth interpolation point for the inverse function $E = f(X)$
NFOIL	Number of absorber foils
NPTS	Number of interpolation points
X(J)	Depth in absorber to reach energy E(J) for the Jth interpolation point (cm)
YY	Absolute value of energy loss in the absorber foil
ZZ	Incident particle energy (MeV)

## Subroutine PROMPT

This subroutine is used to calculate the prompt gamma-ray energy from the iterated least-squares energy for the proton. The kinematics equations solved are from Ref. 30. Both the relativistic and nonrelativistic equations are coded. The more important variables used in this subroutine are listed in Table 20.

# Subroutine PRTNEY

This subroutine is used to calculate the proton energy for a given set of reaction parameters. The kinematics equations solved are from Ref. 30. The more important variables used in this subroutine are listed in Table 21.

## TABLE 20

### LIST OF VARIABLES IN PROMPT SUBROUTINE

I Reaction index

EHE3 Incident <sup>3</sup>He energy

E3 Proton energy

EPG Prompt gamma-ray energy

IRELV = 0 use nonrelativistic equation

= 1 use relativistic equation

#### TABLE 21

# LIST OF VARIABLES IN PRINEY SUBROUTINE

I Reaction index

EHE3 Energy of incident <sup>3</sup>He particle (MeV)

E3 Proton energy (MeV)

EPG Prompt gamma-ray energy (MeV)

AMZ(I) Target masses (amu)

AM4(I) Heavy product masses (amu)

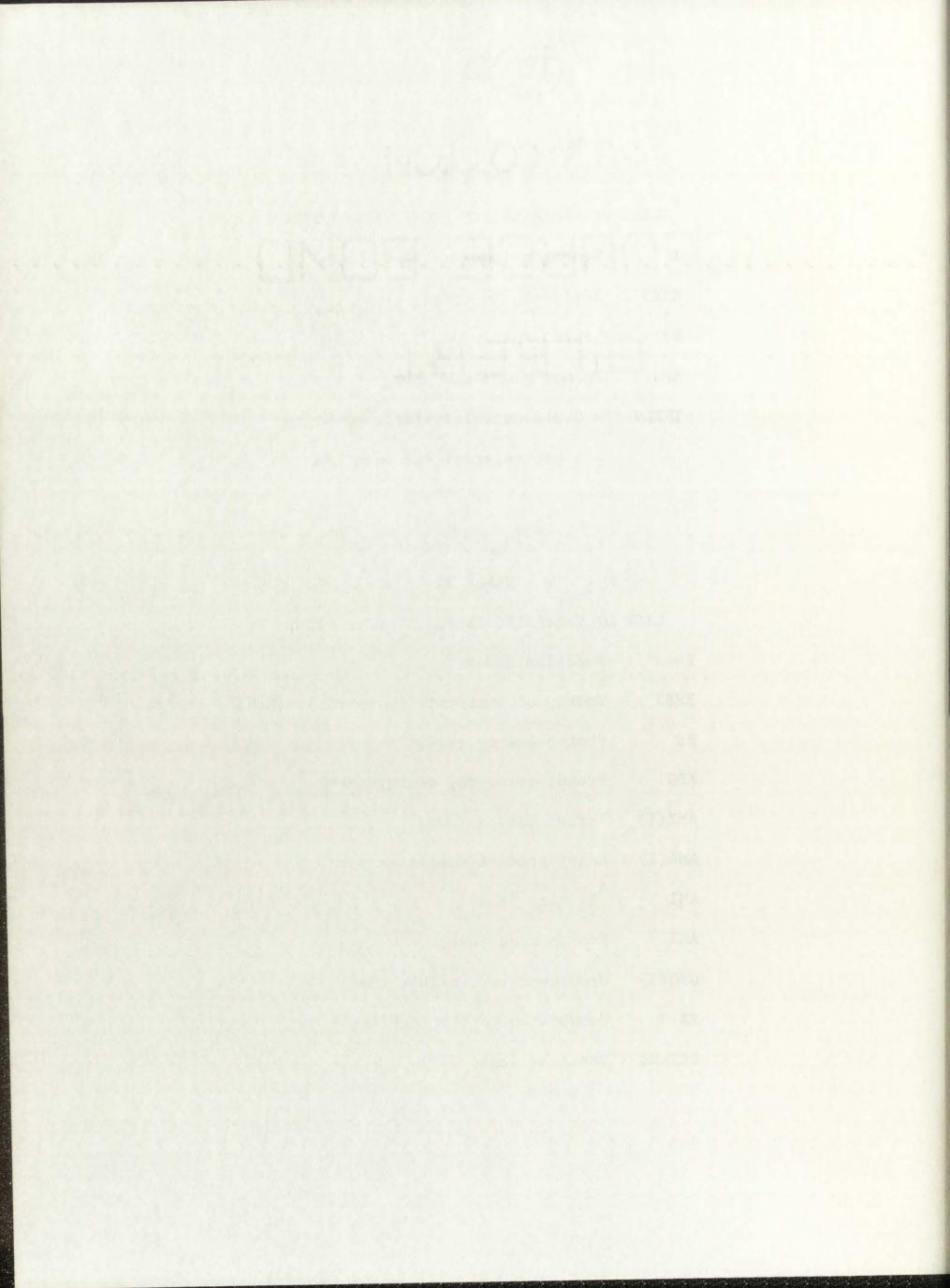
AM1 <sup>3</sup>He mass (amu)

AM3 Proton mass (amu)

GSQ(I) Ground-state Q values (MeV)

EZ Conversion factor (MeV/amu)

DETANG Detector angle (°)

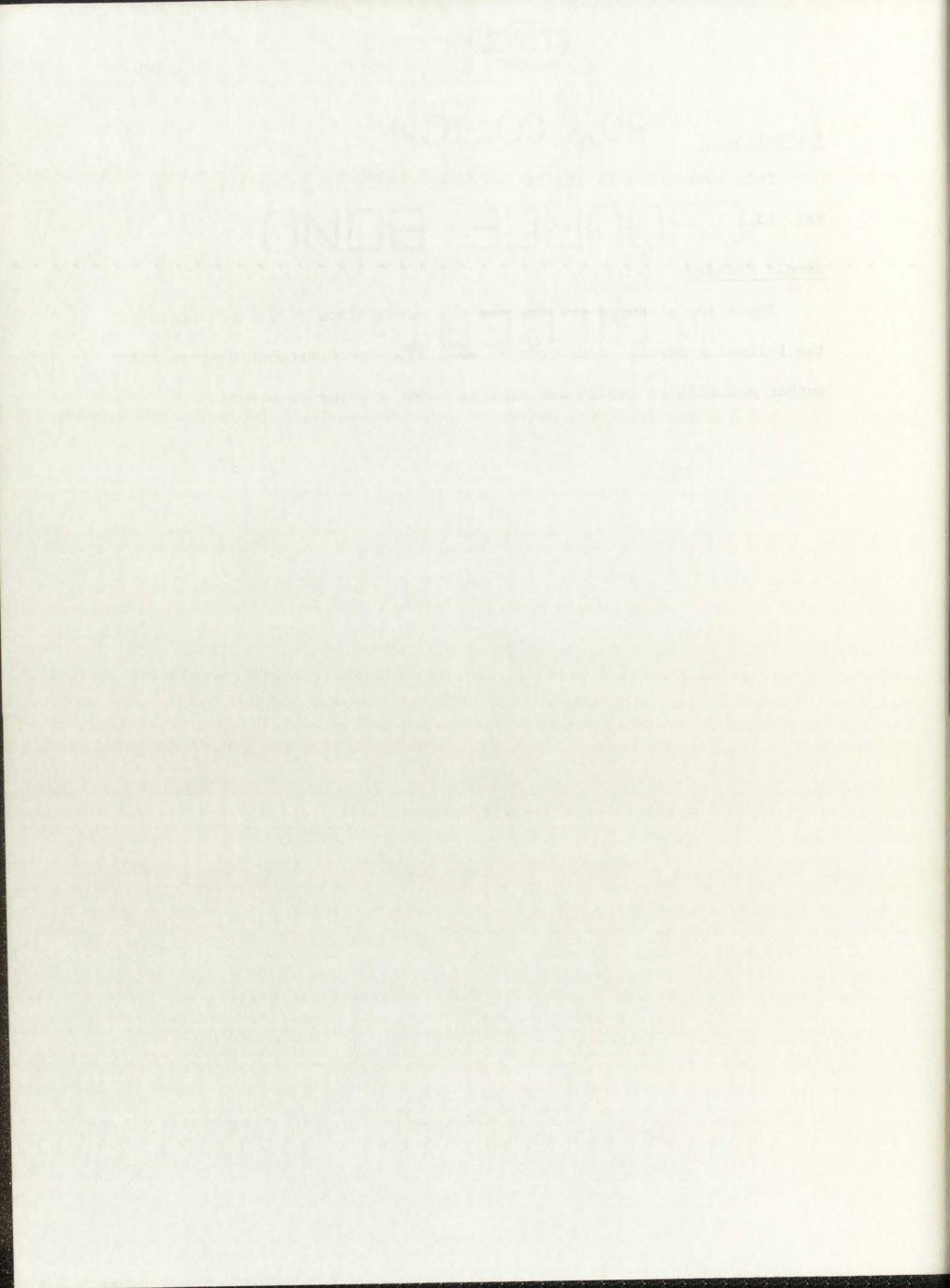


# Subroutine YP

This subroutine is similar to other function subroutines. (See Ref. 25.)

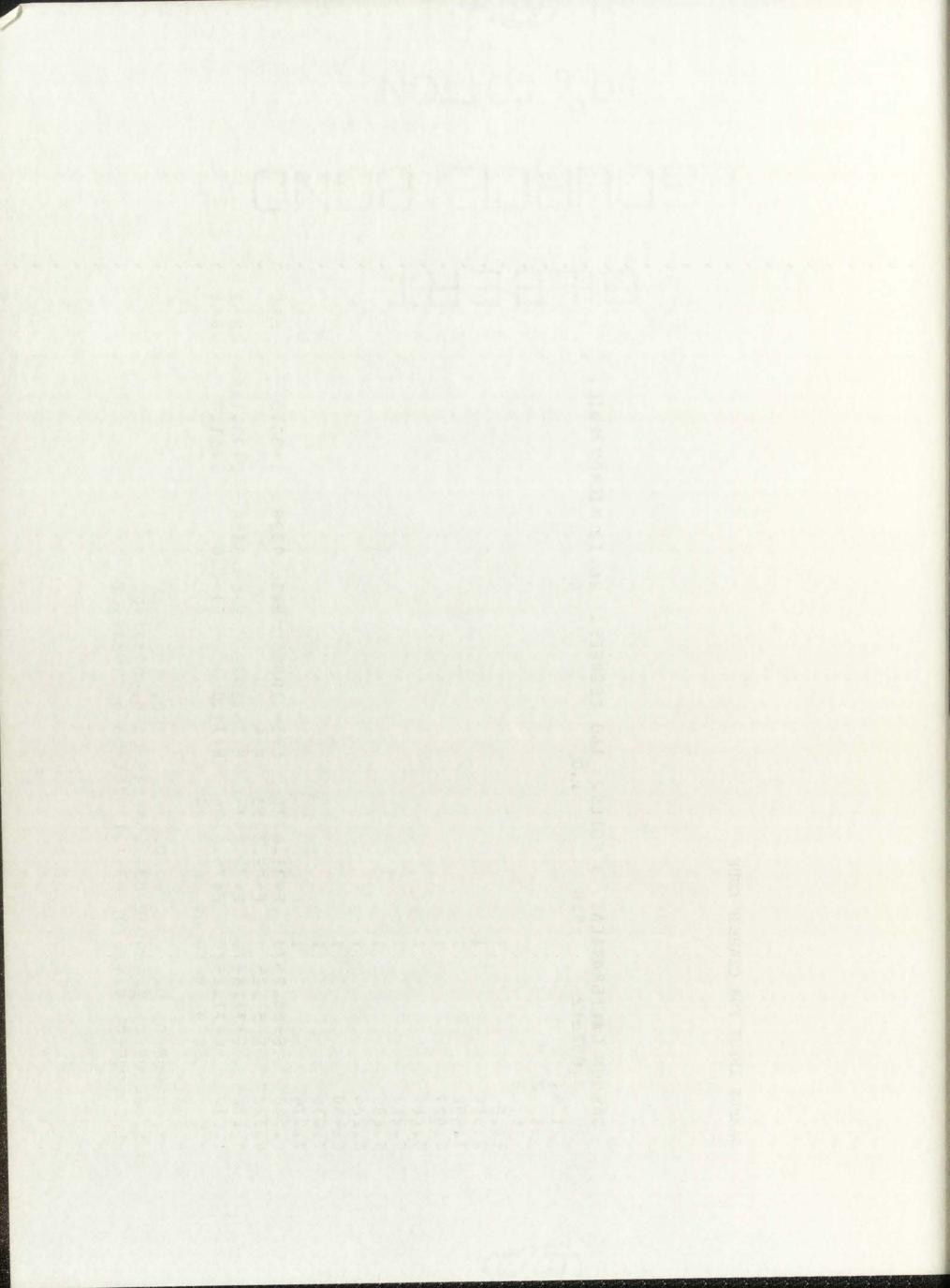
# Sample Problem

Input for a sample problem and the output from it are presented on the following pages. This code is available for distribution from the author and will be copied and sent to those wishing to use it.

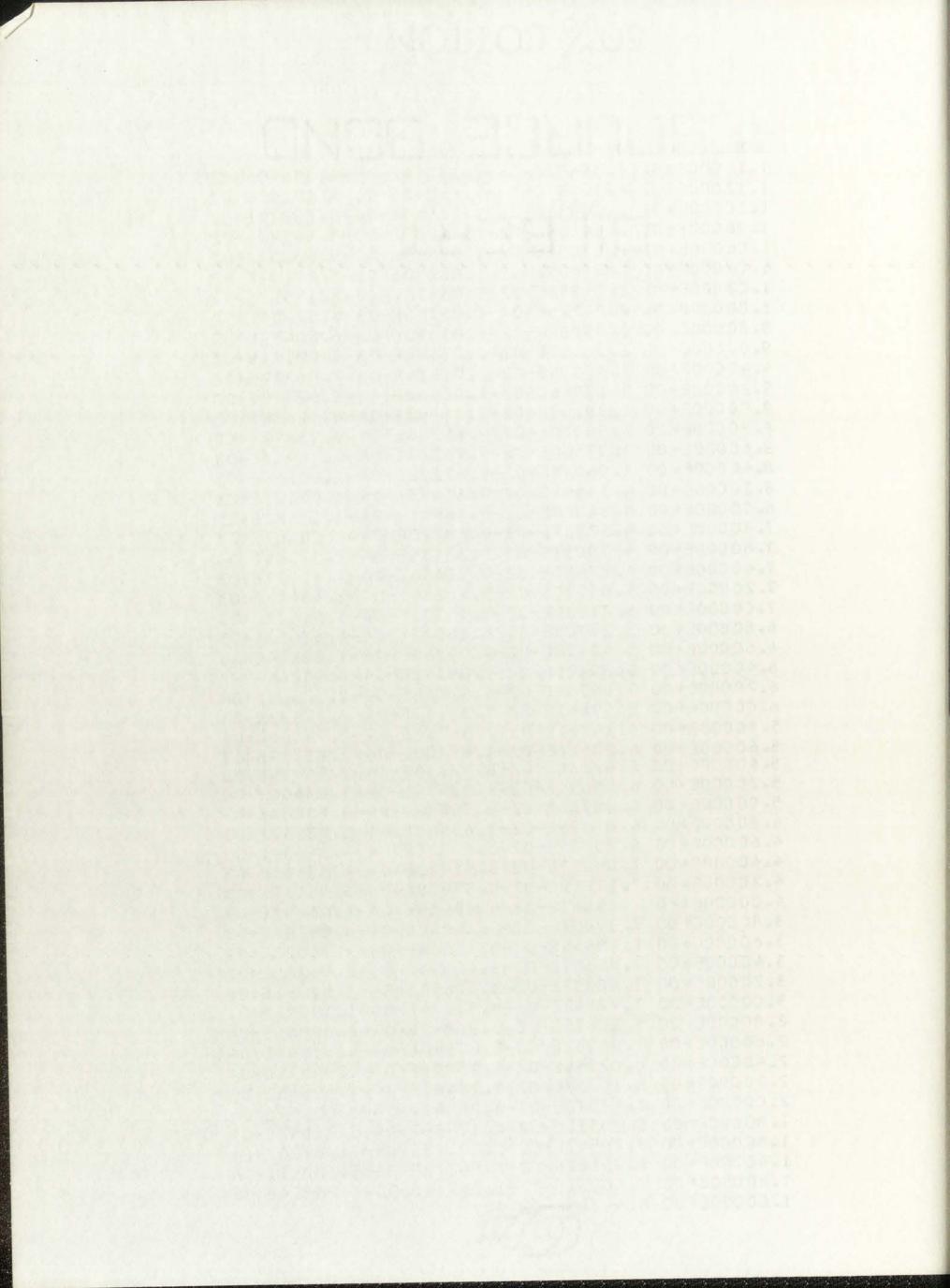


CODE
C24HE3P
FOR
INPUT
SAMPLE

															E+C		E+1	E+5					
26.12 M ICRON /FOIL.															E+30.0		E+73.1248	E+51.0					
															E+36.9328		E+63.3856	E+41.0				E+02	E+02
160 CEGREES.															E+11058	E-4	E+76 .3022	E+71.0			0.	59881E-03-5.40932E+02	E-03-4-19585
. 3 FOILS.															+3106	9	+7204	E+75.6196	15		0.0	3-10	-03-1.
102612 5.0		0		1	1	1	-	1	1	1	1	1	1	-	+05.2	-525	+71.387	E+71.1920	1 8 6-		E+01	8401	+01 4.93570
CARBON 3.0	1 40	11 2	8 9	30	.31	. 95	. 92	10	.71	· 88	6.224	.46	.03	.97	46	.32	.172	11		.593	1.20000	800	1.16000



```
SAMPLE INPUT FOR C24HE3P CODE (continued)
1.14000E+01 7.35492E-03-1.21219E-03-4.77690E+02
1.12000E+01 9.74157E-03-1.15648E-03-4.87151E+02
1.1CCOOE+01 1.20956E-02-1.13688E-03-5.13319E+02
1.08000E+01 1.44169E-02-1.12099E-03-5.34597E+02
1.C6COOE+01 1.67054E-02-1.09915E-03-5.63202E+02
1. C4 COOE+ 01 1. 89609E-02-1.08240E-03-5.89701E+02
1. C2 COOE+ 01 2. 11833E-02-1.06626E-03-6.17553E+02
1. CO 000E+01 2. 33725E-02-1.05756E-03-6.52883E+02
9.80000E+00 2.55283E-02-1.03350E-03-6.80473E+02
9.60000E+00 2.76507E-02-1.03344E-03-7.20821E+02
9.40000E+00 2.97395E-02-1.01274E-03-7.56217E+02
9.20000E+00 3.17946E-02-1.00562E-03-8.01729E+02
9. CCCCOE+00 3.38158E-02-9.94793E-04-8.42688E+02
8.80000E+00 3.58030E-02-9.85208E-04-8.96692E+02
8.60000E+00 3.77560E-02-9.74373E-04-9.38917E+02
8.40000E+00 3.96748E-02-9.67298E-04-1.00568E+03
8.20C00E+00 4.15591E-02-9.61435E-04-1.06107E+03
8. COCOOE+ 00 4. 34088E-02-9.46961E-04-1.13182E+03
7.80C00E+00 4.52237E-02-9.50720E-04-1.20207E+03
7.60000E+00 4.70037E-02-9.35159E-04-1.27365E+03
7.4CC00E+00 4.87487E-02-9.33644E-04-1.37699E+03
7.20000E+00 5.04583E-02-9.25264E-04-1.46413E+03
7. CCCCCCE+00 5. 21324E-02-9.15301E-04-1.56625E+03
6.80000E+00 5.37709E-02-9.18532E-04-1.67613E+03
6.60000E+00 5.53736E-02-9.00569E-04-1.82674E+03
6.40C00E+00 5.69401E-02-9.09191E-04-1.93904E+03
6.20000E+00 5.84704E-02-8.92668E-04-2.12363E+03
6. CCCCOOE+00 5. 99641E-02-8.90137E-04-2.27833E+03
5.80 COOE+ 00 6.14211E-02-8.86786E-04-2.48356E+03
5.60000E+00 6.28411E-02-8.87720E-04-2.71149E+03
5.40000E+00 6.42238E-02-8.72333E-04-2.94435E+03
5.20000E+00 6.55690E-02-8.72949E-04-3.25640E+03
5.00000E+00 6.68763E-02-8.70872E-04-3.53848E+03
4.80000E+00 6.81456E-02-8.63563E-04-3.93047E+03
4.60000E+00 6.93765E-02-8.64877E-04-4.34488E+03
4.4CCOOF+00
           7.05687E-02-8.51928E-04-4.82466E+03
4.20C00E+00 7.17219E-02-8.57409E-04-5.40127E+03
4. CO 000E+00
           7.28357E-02-8.48435E-04-6.06647E+03
3.80C00E+00 7.39097E-02-8.48850E-04-6.85786E+03
3.60000E+00 7.49435E-02-8.41164E-04-7.76000E+03
3.40000E+00 7.59367E-02-8.41495E-04-8.96202E+03
3.20000E+00 7.68887E-02-8.32858E-04-1.02051E+04
3. CCCCCE+00 7. 77992E-02-8.37074E-04-1.19793E+04
2.80 COOE+ 00
           7.86675E-02-8.28847E-04-1.39865E+04
2.60000E+00 7.94931E-02-8.27540E-04-1.65847E+04
2.4CC00E+00 8.02754E-02-8.25995E-04-1.99023E+04
2.20000E+00 8.10137E-02-8.18481E-04-2.42665E+04
2.C0000E+00 8.17072E-02-8.20081E-04-3.00132E+04
1.80C00E+00 8.23552E-02-8.10694E-04-3.72597E+04
1.60000E+00 8.29567E-02-8.30145E-04-5.08730E+04
1.4CCOOF+00 8.35107E-02-7.54228E-04-5.60891E+04
1.20000E+00 8.40161E-02-1.02344E-03-1.21224E+05
1.CC000E+00 8.44714E-02 0.
                                     0.
```

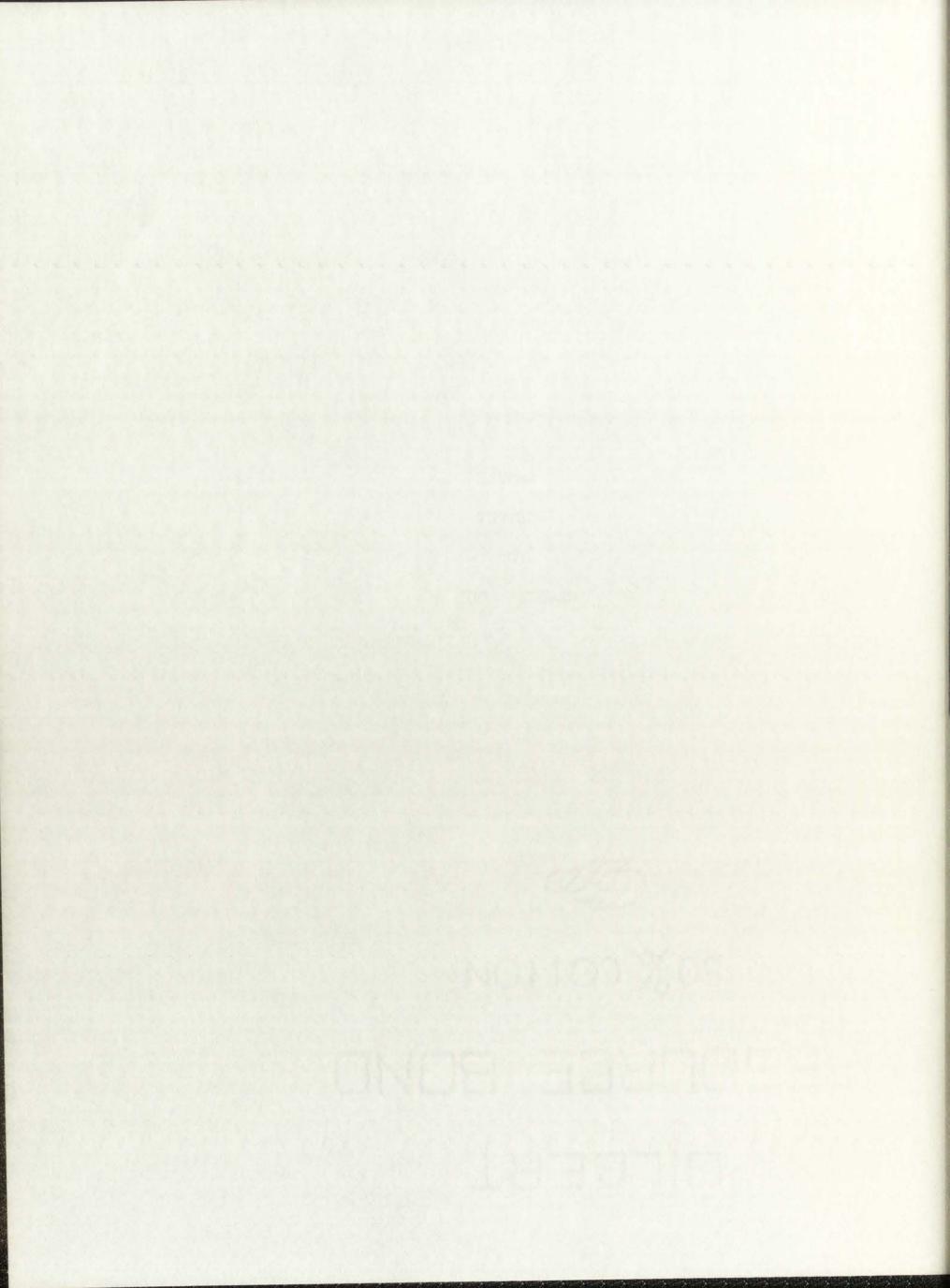


SAMPLE

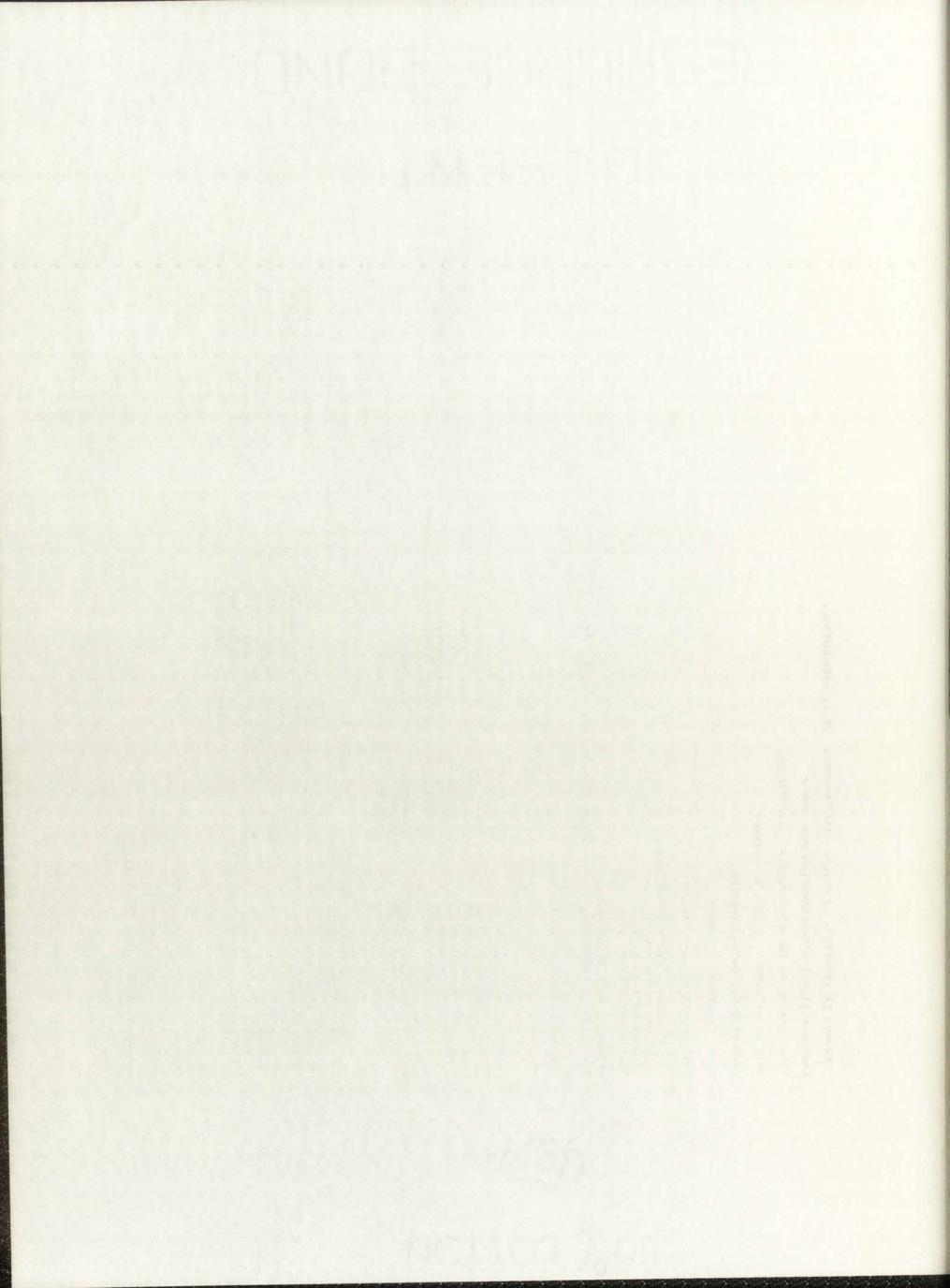
OUTPUT

FOR

C24HE3P CODE

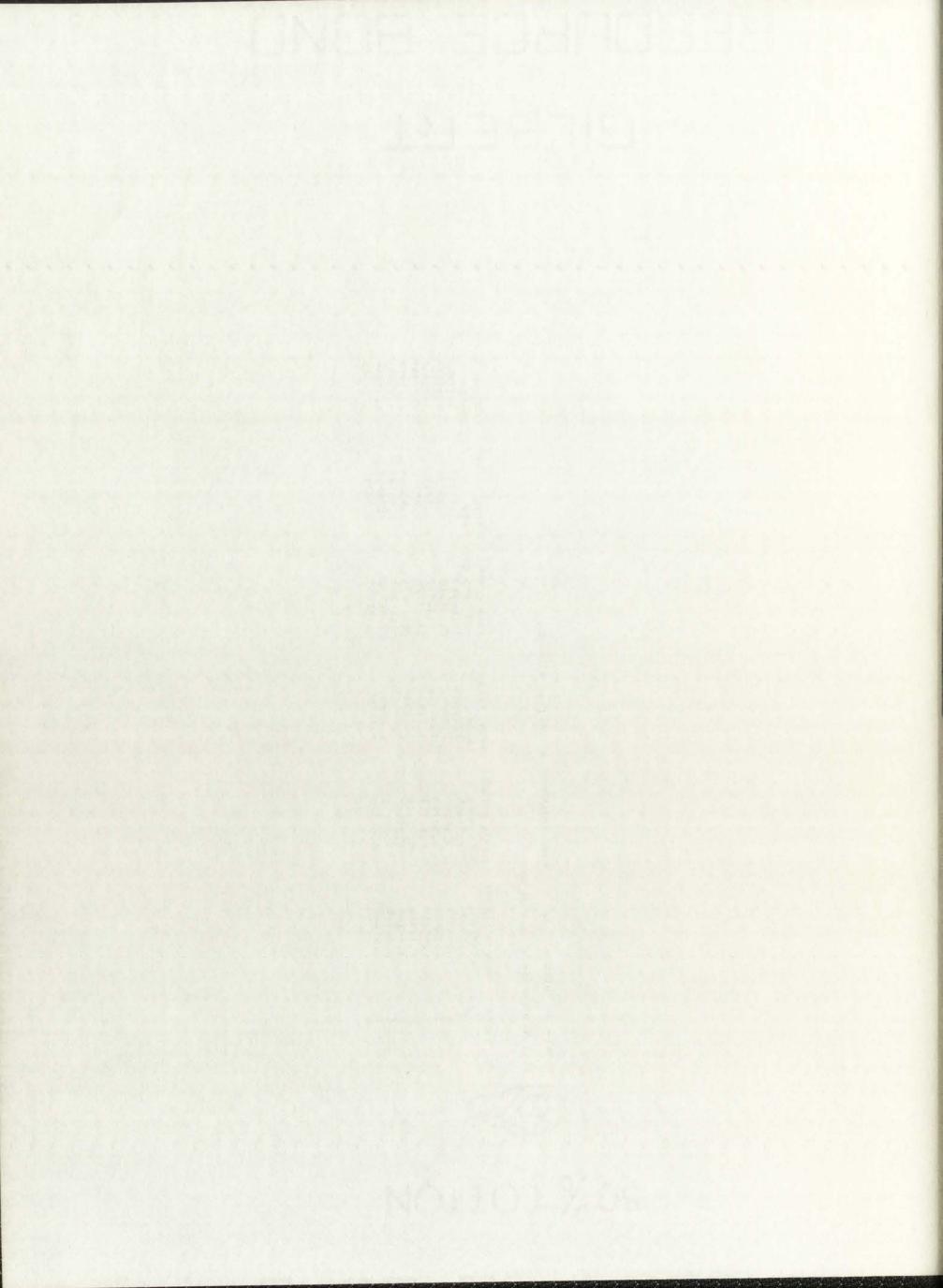


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LUST COUNTS =	16						
CLOCK TIME = 24 NO SOLUTION, SFT XA GREATER THAN X XA GREATER THAN X	1500 MI 1 100 MI 1 100 MI 1 100 MI	.u.					
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125,527		3.047543F +07	2.4012155.407	799770F+0	.00	.4497	00
2,640		2,84,0413F+07	3.3077245.07	.160973F .0		3077	00
944.494		*643670F +07	3.0104946.07	1328945+0	00	1160	0
266.036 443.037 511.501	116.52 6	1.410/59F.06 8.145887E.05 5.249179E.07	1.204973E+07 5.457105E+07	7.607839€.05		1.2049735.07	7.407839E.05
17 ITERATIONS							
# STATED VANIANCE #		4,3523335E+0A					
ENEAGY = 15.72	15.721UTOCHANHEL	4EL104.705	KEV				
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NUMBER OF LINES	3D M						



NUMBER OF FOILS = 3. FOIL THICKNESS = 26.1240 MICHOIS.
MELIUM-3 FNFHUY = 4.5431 MFV

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						1.65044			
						30,10494			
GAMMA FILEDGY	CALC-MEN	2.31900	3.94200	4.92790	5.11700	5,71300	5.44500	6.72410	4 4 5 6 4 5
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PRUTUN ENEMBY	CALC-MEY	6.40370	5.536e	9.776.0	8.60 21 B	4.11999	3.98154	3.10946	1. 5.3440
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## APPENDIX E

### INTERPOLATORY CUBIC SPLINES

Interpolatory cubic splines were used to interpolate and smooth much of the data presented in this paper. The derivation of the equations necessary to do these interpolations is given below.

Figure 55 shows the initial assumptions for solving the cubic spline problem. Data have been obtained at  $x_0, \dots, x_{j-1}, x_j, x_{j+1}, \dots, x_n$ . It is assumed that the second derivative is linear between all  $x_{k-1}, x_k$ , such that

$$\frac{d^2y}{dx^2} = M(x) = \frac{M_k(x - x_{k-1}) + M_{k-1}(x_k - x)}{h},$$
 (1)

where  $h = x_k - x_{k-1}$ 

The above differential equation is solved using the following boundary conditions:

1) 
$$\frac{dy}{dx}\Big|_{x_j,h_1} = \frac{dy}{dx}\Big|_{x_j,h_2}$$

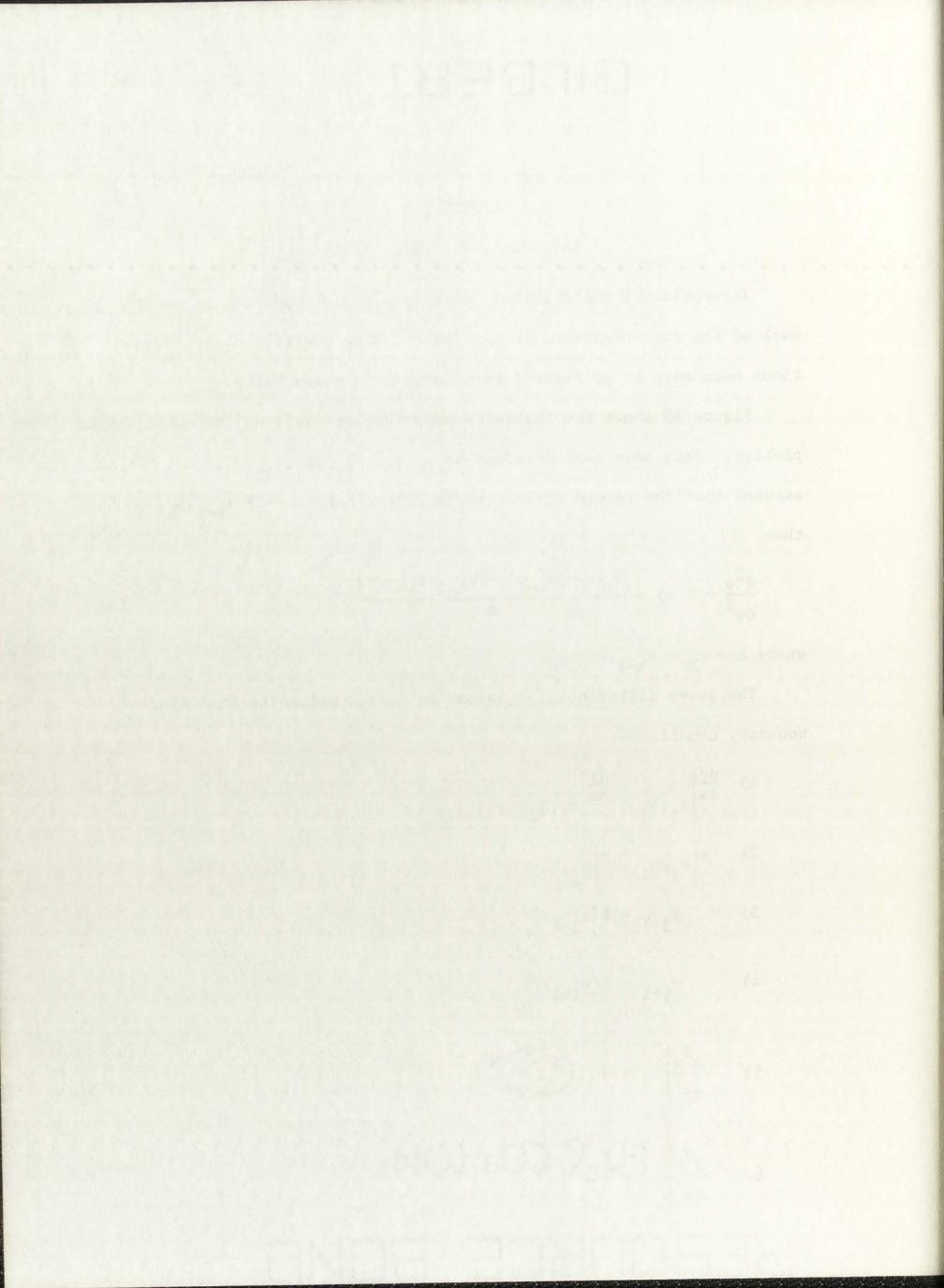
2) 
$$y|_{x_{1},h_{1}} = y|_{x_{1},h_{2}}$$

3) 
$$y_{j-1} = f(x_{j-1})|_{h_1}$$

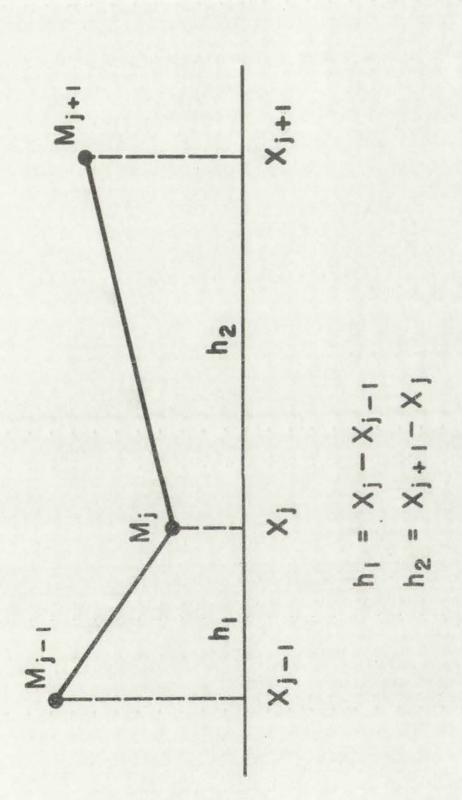
4) 
$$y_{j+1} = f(x_{j+1})|_{h_2}$$

$$5) \qquad \frac{d^2x}{dy^2}\bigg|_{x_0} = 0$$

$$6) \qquad \frac{d^2x}{dy^2}\bigg|_{x_n} = 0$$



# BASIC ASSUMPTIONS FOR CUBIC SPLINE



$$\frac{d^2y}{dx^2} = M(x) = \frac{M_J(x-x_{J-1}) + M_{J-1}(x_J-x)}{h_J}$$

Fig. 55. Basic assumptions for the cubic spline problem.

The solution of the above differential equation for n data points yields a set of equations that form a tridiagonal matrix which can be solved for  $M_{i}$ .

$$\frac{(y_{j} - y_{j+1})}{h_{2}} + \frac{(y_{j} - y_{j-1})}{h_{1}} = -\frac{M_{j}}{3}(h_{1} + h_{2}) - \frac{M_{j-1}}{6}h_{1} - \frac{M_{j+1}}{6}h_{2}.$$
 (2)

x<sub>j</sub>, y<sub>j</sub>, and M<sub>j</sub> can be used to calculate the value of the interpolation function, and also its first and second derivatives.

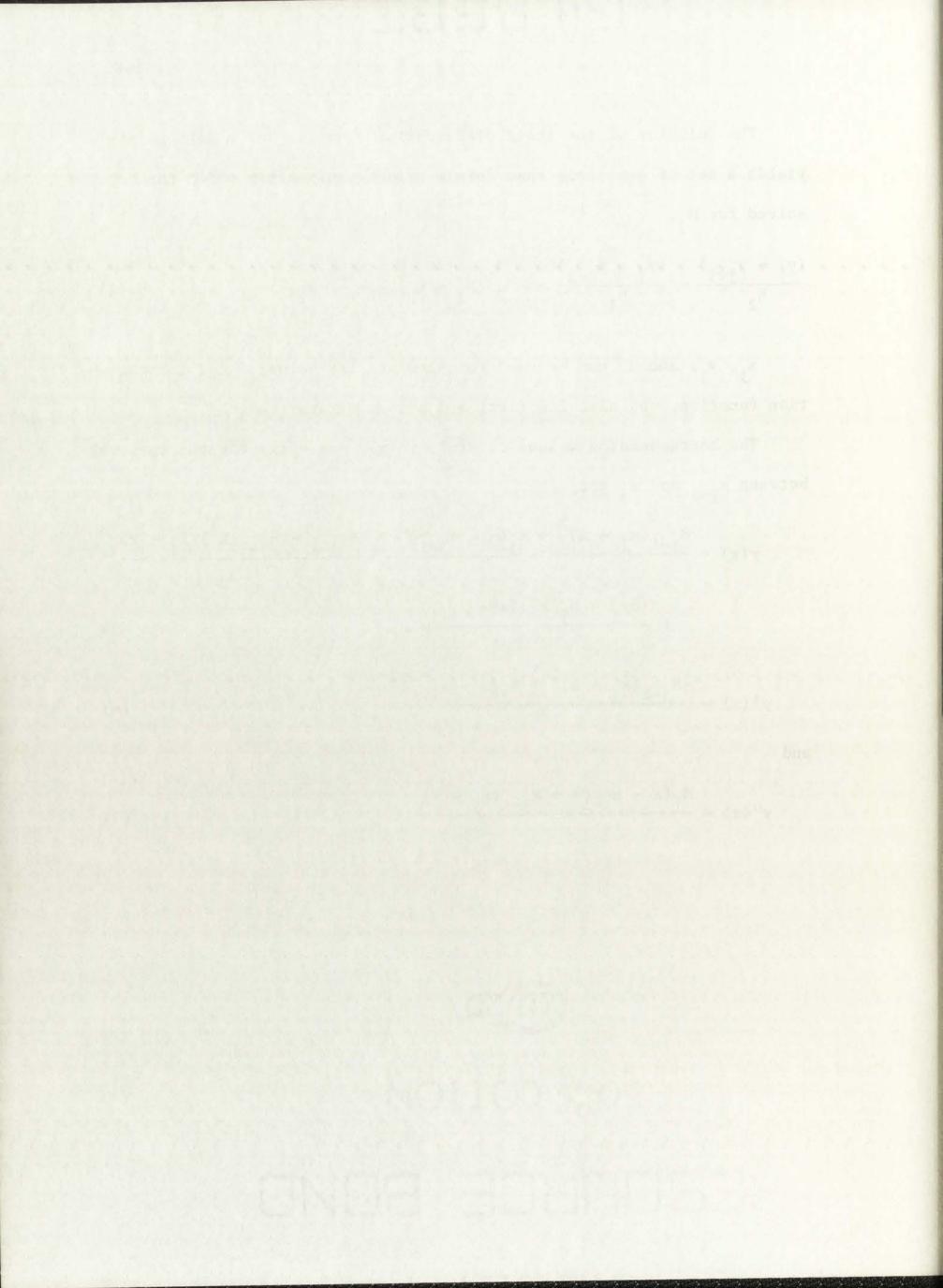
The corresponding values of y(x), y'(x), and y''(x) for the interval between  $x_{i-1}$  and  $x_i$  are

$$y(x) = \frac{M_{j-1}(x_{j} - x)^{3} + M_{j}(x - x_{j-1})^{3} + (6y_{j-1} - M_{j-1} h^{2})(x_{j} - x)}{6h} + \frac{(6y_{j} - M_{j} h^{2})(x - x_{j-1})}{6h},$$
(3)

$$y'(x) = \frac{-M_{j-1}(x_j - x)^2 + M_j(x - x_{j-1})^2}{2h},$$
 (4)

and

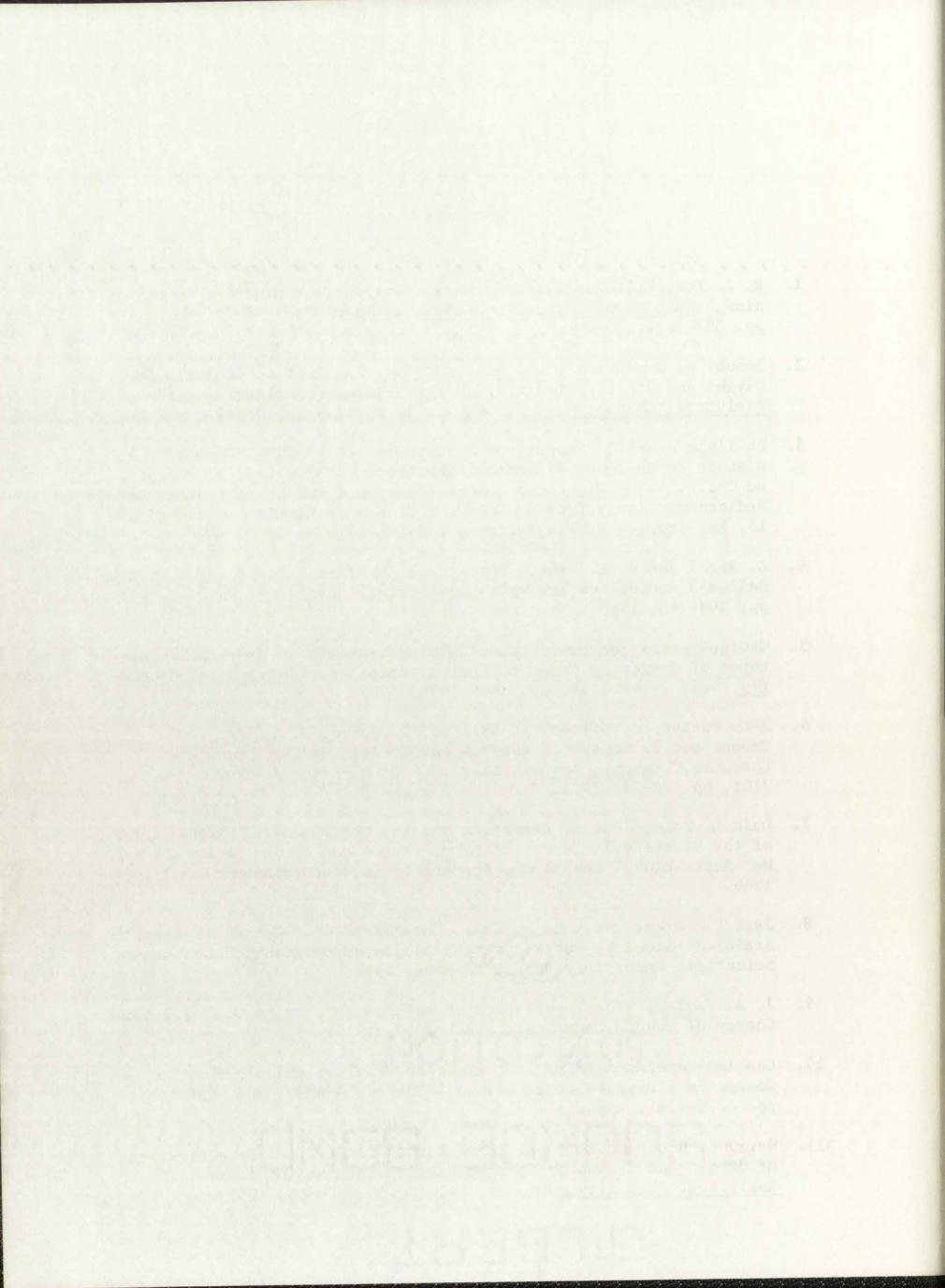
$$y''(x) = \frac{M_{j}(x - x_{j-1}) + M_{j-1}(x_{j} - x)}{h}.$$
 (5)



### REFERENCES

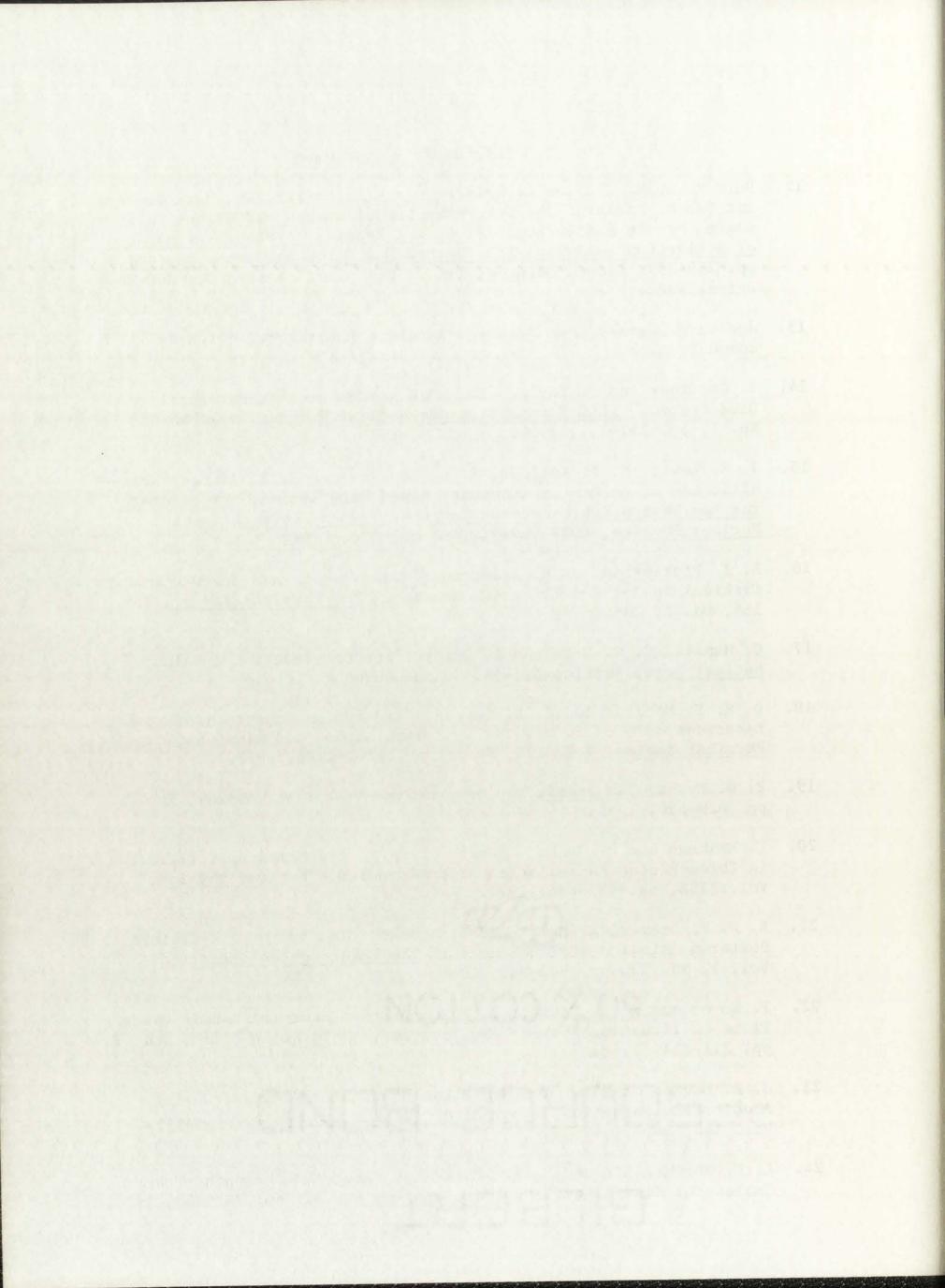
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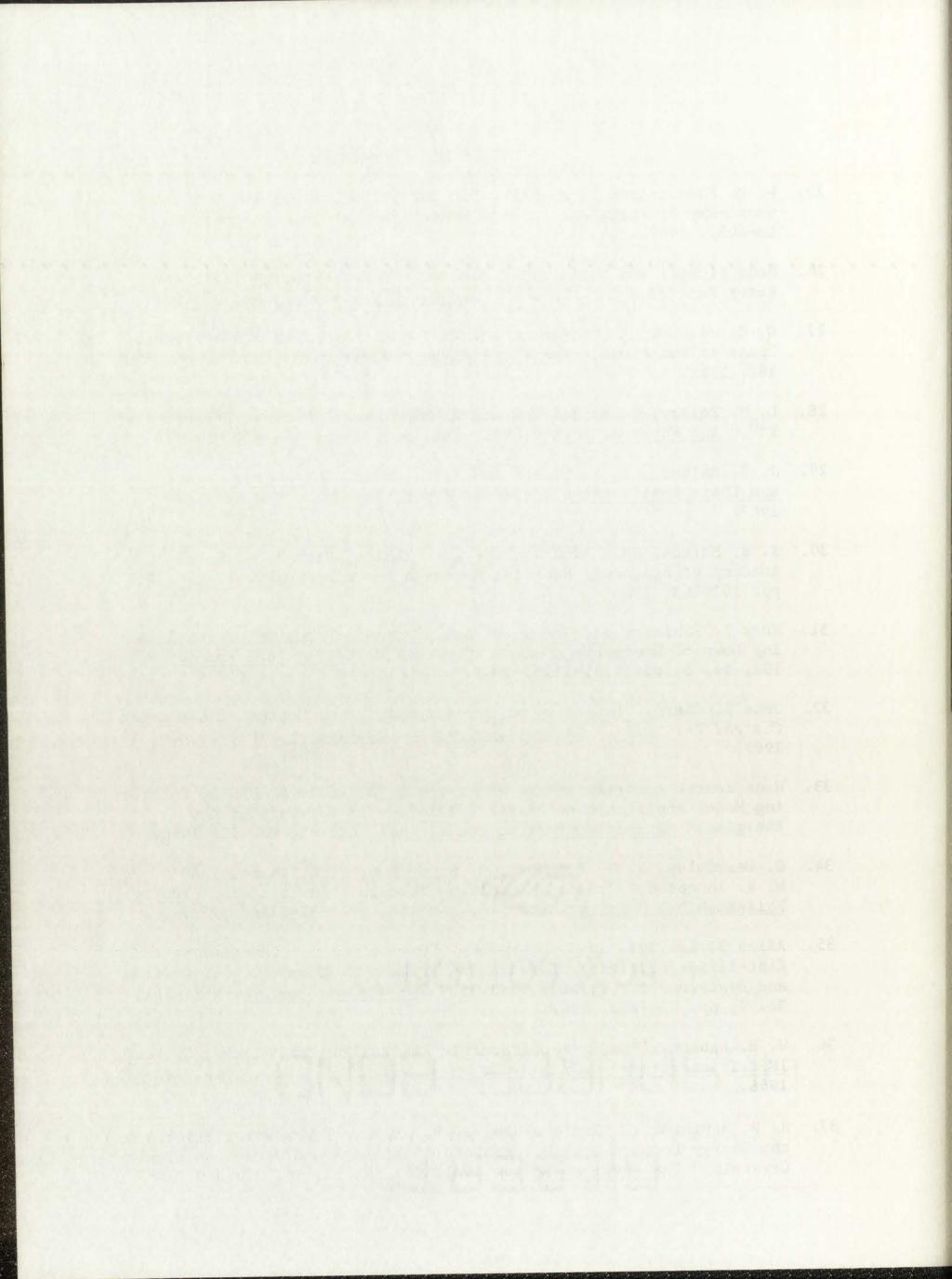
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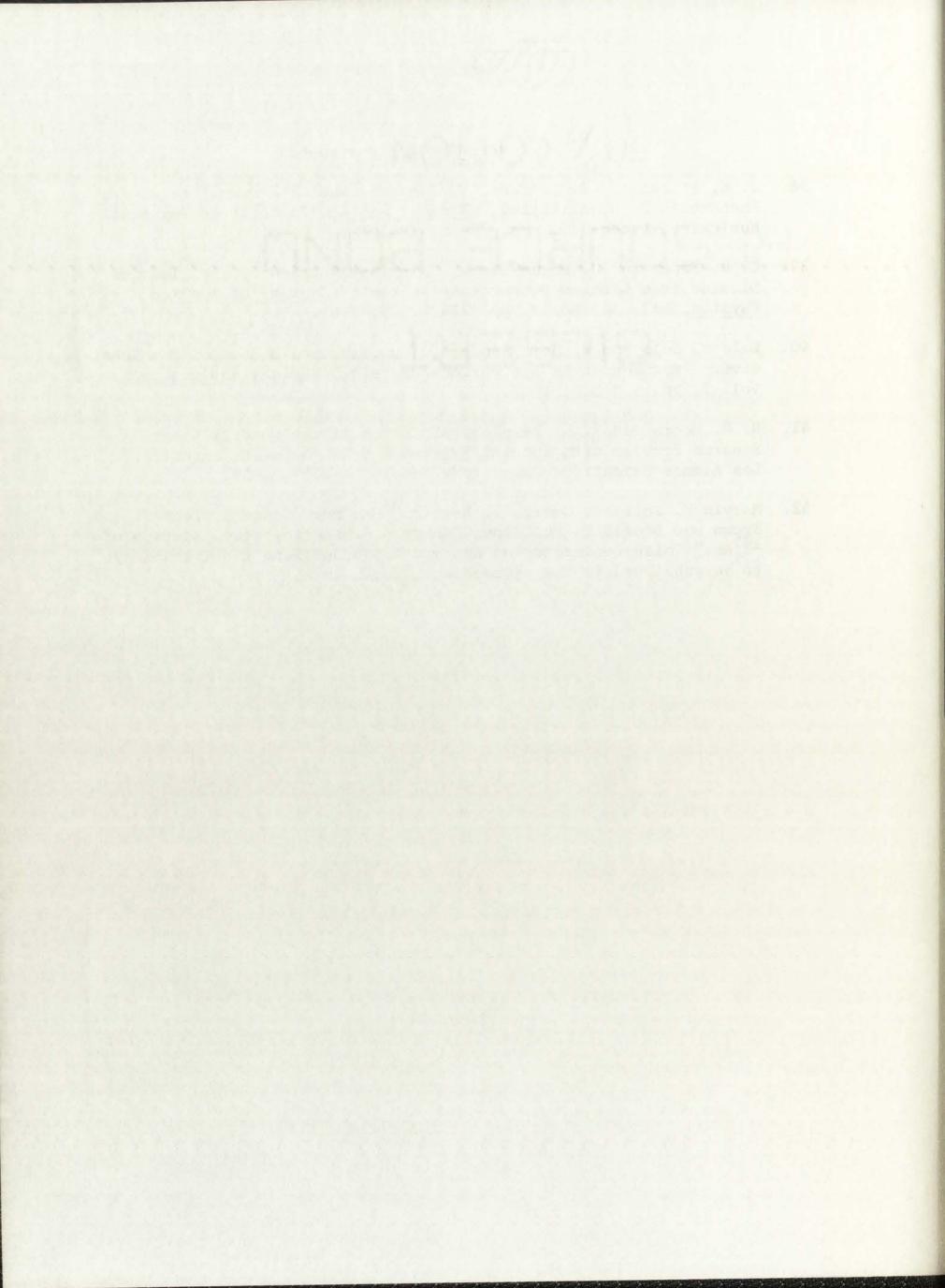
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